



影印版

Calculus (Seventh Edition)

微积分 (第7版)

(下册)

□ James Stewart

高等教育出版社



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Calculus

(Seventh Edition)

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James Stewart

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Calculus; Early Transcendentals, International Metric Edition, 7th Edition James Stewart

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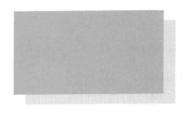
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Contents

Preface xi

To the Student xxiii

Diagnostic Tests xxiv

A PREVIEW OF CALCULUS

1

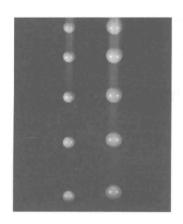
Functions and Models 9



- 1.1 Four Ways to Represent a Function 10
- 1.2 Mathematical Models: A Catalog of Essential Functions 23
- 1.3 New Functions from Old Functions 36
- 1.4 Graphing Calculators and Computers 44
- 1.5 Exponential Functions 51
- 1.6 Inverse Functions and Logarithms 58 Review 72

Principles of Problem Solving 75

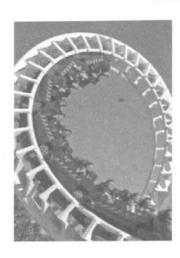
2 Limits and Derivatives 81



- 2.1 The Tangent and Velocity Problems 82
- 2.2 The Limit of a Function 87
- 2.3 Calculating Limits Using the Limit Laws 99
- 2.4 The Precise Definition of a Limit 108
- 2.5 Continuity 118
- 2.6 Limits at Infinity; Horizontal Asymptotes 130
- 2.7 Derivatives and Rates of Change 143
 Writing Project = Early Methods for Finding Tangents 15
- 2.8 The Derivative as a Function 154
 Review 165

Problems Plus 170

Differentiation Rules



3.1	Derivatives of Polynomials and Exponential Functions		
	Applied Project = Building a Better Roller Coaster 184		
3.2	The Product and Quotient Rules 184		
22	Derivatives of Trigonometric Functions 191		

173

3.4 The Chain Rule 198 Applied Project - Where Should a Pilot Start Descent?

Implicit Differentiation 3.5 Laboratory Project = Families of Implicit Curves 217

3.6 Derivatives of Logarithmic Functions

3.7 Rates of Change in the Natural and Social Sciences

3.8 Exponential Growth and Decay

3.9 Related Rates 244

Linear Approximations and Differentials 250 3.10 Laboratory Project - Taylor Polynomials 256

3.11 Hyperbolic Functions Review 264

Problems Plus 268

Applications of Differentiation 273



- Maximum and Minimum Values 4.1 Applied Project = The Calculus of Rainbows
- 4.2 The Mean Value Theorem
- How Derivatives Affect the Shape of a Graph 4.3 290
- 4.4 Indeterminate Forms and l'Hospital's Rule 301 Writing Project - The Origins of l'Hospital's Rule 310
- 4.5 Summary of Curve Sketching
- 4.6 Graphing with Calculus and Calculators
- Optimization Problems 4.7 Applied Project = The Shape of a Can
- 4.8 Newton's Method 338
- Antiderivatives 344 4.9 Review 351

Integrals 359



- 5.1 Areas and Distances 360
 - 5.2 The Definite Integral 371
 - Discovery Project = Area Functions 385
- 5.3 The Fundamental Theorem of Calculus 386
- 5.4 Indefinite Integrals and the Net Change Theorem 397
 Writing Project * Newton, Leibniz, and the Invention of Calculus
- 5.5 The Substitution Rule 407 Review 415

Problems Plus 419

6 Applications of Integration 421



- 6.1 Areas Between Curves 422

 Applied Project The Gini Index 42
- **6.2** Volumes 430
- 6.3 Volumes by Cylindrical Shells 441
- 6.4 Work 446
- 6.5 Average Value of a Function 451

Applied Project = Calculus and Baseball 455

Applied Project . Where to Sit at the Movies 456

Review 457

Problems Plus 459

7 Techniques of Integration 463



- 7.1 Integration by Parts 464
- 7.2 Trigonometric Integrals 471
- 7.3 Trigonometric Substitution 478
- 7.4 Integration of Rational Functions by Partial Fractions 48
- 7.5 Strategy for Integration 494
- 7.6 Integration Using Tables and Computer Algebra Systems 500
 Discovery Project Patterns in Integrals 505

