

2006年高考冲刺20天五套题

数学（北京卷）

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2006 年普通高等学校招生全国统一考试

数学试题(一)

参考公式:

$$\begin{aligned} P(A \cup B) &= P(A) + P(B) \\ P(A \cap B) &= P(A) \cdot P(B) \\ S &= 4\pi R^2 \\ V &= \frac{4}{3}\pi R^3 \\ p_n^k &= C_n^k p^k (1-p)^{n-k} \end{aligned}$$

一、选择题:本大题共 8 小题,每小题 5 分,共 40 分,在每小题给出的四个选项中,只有一项是符合题目要求的.

- $A - B = \{x \mid x \in A \text{ 且 } x \notin B\}$ $M = \{x \mid |x+1| \leq 2, x \in \mathbf{R}\}$
 $N = \{x \mid x = |\sin \alpha|, \alpha \in \mathbf{R}\}$ $M - N =$
 A. $[-3, 1]$ B. $[-3, 0]$ C. $[0, 1]$ D. $[-3, 0]$
- $f(x) = \begin{cases} \cos x & -\frac{\pi}{2} \leq x < 0 \\ \sin x & 0 \leq x < \pi \end{cases}$ $f(-\frac{15}{4}\pi) =$
 A. 1 B. 0 C. $\frac{\sqrt{2}}{2}$ D. $-\frac{\sqrt{2}}{2}$
- $\alpha, \beta, \gamma, l, m$ 是直线, $\alpha \perp \beta, \gamma \perp \alpha, \gamma \perp \beta, l \perp \alpha, m \perp \beta$
 $\alpha \perp \beta, \gamma \perp \alpha, \gamma \perp \beta, l \perp \alpha, m \perp \beta$
 A. ① ② B. ② ③ C. ① ③ D. ②
- O 是 $\triangle ABC$ 内一点, $\vec{OA} + \vec{OB} + \vec{OC} = \vec{0}$
 $A(3, 1), B(-1, 3), C(1, 2)$
 A. $3x + 2y - 11 = 0$ B. $x - 1^2 + y - 2^2 = 5$
 C. $2x - y = 0$ D. $x + 2y - 5 = 0$
- $\frac{1}{4} = \frac{1}{2^2}$ $\frac{1}{3} = \frac{1}{3^1}$ $\frac{1}{2} = \frac{1}{2^1}$ $\frac{1}{3} = \frac{1}{3^1}$
 A. $\frac{1}{4}$ B. $\frac{1}{3}$ C. $\frac{1}{2}$ D. $\frac{1}{3}$

$$4 \qquad 2 \qquad p$$

$$A. \frac{2}{3} \quad 1 \qquad B. \frac{1}{3} \quad 1 \qquad C. 0 \quad \frac{2}{3} \qquad D. 0 \quad \frac{1}{3}$$

$$6. \quad y = f(x) \qquad \mathbf{R} \qquad x_1' - x_2' - 1 \quad \alpha = \frac{x_1 + \lambda x_2}{1 + \lambda} \quad \beta = \frac{x_2 + \lambda x_1}{1 + \lambda}.$$

$$|f(x_1) - f(x_2)| < |f(\alpha) - f(\beta)|$$

$$A. \lambda < 0 \qquad B. \lambda = 0 \qquad C. 0 < \lambda < 1 \qquad D. \lambda (1$$

$$7. \quad F_1, F_2 \qquad \frac{x^2}{4} - y^2 = 1 \qquad P \qquad \overrightarrow{PF_1} \cdot \overrightarrow{PF_2} = 0 \quad | \overrightarrow{PF_2}$$

$$| \overrightarrow{PF_1} |$$

$$A. 2 \qquad B. 2\sqrt{2} \qquad C. 4 \qquad D. 8$$

$$O \qquad AB \qquad y^2 = 2x \qquad \overrightarrow{OA} \cdot \overrightarrow{OB} =$$

$$A. \frac{3}{4} \qquad B. -\frac{3}{4} \qquad C. 3 \qquad D. -3$$

$$8. \quad 4 \qquad A, B, C, D \qquad \overrightarrow{AB} \cdot \overrightarrow{AC} = 0 \quad \overrightarrow{AC} \cdot \overrightarrow{AD} = 0 \quad \overrightarrow{AD} \cdot \overrightarrow{AB} = 0$$

