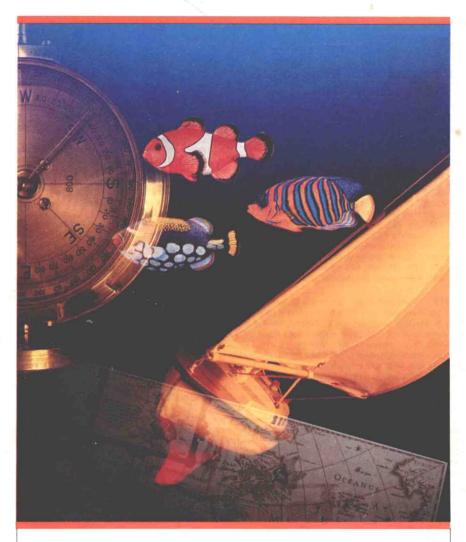


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# MATHEMATICS IN ACTION



Alan R. Hoffer

Steven J. Leinwand

Gary L. Musser

Martin L. Johnson

Richard D. Lodholz

Tina Thoburn

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### CONSULTANTS

Zelda Gold, Mathematics Advisor, Los Angeles Unified School District, Panorama City, California • Audrey Friar Jackson, Math Specialist K-6, Parkway School District, Chesterfield, Missouri • Susan Lair, Department Chairperson, Wedgwood Middle School, Fort Worth Independent School District, Texas • Gail Lowe, Principal, Conejo Valley United School District, Thousand Oaks, California

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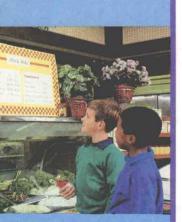
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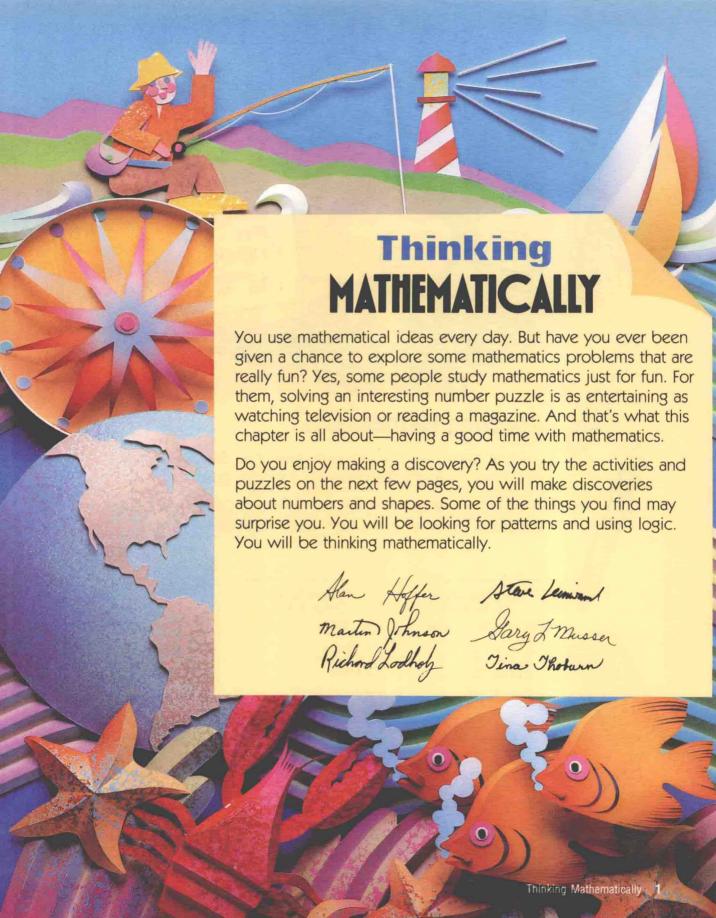
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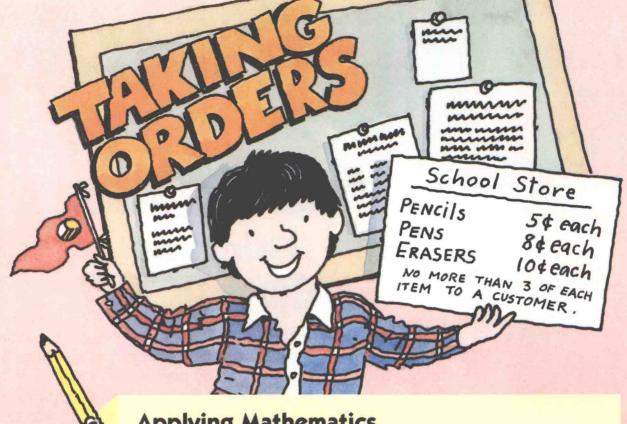
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# **Applying Mathematics**

You use mathematics to solve problems all the time. Think about buying and selling items in a school store.