506 7.7 Approximate Integration

7.8 Improper Integrals

> Review 529

Problems Plus 533

Further Applications of Integration 537



8.1 Arc Length Discovery Project - Arc Length Contest

8.2 Area of a Surface of Revolution Discovery Project - Rotating on a Slant

8.3 Applications to Physics and Engineering 552 Discovery Project - Complementary Coffee Cups

Applications to Economics and Biology 8.4 563

8.5 Probability 568 575 Review

Problems Plus

Differential Equations 579



- 9.1 Modeling with Differential Equations 580
- 9.2 Direction Fields and Euler's Method 585
- 9.3 Separable Equations Applied Project - How Fast Does a Tank Drain? Applied Project . Which Is Faster, Going Up or Coming Down?
- 9.4 Models for Population Growth 605
- 9.5 Linear Equations 616
- 9.6 Predator-Prey Systems 622 Review 629

Problems Plus

635



10.1	Curves Defined by Parametric Equations	636	
	Laboratory Project * Running Circles around Cir	cles 644	

- 10.2 Calculus with Parametric Curves Laboratory Project = Bézier Curves
- 10.3 Polar Coordinates 654 Laboratory Project * Families of Polar Curves
- Areas and Lengths in Polar Coordinates 10.4
- Conic Sections 10.5
- Conic Sections in Polar Coordinates 10.6 Review 685

Problems Plus 688

Infinite Sequences and Series 689



- 11.1 Sequences 690 Laboratory Project = Logistic Sequences
- 11.2 Series 703
- 11.3 The Integral Test and Estimates of Sums
- 11.4 The Comparison Tests 722
- 11.5 Alternating Series 727
- 11.6 Absolute Convergence and the Ratio and Root Tests 732
- 11.7 Strategy for Testing Series
- 11.8 Power Series 741
- 11.9 Representations of Functions as Power Series 746
- 11.10 Taylor and Maclaurin Series Laboratory Project - An Elusive Limit 767 Writing Project - How Newton Discovered the Binomial Series
- Applications of Taylor Polynomials Applied Project - Radiation from the Stars 777 Review 778

Problems Plus 781

785 **Vectors and the Geometry of Space**



- Three-Dimensional Coordinate Systems 786 12.1
- 12.2 Vectors 791
- The Dot Product 800 12.3
- 808 12.4 The Cross Product Discovery Project = The Geometry of a Tetrahedron 816
- 12.5 Equations of Lines and Planes Laboratory Project = Putting 3D in Perspective
- 12.6 Cylinders and Quadric Surfaces Review 834

Problems Plus

Vector Functions 839



- Vector Functions and Space Curves 13.1
- Derivatives and Integrals of Vector Functions 13.2 847
- 13.3 Arc Length and Curvature 853
- 13.4 Motion in Space: Velocity and Acceleration 862 Applied Project . Kepler's Laws 872 Review 873

Problems Plus 876

Partial Derivatives 877



- 14.1 Functions of Several Variables 878
- Limits and Continuity 14.2
- 14.3 Partial Derivatives 900
- Tangent Planes and Linear Approximations 14.4 915
- 14.5 The Chain Rule 924
- Directional Derivatives and the Gradient Vector 14.6 933
- Maximum and Minimum Values 14.7 946

Applied Project - Designing a Dumpster 956

Discovery Project = Quadratic Approximations and Critical Points

14.8 Lagrange Multipliers 957

Applied Project - Rocket Science 964

Applied Project = Hydro-Turbine Optimization 96

Review 967

Problems Plus 971

15 Multiple Integrals 973



- 15.1 Double Integrals over Rectangles 974
- 15.2 Iterated Integrals 983
- 15.3 Double Integrals over General Regions 988
- 15.4 Double Integrals in Polar Coordinates 997
- 15.5 Applications of Double Integrals 1003
- 15.6 Surface Area 1013
- **15.7** Triple Integrals 1017
- Discovery Project = Volumes of Hyperspheres 1027
- 15.8 Triple Integrals in Cylindrical Coordinates 1027
 Laboratory Project The Intersection of Three Cylinders 1032
- 15.9 Triple Integrals in Spherical Coordinates 1033Applied Project * Roller Derby 1039
- 15.10 Change of Variables in Multiple Integrals 1040 Review 1049