$$S_{\triangle ABC} + S_{\triangle ACD} + S_{\triangle ADB} \qquad S$$

$$A. 8 \qquad B. 16 \qquad C. 32 \qquad D. 64$$

二、填空题：本大题共 6 小题，每小题 5 分，共 30 分，把答案填在题中横线上。

$$9. \quad x, y \quad \begin{cases} 2x + y - 2 \leq 0 \\ x - 2y + 4 \leq 0 \\ 3x - y - 3 \geq 0 \end{cases} \quad z = x^2 + y^2 \quad \text{_____}.$$

$$10. \quad A_n^m = 306 \quad C_n^m = 153 \quad \sqrt[3]{x} - \frac{1}{2x} \quad x^2 \quad \text{_____}.$$

$$11. \quad a_n \qquad a_1 + a_2 + a_3 = 8 \quad a_1 + a_2 + \quad + a_6 = 7 \qquad S_n = a_1 + a_2 + \quad a_n$$

$$\lim_{n \rightarrow \infty} S_n = \text{_____}.$$

$$a_n \qquad a_1 + a_2 + a_3 = 8 \quad a_1 + a_2 + \quad + a_6 = 7 \qquad q = \text{_____}.$$

$$12. \quad F_1, F_2 \qquad \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \qquad F \qquad x$$

$$A, B \qquad * ABF_2 \qquad e \quad \text{_____}.$$

$$13. \quad y = f(x) \qquad D \qquad x \notin D \quad f_1(x) =$$

$$f(x) \cdot f_2(x) = f(f_1(x)) \qquad f_n(x) = f(f_{n-1}(x)) \quad n \in \mathbb{N}.$$

$$\textcircled{1} \quad y = f(x) = \frac{1+x}{1-3x} \quad f_8(1) = \text{_____}$$

$$\textcircled{2} \quad y = f(x) \qquad x_0 \notin D \qquad f_1(x_0) \cdot f_2(x_0) \cdot \dots \cdot f_n(x_0) = \text{_____}.$$

$$y = \sin - 2x + \frac{\pi}{3} \quad \text{_____} \quad \text{_____}.$$

$$14. P \quad ABCD \quad a \quad * PAD \quad O_1 \\ * PBC \quad O_2 \quad \text{_____}.$$

三、解答题:本大题共 6 小题,共 80 分,解答应写出文字说明、证明过程或演算步骤.

$$15. \quad 13 \\ \begin{aligned} \frac{a}{b} &= \sin \alpha - x \quad 1 \quad \frac{b}{a} = 1 - \sin \alpha + x \\ 1 \quad x &! R \quad \frac{a}{b} \quad \frac{b}{a} \quad \alpha \\ 2 \quad \sin 2\alpha &= \frac{3}{5} \quad \alpha \quad ! \quad - \frac{3\pi}{4} \quad \pi \quad f(x) = \frac{a}{b} \quad \frac{b}{a} + 2\cos\alpha \quad f(x) \quad 0 \quad \cos\alpha \\ & \end{aligned}$$

$$16. \quad 14 \\ \begin{aligned} &4 \quad 3 \quad 2 \quad 2 \quad 0 \\ &1 \quad 2 \quad \xi \\ &1 \quad \xi \\ &2 \quad \xi \end{aligned}$$

$$\begin{aligned} &0.90 \quad 0.95 \quad 0.95 \\ &1 \\ &2 \quad . \quad 0.001 \end{aligned}$$

17. 13

$$\begin{aligned} & f(x) - 1 = 1 - f(x) - g(x) \\ & 2 \cdot 3 \cdot g(x) = a(x-2) - 2(x-2)^3 - a \\ & 1 \cdot f(x) \\ & 2 \cdot f(x) = 0 \cdot 1 \\ & 3 \cdot a = -6 \cdot 6 \cdot f(x) \end{aligned}$$

4

18. 14

$P \in ABCD$ $ABCD$ $PD \perp$

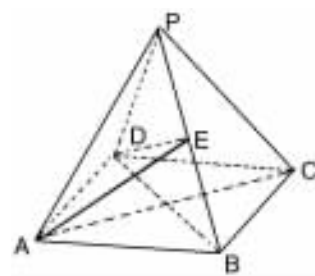
$ABCD$ $PD = AD$

1 $PAC \perp PBD$

2 $PC \perp PBD$

3 $PB \perp E$ $PC \perp ADE$

$A \perp ED \perp B$



19. 13

$$F \perp O \quad l \perp x = 2 \quad P \quad l$$

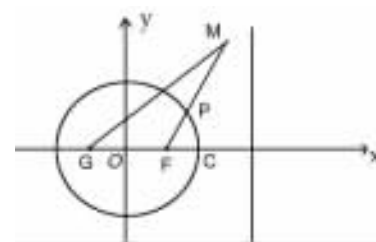
$$d \quad |PF| = \frac{\sqrt{2}}{2}d \quad \frac{2}{3} \neq d \neq \frac{3}{2}.$$

