

海外优秀数学类教材系列丛书

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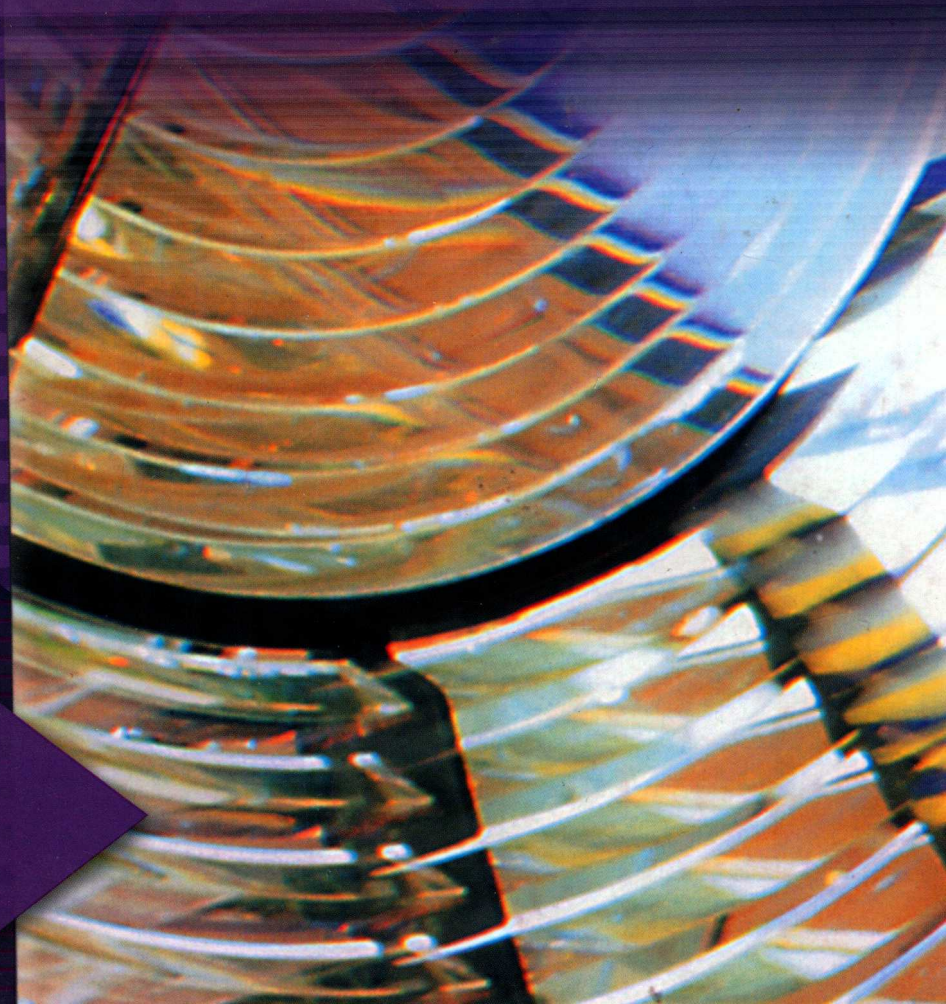
# Thomas' CALCULUS

(Eleventh Edition)

## 托马斯微积分 (第11版)

(下册)

- WEIR
- HASS
- GIORDANO



高等教育出版社

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## 托马斯微积分 (第11版)(下册)

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# CONTENTS

## Preface

ix

## 1

## Preliminaries

1

- 1.1 Real Numbers and the Real Line 1
- 1.2 Lines, Circles, and Parabolas 9
- 1.3 Functions and Their Graphs 19
- 1.4 Identifying Functions; Mathematical Models 28
- 1.5 Combining Functions; Shifting and Scaling Graphs 38
- 1.6 Trigonometric Functions 48
- 1.7 Graphing with Calculators and Computers 59
- QUESTIONS TO GUIDE YOUR REVIEW 68
- PRACTICE EXERCISES 69
- ADDITIONAL AND ADVANCED EXERCISES 71

## 2

## Limits and Continuity

73

- 2.1 Rates of Change and Limits 73
- 2.2 Calculating Limits Using the Limit Laws 84
- 2.3 The Precise Definition of a Limit 91
- 2.4 One-Sided Limits and Limits at Infinity 102
- 2.5 Infinite Limits and Vertical Asymptotes 115
- 2.6 Continuity 124
- 2.7 Tangents and Derivatives 134
- QUESTIONS TO GUIDE YOUR REVIEW 141
- PRACTICE EXERCISES 142
- ADDITIONAL AND ADVANCED EXERCISES 144