Problems Plus 1053

16 Vector Calculus 1055



- **16.1** Vector Fields 1056
 - 16.2 Line Integrals 1063
 - **16.3** The Fundamental Theorem for Line Integrals 1075
 - 16.4 Green's Theorem 1084
 - 16.5 Curl and Divergence 1091
 - 16.6 Parametric Surfaces and Their Areas 1099
 - 16.7 Surface Integrals 1110
 - 16.8 Stokes' Theorem 1122

Writing Project * Three Men and Two Theorems 1128

1128 The Divergence Theorem 16.9

16.10 Summary 1135

> Review 1136

Problems Plus 1139

Second-Order Differential Equations 1141



- 17.1 Second-Order Linear Equations
- 17.2 Nonhomogeneous Linear Equations
- Applications of Second-Order Differential Equations 17.3 1156
- Series Solutions 17.4 1164

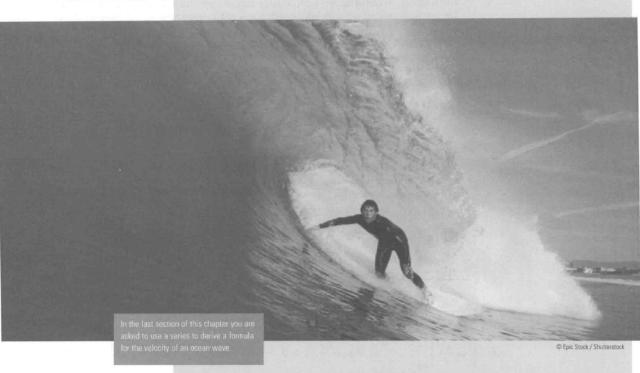
Review 1169

Appendixes A1

- A Numbers, Inequalities, and Absolute Values A2
- В Coordinate Geometry and Lines
- C Graphs of Second-Degree Equations A16
- D Trigonometry A24
- E Sigma Notation A34
- F Proofs of Theorems A39
- G The Logarithm Defined as an Integral A50
- Н Complex Numbers A57
- Answers to Odd-Numbered Exercises A65

Index A135

Infinite Sequences and Series



paradoxes and the decimal representation of numbers. Their importance in calculus stems from Newton's

idea of representing functions as sums of infinite series. For instance, in finding areas he often integrated a function by first expressing it as a series and then integrating each term of the series. We will pursue his idea in Section 11.10 in order to integrate such functions as e^{-x^2} . (Recall that we have previously been unable to do this.) Many of the functions that arise in mathematical physics and chemistry, such as Bessel functions, are defined as sums of series, so it is important to be familiar with the basic concepts of con-

Infinite sequences and series were introduced briefly in A Preview of Calculus in connection with Zeno's

vergence of infinite sequences and series.

Physicists also use series in another way, as we will see in Section 11.11. In studying fields as diverse as optics, special relativity, and electromagnetism, they analyze phenomena by replacing a function with the first few terms in the series that represents it.

11.1 Sequences

A sequence can be thought of as a list of numbers written in a definite order:

$$a_1, a_2, a_3, a_4, \ldots, a_n, \ldots$$

The number a_1 is called the *first term*, a_2 is the *second term*, and in general a_n is the *nth term*. We will deal exclusively with infinite sequences and so each term a_n will have a successor a_{n+1} .

Notice that for every positive integer n there is a corresponding number a_n and so a sequence can be defined as a function whose domain is the set of positive integers. But we usually write a_n instead of the function notation f(n) for the value of the function at the number n.

NOTATION The sequence $\{a_1, a_2, a_3, \ldots\}$ is also denoted by

$$\{a_n\}$$
 or $\{a_n\}_{n=1}^{\infty}$

EXAMPLE 1 Some sequences can be defined by giving a formula for the *n*th term. In the following examples we give three descriptions of the sequence: one by using the preceding notation, another by using the defining formula, and a third by writing out the terms of the sequence. Notice that *n* doesn't have to start at 1.