1 P

$$2 \quad \frac{PF}{OF} = \frac{1}{3} \quad \frac{OP}{OF}$$

$$3 \quad G \quad \frac{GF}{FC} = 2 \quad \frac{MC}{MP} = 3 \quad \frac{PF}{MG}$$

$$P \quad * PGF \quad .$$



20. 13

$$x_n \quad 1 \quad n \quad S_n \quad P_n \quad x_n \quad S_n$$

$$P_n \quad n = 1 \quad 2 \quad 3 \quad k \quad k' \quad 0 \quad 1$$

1 x_n

$$2 \quad y_n = \log x_n \quad 2a^2 - 3a + 1 \quad y_s = \frac{1}{2t} +$$

$$\frac{3}{2} \quad s \quad t \quad ! \quad N^+ \quad s' \quad t \quad M \quad n > M \quad x_n > 1$$

$$M \quad .$$

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数学试题(一) 参考答案

1. B. $M = \begin{pmatrix} -3 & 1 \\ 0 & 1 \end{pmatrix} \quad N = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad M - N = \begin{pmatrix} -3 & 0 \\ 0 & 0 \end{pmatrix}$

2. C. $f\left(-\frac{15}{4}\pi\right) = f\left(-\frac{15}{4}\pi + 3 \times \frac{3}{2}\pi\right) = f\left(\frac{3}{4}\pi\right) = \sin\left(\frac{3}{4}\pi\right) = \frac{\sqrt{2}}{2}$

3. D.
$$\begin{cases} \gamma \text{ } \$ \alpha \\ \gamma \% \alpha = m \\ l \text{ } \$ m \text{ } l, \gamma \end{cases} \therefore l \text{ } \$ \alpha \quad (2)$$

① ③ D.

4. D. $C \text{ } x \text{ } y \therefore \vec{OC} = \alpha \vec{OA} + \beta \vec{OB} \therefore x \text{ } y = \alpha \begin{pmatrix} 3 \\ 1 \end{pmatrix} + \beta \begin{pmatrix} -1 \\ 3 \end{pmatrix} = \begin{pmatrix} 3\alpha - \beta \\ \alpha + 3\beta \end{pmatrix}$
 $\begin{cases} 3\alpha - \beta = 3 \\ \alpha + 3\beta = 5 \end{cases} \therefore \begin{cases} x = 3\alpha - \beta \\ y = \alpha + 3\beta \end{cases} \alpha + \beta = 1 \therefore x + 2y - 5 = 0$

5. B. $p^3 - C_4^3 p^3 + 1 - p + p^4 > p^2 \quad 4p - 1 - p + p^2 > 1 \quad 3p^2 - 4p + 1 < 0 \therefore \frac{1}{3} < p < 1$

6. A. $y = f(x) = x \quad |x_1 - x_2| < \left| \frac{x_1 + \lambda x_2}{1 + \lambda} - \frac{x_2 + \lambda x_1}{1 + \lambda} \right| = \left| \frac{x_1 - x_2}{1 + \lambda} \right|$
 $\therefore |x_1 - x_2| < \left| \frac{x_1 - x_2}{1 + \lambda} \right| \therefore \left| \frac{1 - \lambda}{1 + \lambda} \right| > 1 \therefore \lambda < 0$

7. $A \quad \vec{PF_1} \cdot \vec{PF_2} = 0 \therefore PF_1 \perp PF_2 \therefore |PF_1|^2 + |PF_2|^2 = 4a^2 \quad (1)$
 $|PF_1|^2 + |PF_2|^2 = 4c^2 \quad (2) \quad (2) - (1) \quad 2|PF_1| \cdot |PF_2| = 4b^2 \quad b^2 = 1$
 $\therefore |PF_1| \cdot |PF_2| = 2 \quad A$