## 3

## Differentiation

147

- 3.1 The Derivative as a Function 147
- 3.2 Differentiation Rules 159

3.3	The Derivative as a Rate of Change	171
3.4	Derivatives of Trigonometric Functions	183
3.5	The Chain Rule and Parametric Equations	190
3.6	Implicit Differentiation	205
3.7	Related Rates	213
3.8	Linearization and Differentials	221
	QUESTIONS TO GUIDE YOUR REVIEW	235
	PRACTICE EXERCISES	235
	ADDITIONAL AND ADVANCED EXERCISES	240

**4****Applications of Derivatives****244**

4.1	Extreme Values of Functions	244
4.2	The Mean Value Theorem	255
4.3	Monotonic Functions and the First Derivative Test	262
4.4	Concavity and Curve Sketching	267
4.5	Applied Optimization Problems	278
4.6	Indeterminate Forms and L'Hôpital's Rule	292
4.7	Newton's Method	299
4.8	Antiderivatives	307
	QUESTIONS TO GUIDE YOUR REVIEW	318
	PRACTICE EXERCISES	318
	ADDITIONAL AND ADVANCED EXERCISES	322

**5****Integration****325**

5.1	Estimating with Finite Sums	325
5.2	Sigma Notation and Limits of Finite Sums	335
5.3	The Definite Integral	343
5.4	The Fundamental Theorem of Calculus	356
5.5	Indefinite Integrals and the Substitution Rule	368
5.6	Substitution and Area Between Curves	376
	QUESTIONS TO GUIDE YOUR REVIEW	387
	PRACTICE EXERCISES	388
	ADDITIONAL AND ADVANCED EXERCISES	391

**6****Applications of Definite Integrals****396**

6.1	Volumes by Slicing and Rotation About an Axis	396
6.2	Volumes by Cylindrical Shells	409
6.3	Lengths of Plane Curves	416
6.4	Moments and Centers of Mass	424
6.5	Areas of Surfaces of Revolution and the Theorems of Pappus	436
6.6	Work	447
6.7	Fluid Pressures and Forces	456

QUESTIONS TO GUIDE YOUR REVIEW	461
PRACTICE EXERCISES	461
ADDITIONAL AND ADVANCED EXERCISES	464

**7****Transcendental Functions****466**

7.1 Inverse Functions and Their Derivatives	466
7.2 Natural Logarithms	476
7.3 The Exponential Function	486
7.4 $a^x$ and $\log_a x$	495
7.5 Exponential Growth and Decay	502
7.6 Relative Rates of Growth	511
7.7 Inverse Trigonometric Functions	517
7.8 Hyperbolic Functions	535
QUESTIONS TO GUIDE YOUR REVIEW	546
PRACTICE EXERCISES	547
ADDITIONAL AND ADVANCED EXERCISES	550

**8****Techniques of Integration****553**

8.1 Basic Integration Formulas	553
8.2 Integration by Parts	561
8.3 Integration of Rational Functions by Partial Fractions	570
8.4 Trigonometric Integrals	581
8.5 Trigonometric Substitutions	586
8.6 Integral Tables and Computer Algebra Systems	593
8.7 Numerical Integration	603
8.8 Improper Integrals	619
QUESTIONS TO GUIDE YOUR REVIEW	633
PRACTICE EXERCISES	634
ADDITIONAL AND ADVANCED EXERCISES	638

**9****Further Applications of Integration****642**

9.1 Slope Fields and Separable Differential Equations	642
9.2 First-Order Linear Differential Equations	650
9.3 Euler's Method	659
9.4 Graphical Solutions of Autonomous Differential Equations	665
9.5 Applications of First-Order Differential Equations	673
QUESTIONS TO GUIDE YOUR REVIEW	682
PRACTICE EXERCISES	682
ADDITIONAL AND ADVANCED EXERCISES	683

**10****Conic Sections and Polar Coordinates****685**

- 10.1 Conic Sections and Quadratic Equations 685
- 10.2 Classifying Conic Sections by Eccentricity 697
- 10.3 Quadratic Equations and Rotations 702
- 10.4 Conics and Parametric Equations; The Cycloid 709
- 10.5 Polar Coordinates 714
- 10.6 Graphing in Polar Coordinates 719
- 10.7 Areas and Lengths in Polar Coordinates 725
- 10.8 Conic Sections in Polar Coordinates 732
- QUESTIONS TO GUIDE YOUR REVIEW 739
- PRACTICE EXERCISES 739
- ADDITIONAL AND ADVANCED EXERCISES 742

