WILEY FINANCE

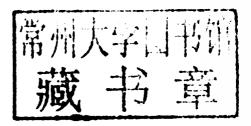
RISK FINANCE AND ASSET VALUE, MEASUREMENT PRICING AND MARKETS

Charles S. Tapiero

Risk Finance and Asset Pricing

Value, Measurements, and Markets

CHARLES S. TAPIERO





Copyright © 2010 by Charles S. Tapiero. All rights reserved.

Published by John Wiley & Sons, Inc., Hoboken, New Jersey. Published simultaneously in Canada.

No part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanical, photocopying, recording, scanning, or otherwise, except as permitted under Section 107 or 108 of the 1976 United States Copyright Act, without either the prior written permission of the Publisher, or authorization through payment of the appropriate per-copy fee to the Copyright Clearance Center, Inc., 222 Rosewood Drive, Danvers, MA 01923, (978) 750-8400, fax (978) 646-8600, or on the Web at www.copyright.com. Requests to the Publisher for permission should be addressed to the Permissions Department, John Wiley & Sons, Inc., 111 River Street, Hoboken, NJ 07030, (201) 748-6011, fax (201) 748-6008, or online at http://www.wiley.com/go/permissions.

Limit of Liability/Disclaimer of Warranty: While the publisher and author have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. No warranty may be created or extended by sales representatives or written sales materials. The advice and strategies contained herein may not be suitable for your situation. You should consult with a professional where appropriate. Neither the publisher nor author shall be liable for any loss of profit or any other commercial damages, including but not limited to special, incidental, consequential, or other damages.

For general information on our other products and services or for technical support, please contact our Customer Care Department within the United States at (800) 762-2974, outside the United States at (317) 572-3993 or fax (317) 572-4002.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books. For more information about Wiley products, visit our web site at www.wiley.com.

Library of Congress Cataloging-in-Publication Data:

Tapiero, Charles S.

Risk finance and asset pricing: value, measurements, and markets / Charles S. Tapiero.

p. cm. — (Wiley finance; 563)

Includes index.

ISBN 978-0-470-54946-9 (cloth); 978-0-470-89237-4 (ebk); 978-0-470-89238-1 (ebk)

1. Financial engineering. 2. Financial risk management. 3. Finance—Mathematical models. 4. Investments—Mathematical models. I. Title.

HG176.7.T37 2010 658.15′5—dc22

2010015106

Printed in the United States of America

10 9 8 7 6 5 4 3 2 1

Risk Finance and Asset Pricing

Founded in 1807, John Wiley & Sons is the oldest independent publishing company in the United States. With offices in North America, Europe, Australia and Asia, Wiley is globally committed to developing and marketing print and electronic products and services for our customers' professional and personal knowledge and understanding.

The Wiley Finance series contains books written specifically for finance and investment professionals as well as sophisticated individual investors and their financial advisors. Book topics range from portfolio management to e-commerce, risk management, financial engineering, valuation and financial instrument analysis, as well as much more.

For a list of available titles, please visit our Web site at www.WileyFinance.com.

To Carole, Oscar, Bettina, Scarlett, Laura-Julia, Talya, and not least, Arielle

Introduction

At both theoretical and practical levels, finance theory has made extraordinary intellectual strides while contributing immensely to economic development. At the same time it has enriched the many financial engineers able to innovate and trade in financial products that create greater liquidity, predict and price assets, manage financial risks, and contribute to the growth of financial markets.

Today, risk finance and engineering is confronted with immense challenges and opportunities. They include:

- Bridging theory and practice following the important contributions made these past decades by Kenneth Arrow and Gerard Debreu's fundamental theory of asset pricing and its many uses to better comprehend the working of financial markets and price assets and their derivatives.
- Reconciling the doubts raised by assumptions of fundamental finance and opportunities to profit by the initiated who can appreciate the pro and cons of these theories.

The motivation for this book arose in the course of my lectures in the Department of Finance and Risk Engineering at the New York University (NYU) Polytechnic Institute following the financial meltdown of 2008–2009. This was a year when risks and all their financial manifestations struck at the heart of financial citadels and world economies. No firm was too big to fail, and risks hitherto conceived of theoretically, ignored, or only dreamed of have revealed their potency. This was also a year when extreme events have come into their own: ex ante ignored, but factual and painful ex post for all those who ignored the unlikely. The whole world was hurting: Unemployment, deflation of assets, and times of reckoning with greed, regulation, constraints, and finiteness of resources have become the underlying tune of financial discourse. Both persons and institutions have questioned the validity of financial models and their practical implications. On the academic front, challenging questions have been raised against the fundamental and complete markets dogma of finance, claiming that models can default and that incomplete markets are far more prevalent than theoretical finance would have us believe.

