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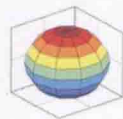
# 控制理论 MATLAB教程

MATLAB for Control Engineers

英文版

[美] Katsuhiko Ogata 著

MATLAB<sup>®</sup>  
FOR  
CONTROL  
ENGINEERS



KATSUHIKO OGATA



电子工业出版社  
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# 控制理论 MATLAB 教程

(英文版)

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[美] Katsuhiko Ogata 著

電子工業出版社

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## 内 容 简 介

本书系统讲述基于 MATLAB 的控制系统分析和设计方法。全书共 7 章。第 1 章总体介绍了 MATLAB 的基本命令;第 2 章介绍了 MATLAB 分析和设计控制系统的预备知识;第 3 章讨论了如何应用 MATLAB 获得动态系统的瞬态响应;第 4 章和第 5 章分别讲解了如何运用 MATLAB 进行根轨迹和频域方法的分析和设计;第 6 章讨论了如何通过 MATLAB 处理状态空间极点配置和观测器设计问题;第 7 章提供了控制系统设计中最优参数组的选取方法及二次型最优控制器的求解方法。

本书的主要读者为自动化专业的本科生、控制科学与工程专业的研究生和从事控制领域工作的科研人员和工程师。

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# 出版说明

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当前,正值我国高等教育特别是信息科学领域的教育调整、变革的重大时期,为使我国教育体制与国际化接轨,有条件的高等院校正在为某些信息学科和技术课程使用国外优秀教材和优秀原版教材,以使我国在计算机教学上尽快赶上国际先进水平。

电子工业出版社秉承多年来引进国外优秀图书的经验,翻译出版了“国外计算机科学教材系列”丛书,这套教材覆盖学科范围广、领域宽、层次多,既有本科专业课程教材,也有研究生课程教材,以适应不同院系、不同专业、不同层次的师生对教材的需求,广大师生可自由选择和自由组合使用。这些教材涉及的学科方向包括网络与通信、操作系统、计算机组织与结构、算法与数据结构、数据库与信息处理、编程语言、图形图像与多媒体、软件工程等。同时,我们也适当引进了一些优秀英文原版教材,本着翻译版本和英文原版并重的原则,对重点图书既提供英文原版又提供相应的翻译版本。

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# 导 读

一个偶然的机，我们阅读了 Ogata 教授所著新书 *MATLAB for Control Engineers*，甚感欣喜。*MATLAB* 语言业已成为控制领域最流行的仿真语言，也是该领域最流行的控制系统分析与设计的计算机辅助工具。目前，*MATLAB* 已被融于控制理论的教学，有些学校甚至专门开设了关于 *MATLAB* 应用的课程。本书正是一本不可多得的 *MATLAB* 控制理论教程和参考书。

控制类专业的读者在初次接触 *MATLAB* 时，通过两种方法都能学会使用 *MATLAB*。一种方法是基本按照 MathWorks 公司提供的 *MATLAB* 使用手册，特别是控制系统工具箱手册中的内容，全面地、分门别类地学习 *MATLAB* 命令。在经过较长时间的练习后，读者会比较全面地掌握 *MATLAB* 的知识。但是，在按照 *MATLAB* 手册的体系进行学习的过程中，读者往往会感觉内容繁杂并且体系庞大。另一种方法是在简单了解 *MATLAB* 的基本概念后，按照控制理论中需要解决的问题来学习和使用有关的命令。由于马上就能解决迫切需要解决的问题，读者立即会对要学的内容产生极大的兴趣。通过较短时间的练习，读者就会熟悉相当数量的关键命令；举一反三，也就能很快掌握采用 *MATLAB* 解决控制理论问题的能力。这本教材采用的正是后一种方法。

*MATLAB* 教程比比皆是，而介绍如何运用 *MATLAB* 软件解决控制问题的书籍却不多见。由于 *MATLAB* 已经成为一个庞大的仿真软件，所以让读者在有限的时间内掌握这种软件，并运用其分析、理解和解决控制理论问题，一直是控制专业类师生及应用人员的迫切愿望。所幸的是，本书将 *MATLAB* 的介绍和控制理论的学习有机地融合在一起，对需要掌握的 *MATLAB* 内容及其深度也把握得恰到好处。读者很容易通过本书来运用 *MATLAB* 解决控制问题，而不会被“淹没”到软件的庞大体系之中。