**11****Infinite Sequences and Series****746**

- 11.1 Sequences 747
- 11.2 Infinite Series 761
- 11.3 The Integral Test 772
- 11.4 Comparison Tests 777
- 11.5 The Ratio and Root Tests 781
- 11.6 Alternating Series, Absolute and Conditional Convergence 787
- 11.7 Power Series 794
- 11.8 Taylor and Maclaurin Series 805
- 11.9 Convergence of Taylor Series; Error Estimates 811
- 11.10 Applications of Power Series 822
- 11.11 Fourier Series 833
- QUESTIONS TO GUIDE YOUR REVIEW 839
- PRACTICE EXERCISES 840
- ADDITIONAL AND ADVANCED EXERCISES 843

**12****Vectors and the Geometry of Space****848**

- 12.1 Three-Dimensional Coordinate Systems 848
- 12.2 Vectors 853
- 12.3 The Dot Product 862
- 12.4 The Cross Product 873
- 12.5 Lines and Planes in Space 880
- 12.6 Cylinders and Quadric Surfaces 889
- QUESTIONS TO GUIDE YOUR REVIEW 899
- PRACTICE EXERCISES 900
- ADDITIONAL AND ADVANCED EXERCISES 902



**13****Vector-Valued Functions and Motion in Space****906**

- 13.1 Vector Functions 906
- 13.2 Modeling Projectile Motion 920
- 13.3 Arc Length and the Unit Tangent Vector  $\mathbf{T}$  931
- 13.4 Curvature and the Unit Normal Vector  $\mathbf{N}$  936
- 13.5 Torsion and the Unit Binormal Vector  $\mathbf{B}$  943
- 13.6 Planetary Motion and Satellites 950
- QUESTIONS TO GUIDE YOUR REVIEW 959
- PRACTICE EXERCISES 960
- ADDITIONAL AND ADVANCED EXERCISES 962

**14****Partial Derivatives****965**

- 14.1 Functions of Several Variables 965
- 14.2 Limits and Continuity in Higher Dimensions 976
- 14.3 Partial Derivatives 984
- 14.4 The Chain Rule 996
- 14.5 Directional Derivatives and Gradient Vectors 1005
- 14.6 Tangent Planes and Differentials 1015
- 14.7 Extreme Values and Saddle Points 1027
- 14.8 Lagrange Multipliers 1038
- 14.9 Partial Derivatives with Constrained Variables 1049
- 14.10 Taylor's Formula for Two Variables 1054
- QUESTIONS TO GUIDE YOUR REVIEW 1059
- PRACTICE EXERCISES 1060
- ADDITIONAL AND ADVANCED EXERCISES 1063

**15****Multiple Integrals****1067**

- 15.1 Double Integrals 1067
- 15.2 Areas, Moments, and Centers of Mass 1081
- 15.3 Double Integrals in Polar Form 1092
- 15.4 Triple Integrals in Rectangular Coordinates 1098
- 15.5 Masses and Moments in Three Dimensions 1109
- 15.6 Triple Integrals in Cylindrical and Spherical Coordinates 1114
- 15.7 Substitutions in Multiple Integrals 1128
- QUESTIONS TO GUIDE YOUR REVIEW 1137
- PRACTICE EXERCISES 1138
- ADDITIONAL AND ADVANCED EXERCISES 1140

**16****Integration in Vector Fields****1143**

- 16.1 Line Integrals 1143
- 16.2 Vector Fields, Work, Circulation, and Flux 1149
- 16.3 Path Independence, Potential Functions, and Conservative Fields 1160
- 16.4 Green's Theorem in the Plane 1169
- 16.5 Surface Area and Surface Integrals 1182
- 16.6 Parametrized Surfaces 1192
- 16.7 Stokes' Theorem 1201
- 16.8 The Divergence Theorem and a Unified Theory 1211
- QUESTIONS TO GUIDE YOUR REVIEW 1222
- PRACTICE EXERCISES 1223
- ADDITIONAL AND ADVANCED EXERCISES 1226

**Appendices****AP-1**

- A.1 Mathematical Induction AP-1
- A.2 Proofs of Limit Theorems AP-4
- A.3 Commonly Occurring Limits AP-7
- A.4 Theory of the Real Numbers AP-9
- A.5 Complex Numbers AP-12
- A.6 The Distributive Law for Vector Cross Products AP-22
- A.7 The Mixed Derivative Theorem and the Increment Theorem AP-23
- A.8 The Area of a Parallelogram's Projection on a Plane AP-28
- A.9 Basic Algebra, Geometry, and Trigonometry Formulas AP-29

**Answers****A-1****Index****I-1****A Brief Table of Integrals****T-1****Credits****C-1**