B. $AB \quad A\left(\frac{1}{2}, 1\right) \quad B\left(\frac{1}{2}, -1\right) \therefore \vec{OA} = \left(\frac{1}{2}, 1\right) \quad \vec{OB} = \left(\frac{1}{2}, -1\right)$
 $\therefore \vec{OA} \cdot \vec{OB} = -\frac{3}{4} \quad B$

8. C. $AB \quad AC \quad AD \quad AB^2 + AC^2 + AD^2 = 2r^2 = 64$
 $S_{\triangle ABC} + S_{\triangle ACD} + S_{\triangle ADB} = \frac{1}{2}AB \times AC + \frac{1}{2}AC \times AD + \frac{1}{2}AD \times AB = \frac{AB^2 + AC^2}{4} + \frac{AC^2 + AD^2}{4} + \frac{AD^2 + AB^2}{4} = \frac{AB^2 + AC^2 + AD^2}{2} = 32 \quad AB = AC = AD$

$$9. \frac{4}{5}. \quad z \quad 2x + y - 2 = 0$$

$$10. -102. \quad C_n^m = 153 \quad A_n^m = 306 \quad n = 18 \quad T_{r+1} = C_{18}^r x^{\frac{1}{3}} 18-r - \frac{1}{2x} r = -\frac{1}{2} r$$

$$C_{18}^r x^{6-\frac{4}{3}r} \therefore 6 - \frac{4}{3}r = 2 \therefore r = 3. T = -\frac{1}{2} {}^3C_{18}^3 = -102$$

$$11. \quad \frac{64}{9}. \quad a_n \quad q \quad a_1 + a_2 + a_3 + \dots + a_6 = a_1 + a_2 + a_3 + q^3 a_1 +$$

$$a_2 + a_3 = 1 + q^3 \quad a_1 + a_2 + a_3 = 8 \quad 1 + q^3 = 7 \therefore q = -\frac{1}{2} \therefore a_1 + a_2 + a_3 = a_1 -$$

$$\frac{1}{2}a_1 + \frac{1}{4}a_1 = 8 \therefore \lim_{n \rightarrow \infty} S_n = \frac{a_1}{1-q} = \frac{64}{9}.$$

$$-\frac{1}{2}$$

$$12. 1 < e < 1 + \sqrt{2}. \quad A\left(-c \frac{b^2}{a}\right) \quad -AF_2F_1 = -BF_2F_1 \quad *ABF_2$$

$$-AF_2B \quad . \quad -AF_2F_1 < 45^\circ \therefore |AF_1| < |F_1F_2| \therefore \frac{b^2}{a} < 2c$$

$$\therefore b^2 < 2ac \therefore c^2 - a^2 - 2ac < 0 \therefore e^2 - 2e - 1 < 0 \quad e > 1 \therefore 1 < e < 1 + \sqrt{2}.$$

$$13. \quad \textcircled{1} 0 \quad \textcircled{2} \sin \pi x = 1 - x \quad f(x) = -1 - x \quad x_0 = 0 \quad f(x) = \sin \pi x \quad x_0 = 0.5.$$

$$x = \frac{k}{2}\pi - \frac{\pi}{12} \quad k \in \mathbb{Z} \quad k\pi + \frac{5\pi}{12} \quad k\pi + \frac{11\pi}{12} \quad k \in \mathbb{Z}$$

$$-2x + \frac{\pi}{3} = k\pi + \frac{\pi}{2} \quad k \in \mathbb{Z} \quad x = \frac{k}{2}\pi - \frac{\pi}{12} \quad k \in \mathbb{Z}$$

$$\therefore y = \sin(-2x + \frac{\pi}{3}) = -\sin(2x - \frac{\pi}{3}) \quad \sin(2x - \frac{\pi}{3})$$

$$\therefore 2k\pi + \frac{\pi}{2} \neq 2x - \frac{\pi}{3} \neq 2k\pi + \frac{3}{2}\pi \quad k \in \mathbb{Z} \therefore x \neq k\pi + \frac{5}{12}\pi \quad k\pi + \frac{11}{12}\pi \quad k \in \mathbb{Z}$$

$$14. a.$$

$$15. 1 \therefore \frac{a}{b} = 0 \quad \sin(\alpha - x) - \sin(\alpha + x) = 0 \therefore \cos \alpha \sin x = 0 \quad \therefore x \in \mathbb{R} \therefore \cos \alpha = 0 \therefore \alpha = k\pi + \frac{\pi}{2} \quad k \in \mathbb{Z}$$