(a)
$$\left\{\frac{n}{n+1}\right\}_{n=1}^{\infty}$$
 $a_n = \frac{n}{n+1}$ $\left\{\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \dots, \frac{n}{n+1}, \dots\right\}$

(b)
$$\left\{\frac{(-1)^n(n+1)}{3^n}\right\}$$
 $a_n = \frac{(-1)^n(n+1)}{3^n}$ $\left\{-\frac{2}{3}, \frac{3}{9}, -\frac{4}{27}, \frac{5}{81}, \dots, \frac{(-1)^n(n+1)}{3^n}, \dots\right\}$

(c)
$$\{\sqrt{n-3}\}_{n=3}^{\infty}$$
 $a_n = \sqrt{n-3}, n \ge 3 \quad \{0, 1, \sqrt{2}, \sqrt{3}, \dots, \sqrt{n-3}, \dots\}$

(d)
$$\left\{\cos\frac{n\pi}{6}\right\}_{n=0}^{\infty}$$
 $a_n = \cos\frac{n\pi}{6}, \ n \ge 0 \quad \left\{1, \frac{\sqrt{3}}{2}, \frac{1}{2}, 0, \dots, \cos\frac{n\pi}{6}, \dots\right\}$

V EXAMPLE 2 Find a formula for the general term a_n of the sequence

$$\left\{\frac{3}{5}, -\frac{4}{25}, \frac{5}{125}, -\frac{6}{625}, \frac{7}{3125}, \ldots\right\}$$

assuming that the pattern of the first few terms continues.

SOLUTION We are given that

$$a_1 = \frac{3}{5}$$
 $a_2 = -\frac{4}{25}$ $a_3 = \frac{5}{125}$ $a_4 = -\frac{6}{625}$ $a_5 = \frac{7}{3125}$

Notice that the numerators of these fractions start with 3 and increase by 1 whenever we go to the next term. The second term has numerator 4, the third term has numerator 5; in general, the nth term will have numerator n + 2. The denominators are the powers of 5,

691

$$a_n = (-1)^{n-1} \frac{n+2}{5^n}$$

EXAMPLE 3 Here are some sequences that don't have a simple defining equation.

- (a) The sequence $\{p_n\}$, where p_n is the population of the world as of January 1 in the year n.
- (b) If we let a_n be the digit in the *n*th decimal place of the number e, then $\{a_n\}$ is a well-defined sequence whose first few terms are

$$\{7, 1, 8, 2, 8, 1, 8, 2, 8, 4, 5, \ldots\}$$

(c) The **Fibonacci sequence** $\{f_n\}$ is defined recursively by the conditions

$$f_1 = 1$$
 $f_2 = 1$ $f_n = f_{n-1} + f_{n-2}$ $n \ge 3$

Each term is the sum of the two preceding terms. The first few terms are

$$\{1, 1, 2, 3, 5, 8, 13, 21, \ldots\}$$

This sequence arose when the 13th-century Italian mathematician known as Fibonacci solved a problem concerning the breeding of rabbits (see Exercise 83).

A sequence such as the one in Example 1(a), $a_n = n/(n+1)$, can be pictured either by plotting its terms on a number line, as in Figure 1, or by plotting its graph, as in Figure 2. Note that, since a sequence is a function whose domain is the set of positive integers, its graph consists of isolated points with coordinates

$$(1, a_1)$$
 $(2, a_2)$ $(3, a_3)$... (n, a_n) ...

From Figure 1 or Figure 2 it appears that the terms of the sequence $a_n = n/(n+1)$ are approaching 1 as n becomes large. In fact, the difference

$$1 - \frac{n}{n+1} = \frac{1}{n+1}$$

can be made as small as we like by taking n sufficiently large. We indicate this by writing

$$\lim_{n\to\infty}\frac{n}{n+1}=1$$

In general, the notation

$$\lim_{n\to\infty} a_n = L$$

means that the terms of the sequence $\{a_n\}$ approach L as n becomes large. Notice that the following definition of the limit of a sequence is very similar to the definition of a limit of a function at infinity given in Section 2.6.