Suppose you are running the school store. Copy and complete the following order forms from other students.

1.

School Store Order Form Item Cost 2 Pencils 3 Erasers Total Cost

2.

School Store Order Form # Item Cost 1 Pencil 3 Pens 2 Erasers Total Cost

3.

School Store Order Form		
#	Item	Cost
3 F	Pens	
3 F	Pencils	
To	tal Cost	

- 4. Make up your own order and find its cost.
- 5. A friend of yours spent exactly 30¢ in the store. What possible purchases could your friend have made?
- 6. Can you spend exactly 50¢? Why or why not?



Suppose you are the clerk in the school store. Solve the following problems.

- 7. Mike pays for 1 pencil, 3 pens, and 1 eraser with 2 quarters. How much does Mike spend? How much change does Mike get? What coins would you give him to make the change?
- 8. Alissa buys one of each item with a dollar. How much does she spend? How much change does she get? What coins would you give her to make the change?
- 9. Lonnie needs 3 pencils and 2 pens. He has a quarter. What problem does Lonnie face? What can Lonnie do to solve his problem?

Now suppose you are a customer in the store.

- 10. What is the greatest amount you could spend at one time in the school store? (Hint: Remember the sign.)
- 11. List all the different orders you can make of 3 or more items that have a total cost of 25¢ or less.
- 12. Suppose you had exactly 26¢. Could you spend the 26¢ exactly in the school store? How? Is there more than one way to spend exactly 26¢ in the store? What other ways could you spend exactly 26¢?





PLAYING WITH .... NUMBERS



First, make a set of 9 playing cards, one card for each of the numbers 1 to 9. Use blank cards or cut sheets of paper into 9 equal-sized pieces.

1

2

3

4

5

6

7

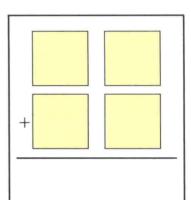
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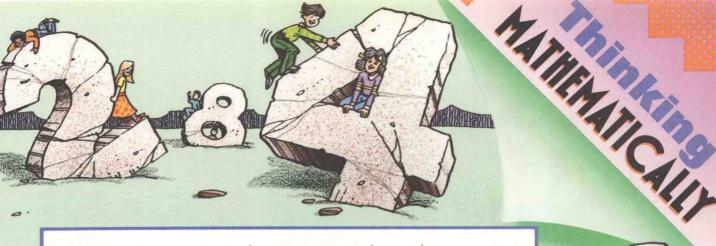
Next, on another sheet of paper, draw a board like the one at the right. The spaces should be about the same size as your cards.

Play the games.

1. Pick any 4 of your cards. Place them on your board so that you get the greatest sum. How did you arrange the numbers you picked?



- 2. Now pick the 4 cards that would give you the greatest sum. How would you arrange these cards? What is the greatest possible sum?
- 3. Pick the 4 cards that would give you the least possible sum. How would you arrange these cards? What is the least possible sum?
- 4. Can you use 4 cards to get a sum of exactly 75 in this game? How many different ways can you get 75 using 4 cards?



5. Try making up some of your own questions using the addition arrangement. Try out your questions with a partner.

Now make a subtraction board like the one to the right.

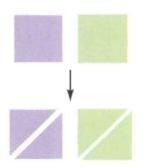
- 6. Pick any 3 cards. Arrange them on the board to get the greatest possible difference.
- 7. Use these same 3 cards to get the least possible difference.
- 8. Which 3 cards would you pick to get a difference closest to 10? What is the difference? Is there another way?
- 9. Discuss your reasoning on Problems 6, 7, and 8 with a partner.
- 10. Now pick the 3 cards that will give you the greatest possible difference. What is this difference? How do you know that it is the greatest possible difference?
- 11. Pick the 3 cards that will give you the least possible difference. What is this difference? How do you know that it is the least possible difference?
- 12. Make up your own questions using the subtraction arrangement. Try them out with a partner.





# **Visual Reasoning**

Cut out two identical squares from two sheets of different-colored paper. Then fold each square in half to make a triangle and cut along the fold. You should have four triangles—two of each color.



Now experiment with your triangles. Put them together to make a rectangle. Then move the triangles around to make another rectangle with a different design. Each time you create a new design, draw a picture of it. For example:



Be careful. and are not different designs.

You can make the design on the second rectangle simply by turning the first rectangle.

- 1. Work with a partner. Compare your designs. Did you both find the same designs? Can you find other designs working together?
- 2. How many different rectangular designs can you make?
- 3. What other shapes and designs can each of you make using your four triangles? Do you have to decide on some rules for how to arrange the triangles?
- 4. Work with your partner and use all eight of your triangles to create shapes and designs. See what you can discover. Do you think you will make more shapes and designs than you did with four triangles? Why?