Ogata 教授所著的 *Modern Control Engineering* 一书已成为控制理论的最经典教材之一，据悉其第五版将于 2009 年问世。这本 *MATLAB* 教材的编排与 Ogata 的现代控制工程教材同步。读者一打开本书，就会有一种似曾相识的亲切感，也许就会有继续研读的愿望。书中除了开篇关于 *MATLAB* 基本内容的介绍之外，其他章节的安排基本上与 *Modern Control Engineering* 一一对应，覆盖了系统建模、瞬态响应分析、根轨迹分析、频域分析以及状态空间控制系统设计方法和优化问题。因此，本书基本上按照控制理论的体系来安排全书内容，体现了控制理论为主体，*MATLAB* 为辅助工具的思想。这种编排方式便于学生同步学习或针对特定控制问题寻求 *MATLAB* 处理方法。

本书的主要目的是讲述如何使用MATLAB命令分析和解决控制问题,但书中也较为全面地介绍了控制理论的基本概念和理论,并以MATLAB命令对例题进行全面的分析和求解,所以读者会感到书中的内容特别具有针对性。因此,通过对本书的学习不仅能够掌握利用MATLAB进行控制系统仿真的技能,而且能够加深对控制理论中基本概念的理解,培养控制系统分析和设计的能力。

正是由于本书的上述特点,相信很多读者都会开卷有益。本书不仅可以作为控制系统仿真课程的教材,也可以作为本科生或研究生自动控制原理课程的辅助教材。本书深入浅出的写作风格也使它成为从事控制领域工作的科研人员和工程技术人员的自学用书和参考手册。

清华大学 王诗宓 王峻



# Preface

This book is written to assist those students and practicing engineers who wish to study MATLAB to solve control engineering problems. It is written at the level of the senior engineering student.

The book is organized into seven chapters. Chapter 1 presents an introduction to MATLAB. Chapter 2 deals with preliminary materials that the reader must know prior to applying MATLAB to the analysis and design of control systems. Chapter 3 is a detailed discussion of how to apply MATLAB to obtain transient response outputs of dynamic systems to time-domain inputs. Chapter 4 treats root-locus analysis and design with MATLAB. Detailed frequency-response analysis and design with MATLAB are given in Chapter 5. Chapter 6 discusses state-space design problems, such as pole placement and state observers, solved with MATLAB. Finally, Chapter 7 presents a computational approach to obtaining optimal sets of parameter values in connection with control systems design. The book concludes with a discussion of MATLAB's approach to solving quadratic optimal control problems.

The book includes some of the MATLAB materials presented in my previous publications *Modern Control Engineering* (4th ed.) and *System Dynamics* (4th ed.).

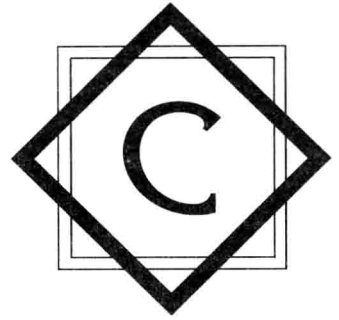
All sample problems discussed in the book are given detailed explanations so that the reader will acquire a good understanding of MATLAB's approach to solving the analysis and design problems presented.

The book assumes that the reader has a relatively new version of MATLAB in his or her computer. In plotting root-locus diagrams or Nyquist diagrams with MATLAB, the reader's grid command may produce grid lines or curves different from those presented here; it all depends on the version of MATLAB. (For problems that may arise with regard to grid lines or curves, see the appendix.)

It is hoped that the reader will find this book useful in applying MATLAB to solve many control engineering problems.