$$2 f(x) = -2\cos \alpha \sin x + 2\cos \alpha = 2\cos \alpha (1 - \sin x) \therefore f(x) = 0 \therefore \cos \alpha < 0$$

$$\therefore \sin 2\alpha = 2\sin \alpha \cos \alpha > 0 \therefore \sin \alpha < 0 \therefore \alpha \in (-\frac{3\pi}{4}, -\frac{\pi}{2}) \therefore 2\alpha \in (-\frac{3}{2}\pi, -\pi)$$

$$\therefore \cos 2\alpha < 0 \therefore \cos 2\alpha = -\frac{4}{5} \therefore \cos \alpha = -\sqrt{\frac{1 + \cos 2\alpha}{2}} = -\frac{\sqrt{10}}{10}.$$

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$$\begin{aligned}
16. \quad \xi \quad 0 \ 1 \ 2 \ 3 \ 4 \ P \ \xi = 0 &= \frac{C_4^2}{C_9^2} = \frac{1}{6} \\
P \ \xi = 1 &= \frac{4 \times 3}{C_9^2} = \frac{1}{3} \quad P \ \xi = 2 = \frac{4 \times 2}{C_9^2} + \frac{C_3^2}{C_9^2} = \frac{11}{36} \\
P \ \xi = 3 &= \frac{3 \times 2}{C_9^2} = \frac{1}{6} \quad P \ \xi = 4 = \frac{C_2^2}{C_9^2} = \frac{1}{36}. \\
2 \ E\xi &= 0 \times \frac{1}{6} + 1 \times \frac{1}{3} + 2 \times \frac{11}{36} + 3 \times \frac{1}{6} + 4 \times \frac{1}{36} = \frac{14}{9}.
\end{aligned}$$

$$\begin{array}{ccccccc}
 & & & & A & B & C \\
 1 & P(A) & = 0.90 & P(B) & = P(C) & = 0.95 & p(\bar{A}) = 0.10 & P(\bar{B}) = P(\bar{C}) = 0.05 \\
 & & & & A & B & C \\
 & & & & P(A) & B & \bar{C} & + P(A) & \bar{B} & C
 \end{array}$$

$$\begin{aligned}
& + \\
& P \bar{A} B C = P A P B P \bar{C} + P A P \bar{B} P C + P \bar{A} P B P C \\
& = 0.176.
\end{aligned}$$

$$2 \quad P \bar{A} \bar{B} \bar{C} + P \bar{A} B \bar{C} + P A \bar{B} \bar{C} + P \bar{A} \bar{B} \bar{C} = 0.012$$

$$\begin{aligned}
 17. \quad & \begin{aligned} & \vdots f x \quad g x \quad x = 1 \quad \vdots f x = g 2 - x . \\ & \vdots x ! - 1 0 \quad 2 - x ! 2 3 \quad \vdots f x = g 2 - x = -ax + 2x^3 \\ & \vdots f x \quad \vdots x ! 0 1 \quad -x ! - 1 0 \quad \vdots f x = f - x = ax - 2x^3 . \\ & \vdots f x = \begin{cases} -ax + 2x^3 & -1 \# x < 0 \\ ax - 2x^3 & 0 \# x \# 1 \end{cases} \end{aligned} \\
 2 \quad & \begin{aligned} & \vdots f x \quad 0 1 \quad \vdots f' x = a - 6x^2 \quad (0 : a (6x^2 \quad 0 1 \quad \vdots : x \\ & ! 0 1 \quad 6x^2 \# 6 : a (6 \quad a ! 6 + \infty . \end{aligned}
 \end{aligned}$$

$$3 \quad f(x) = x^2 - 2x + 1 \quad f'(x) = 2x - 2 \quad x = \sqrt{\frac{a}{6}} \quad f\left(\sqrt{\frac{a}{6}}\right) = 4 \quad a = 6$$

$$6 \quad x = 1 \quad a ! \quad -6 \quad 6 \quad f \quad x \quad 4.$$

18. $1 \quad \therefore PD \ \$ \quad ABCD \therefore AC \ \$ \ PD \quad \therefore \quad ABCD \quad \therefore AC \ \$ \ BD \quad AC ,$
 $PBD \therefore \quad PAC \ \$ \quad PBD.$

$$\begin{array}{cccccccccccc} 2 & AC & BD & & O & PO & 1 & AC & \$ & PBD \therefore PC & PBD & PO \\ \therefore - CPO & PC & PBD & & & & \therefore PD = AD \therefore & Rt \star PDC & PC = \sqrt{2} CD \end{array}$$