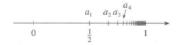


FIGURE 1

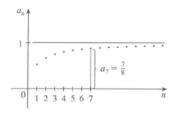


FIGURE 2

1 Definition A sequence $\{a_n\}$ has the limit L and we write

$$\lim_{n \to \infty} a_n = L \quad \text{or} \quad a_n \to L \text{ as } n \to \infty$$

if we can make the terms a_n as close to L as we like by taking n sufficiently large. If $\lim_{n\to\infty} a_n$ exists, we say the sequence **converges** (or is **convergent**). Otherwise, we say the sequence **diverges** (or is **divergent**).

Figure 3 illustrates Definition 1 by showing the graphs of two sequences that have the limit L.



A more precise version of Definition 1 is as follows.

2 Definition A sequence $\{a_n\}$ has the **limit** L and we write

$$\lim_{n \to \infty} a_n = L \quad \text{or} \quad a_n \to L \text{ as } n \to \infty$$

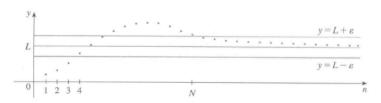
if for every $\varepsilon > 0$ there is a corresponding integer N such that

if
$$n > N$$
 then $|a_n - L| < \varepsilon$

Definition 2 is illustrated by Figure 4, in which the terms a_1, a_2, a_3, \ldots are plotted on a number line. No matter how small an interval $(L - \varepsilon, L + \varepsilon)$ is chosen, there exists an N such that all terms of the sequence from a_{N+1} onward must lie in that interval.



Another illustration of Definition 2 is given in Figure 5. The points on the graph of $\{a_n\}$ must lie between the horizontal lines $y = L + \varepsilon$ and $y = L - \varepsilon$ if n > N. This picture must be valid no matter how small ε is chosen, but usually a smaller ε requires a larger N.



Compare this definition with Definition 2.6.7.

FIGURE 5

If you compare Definition 2 with Definition 2.6.7 you will see that the only difference between $\lim_{n\to\infty} a_n = L$ and $\lim_{x\to\infty} f(x) = L$ is that n is required to be an integer. Thus we have the following theorem, which is illustrated by Figure 6.

3 Theorem If $\lim_{x\to\infty} f(x) = L$ and $f(n) = a_n$ when n is an integer, then $\lim_{n\to\infty} a_n = L$.

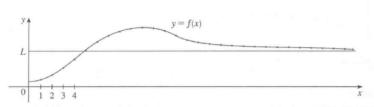


FIGURE 6

In particular, since we know that $\lim_{x\to\infty} (1/x^r) = 0$ when r > 0 (Theorem 2.6.5), we have

$$\lim_{n \to \infty} \frac{1}{n^r} = 0 \quad \text{if } r > 0$$

If a_n becomes large as n becomes large, we use the notation $\lim_{n\to\infty} a_n = \infty$. The following precise definition is similar to Definition 2.6.9.

5 Definition $\lim_{n\to\infty} a_n = \infty$ means that for every positive number M there is an integer N such that

if
$$n > N$$
 then $a_n > M$

If $\lim_{n\to\infty} a_n = \infty$, then the sequence $\{a_n\}$ is divergent but in a special way. We say that $\{a_n\}$ diverges to ∞ .

The Limit Laws given in Section 2.3 also hold for the limits of sequences and their proofs are similar.

Limit Laws for Sequences

If
$$\{a_n\}$$
 and $\{b_n\}$ are convergent sequences and c is a constant, then
$$\lim_{n\to\infty} (a_n + b_n) = \lim_{n\to\infty} a_n + \lim_{n\to\infty} b_n$$

$$\lim_{n\to\infty} (a_n - b_n) = \lim_{n\to\infty} a_n - \lim_{n\to\infty} b_n$$

$$\lim_{n\to\infty} ca_n = c \lim_{n\to\infty} a_n \qquad \lim_{n\to\infty} c = c$$

$$\lim_{n\to\infty} (a_nb_n) = \lim_{n\to\infty} a_n \cdot \lim_{n\to\infty} b_n$$

$$\lim_{n\to\infty} \frac{a_n}{b_n} = \frac{\lim_{n\to\infty} a_n}{\lim_{n\to\infty} b_n} \quad \text{if } \lim_{n\to\infty} b_n \neq 0$$

$$\lim_{n\to\infty} a_n^p = \left[\lim_{n\to\infty} a_n\right]^p \quad \text{if } p > 0 \text{ and } a_n > 0$$

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