KATSUHIKO OGATA





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# Introduction to MATLAB

## 1-1 INTRODUCTION

MATLAB<sup>®</sup> is a matrix-based system for performing mathematical and engineering calculations. We may think of MATLAB as a language of technical computing. All variables handled in MATLAB are matrices. That is, MATLAB has only one data type: a matrix, or rectangular array, of numbers. MATLAB has an extensive set of routines for obtaining graphical outputs.

This section presents background material necessary for the effective use of MATLAB in solving control engineering problems. First, we introduce MATLAB commands and mathematical functions. Then we present matrix operators, relational and logical operators, and special characters used in MATLAB. Finally, we introduce the semicolon operator, MATLAB ways to enter vectors and matrices into the computer, the colon operator, and other important material that we must become familiar with before writing MATLAB programs to solve control engineering problems.

MATLAB is used with a variety of toolboxes. (A toolbox is a collection of special files called M-files.) For control systems analysis and design, MATLAB is used with the control system toolbox. When we refer to MATLAB in this book, we include the basic programs of MATLAB and the control system toolbox.

MATLAB is basically command driven. Therefore, the user must know the commands that are used in solving computational problems. Table 1-1 lists various types of MATLAB commands and predefined functions that are frequently utilized in solving control engineering problems.

**Table 1–1** MATLAB Commands and Matrix Functions

Commands and Matrix Functions Commonly Used in Solving Control Engineering Problems	Explanations of What Commands Do and Matrix Functions Mean
abs acker  angle ans atan axis	Absolute value, complex magnitude. Compute a state-feedback gain matrix for pole placement, using Ackermann's formula. Phase angle. Answer when expression is not assigned. Arctangent. Manual axis scaling.
bode	Plot Bode diagram.
clear clf computer conj conv corrcoef cos cosh cov ctrb c2d	Clear workspace. Clear current figure. Type of computer. Complex conjugate. Convolution, multiplication. Correlation coefficients. Cosine. Hyperbolic cosine. Covariance. Compute the controllability matrix. Conversion of continuous-time models to discrete-time models.
deconv det diag	Deconvolution, division. Determinant. Diagonal matrix.
eig end  exit exp expm eye	Eigenvalues and eigenvectors. Terminate scope of for, while, switch, try, and if statements. Terminate program. Exponential base $e$ . Matrix exponential. Identity matrix.
feedback filter for  format long  format long e  format short	Feedback connection of two LTI models. Direct filter implementation. Repeat statement(s) a specified number of times. Fifteen-digit scaled fixed point. (Example: 1.33333333333333) Fifteen-digit floating point. (Example: 1.33333333333333e + 000) Five-digit scaled fixed point. (Example: 1.3333)

**Table 1-1** (continued)

Commands and Matrix Functions Commonly Used in Solving Control Engineering Problems	Explanations of What Commands Do and Matrix Functions Mean
format short e  freqs freqz	Five-digit floating point. (Example: 1.3333e + 000) Laplace transform frequency response. z-Transform frequency response.
gram grid grid off  grid on	Controllability and observability gramians. Toggles the major lines of the current axes. Removes major and minor grid lines from the current axes. Adds major grid lines to the current axes.
help hold hold off   hold on	Lists all primary help topics. Toggles the hold state. Returns to the default mode whereby plot commands erase the previous plots and reset all axis properties before drawing new plots. Holds the current plot and all axis properties so that subsequent graphing commands add to the existing graph.
i imag impulse inf inv	$\sqrt{-1}$ Imaginary part. Impulse response of LTI models. Infinity ( $\infty$ ) Inverse
j	$\sqrt{-1}$
legend length linspace load log loglog logm logspace log10 lqe lqr lsim  lyap	Graph legend. Length of vector. Linearly spaced vector. Load workspace variables from disk. Natural logarithm. Loglog $x$ - $y$ plot. Matrix logarithm. Logarithmically spaced vector. Log base 10. Linear quadratic estimator design. Linear quadratic regulator design. Simulate time response of LTI models to arbitrary inputs. Solve continuous-time Lyapunov equations.