$$ABCD \quad OC = \frac{1}{2}AC = \frac{\sqrt{2}}{2}CD \therefore Rt \triangle POC \quad - \angle CPO = 30^\circ \quad PC \quad PBD$$

$$\begin{array}{ccccccccccc} 3 & PBD & DE & \$ PO & PB & E & AE & PC & \$ & ADE \\ 1 & AC & \$ & PBD & \therefore AC & \$ DE & PO & AC & & O & \therefore DE & \$ & PAC & \therefore DE \end{array}$$

$$\angle PCP = \angle PDC = \angle ABCD \therefore \angle PCP = \angle PDC$$

$$\therefore \angle PCP = \angle PDC \therefore \angle PCP = \angle PDC \therefore \angle PCP = \angle PDC \therefore \angle PCP = \angle PDC$$

$$PC = PD = a$$

$$Rt \triangle PDC \quad OF = \frac{\sqrt{6}}{6}a \quad AO = \frac{\sqrt{2}}{2}a \therefore Rt \triangle AOF \quad - \angle OFA = 60^\circ$$

$$\angle AED = 60^\circ.$$

$$19. \quad \frac{|PF|}{d} = \frac{\sqrt{2}}{2} < 1 \therefore P \quad F \quad l \quad x = 2$$

$$\begin{cases} e = \frac{c}{a} = \frac{\sqrt{2}}{2} \\ \frac{a^2}{c} - c = 1 \end{cases} \quad \begin{cases} a = \sqrt{2} \therefore b = 1 \\ c = 1 \end{cases} \therefore \frac{2}{3} \neq d \neq \frac{3}{2}$$

$$\therefore \frac{2}{3} \neq |2-x| \neq \frac{3}{2} \quad \frac{2}{3} \neq 2-x \neq \frac{3}{2} \therefore \frac{1}{2} \neq x \neq \frac{4}{3}$$

$$\therefore P \quad \frac{x^2}{2} + y^2 = 1 \quad \frac{1}{2} \neq x \neq \frac{4}{3}$$

$$2 \therefore \vec{PF} = 1-x-y \quad \vec{OF} = 1 \quad \vec{OP} = x-y \therefore \vec{PF} \cdot \vec{OF} = 1-x-1+y=0=1-x=\frac{1}{3}$$

$$\therefore x = \frac{2}{3} \quad \frac{x^2}{2} + y^2 = 1 \quad y = \pm \frac{\sqrt{7}}{3} \therefore \vec{OP} = \frac{2}{3} \frac{\sqrt{7}}{3} \quad \vec{OP} = \frac{2}{3} - \frac{\sqrt{7}}{3}$$

$$\therefore \cos \angle OPF = \frac{\vec{OP} \cdot \vec{OF}}{|\vec{OP}| |\vec{OF}|} = \frac{2\sqrt{11}}{11} \therefore \angle OPF = \arccos \frac{2\sqrt{11}}{11}$$

$$3 \quad |\vec{GF}| = 2 \quad |\vec{FC}| = 2 \therefore G$$

$$\therefore \begin{cases} |\vec{PG}| = |\vec{PM}| = 3 \quad |\vec{PF}| \\ |\vec{PG}| + |\vec{PF}| = 2 \times \sqrt{2} \end{cases} \therefore \begin{cases} |\vec{PF}| = \frac{\sqrt{2}}{2} \\ |\vec{PG}| = \frac{3\sqrt{2}}{2} \end{cases}$$

$$\therefore |\vec{GF}| = 2 \therefore |\vec{PF}|^2 + |\vec{GF}|^2 = |\vec{PG}|^2 \therefore \angle PGF = Rt \angle$$

$$\therefore S = \frac{1}{2} |\vec{GF}| \times |\vec{PF}| = \frac{\sqrt{2}}{2}.$$

$$20. \quad 1 \therefore P_n = P_{n+1} \quad k \therefore \frac{S_{n+1} - S_n}{x_{n+1} - x_n} = k \quad k-1 \quad x_{n+1} = kx_n \therefore k'$$

$$0 \quad x_{n+1} \neq 1 \quad x_n \neq 1 \therefore \frac{x_{n+1}}{x_n} = \frac{k}{k-1} = \therefore x_n = \frac{k}{k-1}.$$