**Table 1–1** (continued)

Commands and Matrix Functions Commonly Used in Solving Control Engineering Problems	Explanations of What Commands Do and Matrix Functions Mean
margin  max mean median mesh min minreal	Gain and phase margins and crossover frequencies. Maximum value. Mean value. Median value. Three-dimensional mesh surface. Minimum value. Minimal realization and pole–zero cancellation.
NaN ngrid nichols num2str nyquist	Not a number. Generate grid lines for a Nichols plot. Draw the Nichols plot of the LTI model. Convert number to string. Plot Nyquist frequency response.
obsv ode45    ode23  ode113  ones ord2	Compute the observability matrix. Solve nonstiff differential equations, medium-order method. (If time constants involved do not vary by several orders of magnitude or more, the differential equations are called nonstiff differential equations.) Solve nonstiff differential equations, low-order method. Solve nonstiff differential equations, variable-order method. Constant. Generate continuous-time second-order system.
pade parallel pi place  plot polar pole poly polyfit polyval polyvalm printsys prod pzmap	Pade approximation of time delays. Parallel interconnection of two LTI models. $Pi(\pi)$ . Compute a state-feedback gain matrix for pole placement. Linear $x$ – $y$ plot. Polar plot. Compute the poles of LTI models. Convert roots to polynomial. Polynomial curve fitting. Polynomial evaluation. Matrix polynomial evaluation. Print system in pretty format. Product of elements. Pole–zero map of LTI models.

**Table 1–1** (continued)

Commands and Matrix Functions Commonly Used in Solving Control Engineering Problems	Explanations of What Commands Do and Matrix Functions Mean
quit	Terminate program
rand rank real rem residue rlocfind rlocus rmodel  roots	Generate random numbers and matrices. Calculate the rank of a matrix. Real part. Remainder after division. Partial-fraction expansion. Find root-locus gains for a given set of roots. Plot root loci. Generate random stable continuous-time $n$ th-order test models. Polynomial roots.
semilogx semilogy series shg sign sin sinh size sqrt sqrtm ss  ss2tf  std step subplot sum switch	Semilog $x$ - $y$ plot ( $x$ -axis logarithmic). Semilog $x$ - $y$ plot ( $y$ -axis logarithmic). Interconnect two LTI models in series. Show graph window. Signum function. Sine. Hyperbolic sine. Size of matrix. Square root. Matrix square root. Create state-space model or convert LTI model to state-space model. Convert state-space model to transfer-function model. Standard deviation. Plot unit-step response. Create axes in tiled positions. Sum of elements. Switch among several cases, based on expression.
tan tanh text tf  tf2ss  tf2zp  title trace	Tangent. Hyperbolic tangent. Arbitrarily positioned text. Create transfer-function model or convert LTI model to transfer-function model. Convert transfer-function model to state-space model. Convert transfer-function model to zero-pole model. Plot title. Trace of a matrix.



**Table 1–1** (continued)

Commands and Matrix Functions Commonly Used in Solving Control Engineering Problems	Explanations of What Commands Do and Matrix Functions Mean
who whos	Lists all the variables currently in memory. List all the variables in the current workspace, together with information about their size, bytes, class, etc.
xlabel	x-axis label.
ylabel	y-axis label.
zero zeros zlabel zpk zp2tf	Transmission zeros of LTI systems. Zeros array. z-axis label Create zero–pole–gain models or convert to zero–pole–gain format. Convert zero–pole model to transfer- function model.

**Accessing and exiting MATLAB.** On most systems, once MATLAB has been installed, execute the command MATLAB to invoke MATLAB. To exit MATLAB, execute the command exit or quit.

MATLAB has an online help facility that may be invoked whenever the need arises. The command help will display a list of predefined functions and operators for which online help is available. The command

help 'function name'

will give information on the purpose and use of the specific function named. The command

help help

will give information on how to use the online help.

**Matrix operators.** The following notation is used in matrix operations (if multiple operations are involved, the order of the arithmetic operations can be altered with the use of parentheses):

+	Addition
–	Subtraction
*	Multiplication
^	Power
'	Conjugate transpose
/ or \	Matrix division
./ or .\	Array division