$$\begin{aligned}
& 2 \quad 1 < a < \frac{3}{2} \quad 0 < 2a^2 - 3a + 1 < 1 \quad \frac{1}{y_{n+1}} - \frac{1}{y_n} \quad \frac{1}{y_n} \\
& \quad \quad \quad - 2 \quad \quad \quad \therefore \quad M \quad \begin{cases} \frac{1}{y_m} > 0 \\ \frac{1}{y_{m+1}} < 0 \end{cases} \\
& \begin{cases} 2s + t - 1 - 2M - 1 > 0 \\ 2s + t - 1 - 2M + 1 < 0 \end{cases} \\
& \therefore s + t - \frac{1}{2} < M < s + t + \frac{1}{2} \quad \because M \in \mathbb{N}^+ \quad \therefore M = s + t \quad \therefore \quad n > M \quad \frac{1}{y_n} \neq \frac{1}{y_{m+1}} \neq 0 \\
& \because 0 < 2a^2 - 3a + 1 < 1 \quad \therefore \quad n > m \quad x_n = 2a^2 - 3a + 1^{\frac{1}{y_n}} > 1 \\
& \therefore \quad M = s + t \quad n > m \quad x_n > 1.
\end{aligned}$$

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数学试题(二)

参考公式：

$$\begin{aligned} P(A \cap B) &= P(A) + P(B) & S &= 4\pi R^2 \\ P(A \cup B) &= P(A) - P(B) & R & \\ P_n^k &= C_n^k p^k (1-p)^{n-k} & V &= \frac{4}{3}\pi R^3 \end{aligned}$$

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一、选择题：本大题共 8 小题，每小题 5 分，共 40 分，在每小题给出的四个选项中，只有一项是符合题目要求的。

- $z = 2 + i, z = 1 + 2i$
 A. $\sin^4 \theta + \cos^4 \theta = \frac{5}{9}$
 B. $\sin 2\theta$
 C. $\frac{2}{3}$
 D. $-\frac{2}{3}$
- $f(x) = x^2 - 4x + 3, M = \{x | f(x) + f(y) \neq 0\}, N = \{x | f(x) - f(y) = 0\}$
 A. $\frac{\pi}{4}$
 B. $\frac{\pi}{2}$
 C. π
 D. 2π
- $a, b, c \in \mathbb{R}, a \neq b, a \neq c, b \neq c$
 $a/b < c/a, b/a < c/b, a/c < b/a, b/c < a/b$
 A. ① ②
 B. ② ③
 C. ② ④
 D. ③ ④
- F_1, F_2
 $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1, a > 0, b > 0$
 $\frac{|PF_2|^2}{|PF_1|} = 8a$
 A. $\frac{2\sqrt{2}}{3}$
 B. $-\frac{2\sqrt{2}}{3}$
 C. $\frac{2}{3}$
 D. $-\frac{2}{3}$

- A. $1 + \infty$ B. 0.3 C. 1.3 D. 1.2
5. $\begin{matrix} \vec{e}_1 = 1 & 0 \\ \vec{e}_2 = 0 & 1 \end{matrix}$ $P = P_0 - 1.2$ $\begin{matrix} \vec{e}_1 + \vec{e}_2 \\ | \vec{e}_1 + \vec{e}_2 | \end{matrix}$ $Q = Q_0 - 2 - 1$ $\begin{matrix} 3\vec{e}_1 + 2\vec{e}_2 \\ | 3\vec{e}_1 + 2\vec{e}_2 | \end{matrix}$ $P \cdot Q$ $t = 0$
- $PQ \cdot P_0Q_0 = t$
- A. 1 B. 2 C. 3 D. 4
6. $f(x) = R$ $x \in R$ $f(x+6) = f(x) + f(3)$ $f(2) = 1$
- $f(2006) =$
- A. 2006 B. 2 C. 1 D. 0
7. $P - ABC = M \cdot N$ $PB \cdot PC$ $AM \cdot N \cdot PBC$
- A. $\frac{\sqrt{3}}{2}$ B. $\sqrt{2}$ C. $\frac{\sqrt{5}}{2}$ D. $\frac{\sqrt{6}}{2}$
8. R $f(x) = \begin{cases} |\lg|x-1|| & |x| \neq 1 \\ 0 & x = 1 \end{cases}$ x $f^2(x) + bf(x) + c =$
- $0 \leq 7$
- A. $b < 0, c > 0$ B. $b > 0, c < 0$
- C. $b < 0, c = 0$ D. $b \geq 0, c = 0$

二、填空题：本大题共 6 小题，每小题 5 分，共 30 分，把答案填在题中横线上。

9. $y = 2^{1-x} + 3, x \in R$ _____.
10. $f'(x_0) = 2$ $\lim_{k \rightarrow 0} \frac{f(x_0 + k) - f(x_0)}{2k} =$ _____.
- $\left(x^3 + \frac{1}{x^2}\right)^n$ 6 _____.
11. R 45° 120° 75° 120°
- _____.
12. $f(x) = 2x^3 - 6x^2 + m, m$ -2.2 3 $m =$ _____.
- -2.2 _____.
13. $f(x) = R$ $m > 0$ $|f(x)| \neq m|x|$ x
- $f(x) = F$
- ① $f(x) = 0$ ② $f(x) = x^2$ ③ $f(x) = \sqrt{2} \sin x + \cos x$ ④ $f(x) = \frac{x}{x^2 + x + 1}$ ⑤ $f(x)$
- R x_1, x_2 $|f(x_1) - f(x_2)| \neq 2|x_1 - x_2|$.
- F _____.
14. F_1, F_2 C F_1 F_2 C
- P C e $|PF_1| = e|PF_2|$ e _____.

三、解答题:本大题共 6 小题,共 80 分. 解答应写出文字说明,证明过程或演算步骤.

15. $\frac{13}{2} \sin A \cos B \cos C - \frac{1}{2} (a^2 \cos B + b^2 \cos A + c^2 \cos C) = S_1$

$\left(\tan \frac{C}{2} + \cot \frac{C}{2} \right) S = 18.$

$\frac{1}{2} ab \sin C = 3\sqrt{2} \sin C.$

16. 14

	0 ~ 5	6 ~ 10	11 ~ 15	16 ~ 20	21 ~ 25	25
	0.1	0.15	0.25	0.25	0.2	0.05

$\frac{1}{2} \times 20 \times 7 \times 3 \times 15 = 0.75$

17.

13

$$a_n \quad n \quad S_n = \frac{1}{2} n^2 - n + 2 \quad b_n \quad b_1 = 1 \quad b_n - b_{n-1} =$$

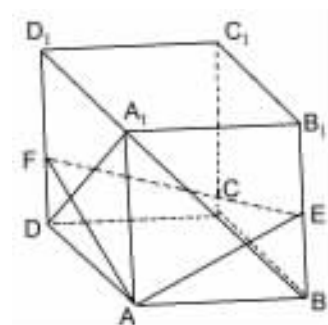
$$\frac{1}{2^{n-1}} n (2$$

$$\begin{matrix} 1 & a_n & b_n \\ 2 & & n \end{matrix} \quad n_0 \quad n \quad a_n > 5b_n.$$

18.

14

$$\begin{matrix} & & ABCD - A_1B_1C_1D_1 & & \sqrt{3} \\ 3 & EF & BB_1 DD_1 & AE \text{ \textcircled{A} } A_1B & AF \text{ \textcircled{A} } A_1D. \\ 1 & A_1C \text{ \textcircled{A} } & AEF \\ 2 & A - EF - B \\ 3 & B_1 & AEF & . \end{matrix}$$



19. 13 $\mathbf{R}$ $f(x) = ax^3 - 2bx^2 + cx + 4d$ $a, b, c, d \in \mathbf{R}$

$$f(1) = f(x) - \frac{2}{5}.$$

1 $f(x)$

2 $x \in [-1, 1]$

3 $x_1, x_2 \in [-1, 1] \quad |f(x_1) - f(x_2)| \leq \frac{4}{5}.$

20. 13 $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ $a > 0, b > 0$ A, B F, c

0 $c > 0$ $l(x) = \frac{1}{2} \quad |AF| = 3, \quad F$ P, Q

PB l M .

I

II $\overrightarrow{OP} \cdot \overrightarrow{OQ} = -17$ ΔPBQ S

III $\overrightarrow{PF} = \lambda \overrightarrow{FQ}$ $\lambda' = 0, \lambda' = -1$ $\mu = f(\lambda)$ $\overrightarrow{AM} = \mu \overrightarrow{MQ}.$

$\overrightarrow{PF} = 2 \overrightarrow{FQ}$ μ $\overrightarrow{AM} = \mu \overrightarrow{MQ}.$ μ

班 级

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