The financial meltdown of 2008–2009 has also ignited a far greater concern for the underlying purposes of finance, not only as a means to get rich but to confront the risks that beset us—whether predictable or not. These include population growth, environmental challenges, globalization of finance, infrastructure, wellness, and so on. These are real problems of common and personal importance. Financial transparency is called for to be part of the answer. The intent of this book is to provide an accessible formulation of theoretical financial constructs embedded in a broad variety of real and useful problems.

XVI INTRODUCTION

The crisis of 2008–2009 has revealed that risks borne by those uninitiated in the complexity of financial products and markets can be very costly. It has also become apparent that corporations and financial firms, traditionally managing real resources, have gradually shifted their economic activity by turning to financial manipulations, acting as intermediaries, with losses assumed by uninformed investors. These firms have capitalized on leverage and short-term returns while strapping healthy corporations with a debt they may not be able to bear. Governmental institutions have not been spared either. They, too, have turned to financial markets to seek the funds needed for investments in infrastructure or to meet their financing needs. Pandora's financial box has been opened, and finance—for all the good and the risks it deals with and manages—has at the same time the potential to cause great damage if not understood.

Further, there is an increased awareness that financial systems are changing. For example, the traditional role of banks to provide liquidity to borrowers and business firms may have been jeopardized in their pursuit of (short-term) profits. These financial institutions have become marketers of financial products and intermediaries to ever-growing financial markets, rather than filling the role of providers of liquidity which underlies their charter granted by society and its governments. In the pursuit of profits, new financial institutions and previously nonfinancial firms have emerged and converged in new enterprises that both offer financial services and manage their own economic interests. These firms, such as insurance companies, provide liquidity and are transforming the financial system. In these processes, financial engineers remain the means to provide financial products and help decide how and where to invest and how to manage risks. The insurance-finance convergence has also afforded a means to assure buyers and sellers and thus contribute to the liquidity needed. The creation of a global insurance exchange in New York to cover complex risks, modeled after Lloyd's of London, is just such an example. Finally, the recent financial crisis has revealed that liquidity matters very much and the future may be unpredictable. Non-transparency, complexity and ambiguity have combined with greed to induce "Management's Risks" as being able to derail financial sustainability and produce financial models that are not efficient. These revelations have increased our awareness that financial expectations can and do falter. This renewed awareness may alter the financial regulatory environment, financial markets, financial attitudes and by extension the future challenges of financial risk engineering. In such an environment, we may be confronted with new problems and new opportunities to provide the solutions needed by financial, corporate firms and individuals.

WHO THIS BOOK IS FOR

This book is intended for both beginning and practicing financial engineers and seeks to engender an appreciation for and understanding of pricing of real financial problems. Throughout my classes I have become aware that many concepts transparent to mathematically savvy students are not understood by others. Inversely, many students with an extensive mathematics background fail to understand that financial engineering is not about mathematics but about complex relationships between buyers and sellers acting in financial markets, imputing values and prices to just about everything that can be traded. To better appreciate what financial engineering

is, can do, and its limitations, it is necessary to have a strong footing in principles of economics and finance, data and statistical analysis, personal utility, and their behavioral manifestations in financial markets and financial modeling. In particular, financial modeling provides a means to interpret implied values and prices such as options, credit derivatives, and so on.

In this sense, financial engineering is both real and virtual. Its usefulness is fueled by the needs of financial parties and by its potential contributions to investors, speculators, and society at large. The perspectives of this book, unlike many important books in financial engineering and mathematics, are thus: to bridge theory and practice; to study financial engineering as a means and not only as an end to make money; and to emphasize a real finance that can provide the support needed to meet both individual and collective needs. At the same time, the book emphasizes an intuitive and comprehensive approach to the foundations of risk finance and its many applications to asset pricing, real financial problems, and financial risk management. In such a frame of mind, the book's theoretical frameworks for expected utility, the Arrow-Debreu foundations of fundamental finance, and basic statistical manipulations of data and financial modeling, are shown to be useful, relevant, and complementary.

HOW THIS BOOK IS STRUCTURED

Theoretical concepts and theories applied mindlessly can have dire consequences. Thus, understanding the underlying rationales that financial engineers use in financial modeling, optimization, and decision making is important. By the same token, financial engineers cannot be the canary in the coal mine and ought to recognize that there is an inherent social and ethical responsibility that need not contradict the pursuit of wealth and money. There are as many opportunities to profit by contributing to economic sustainability—via investment in needed infrastructures, preventing booms and busts, reducing social inequities, pointing to market potential defaults and failures, and so on—as there are opportunities to profit from the design of complex and marketable financial products that provide greater and needed financial liquidity, and from seeking arbitrage opportunities and better forecasting financial market prices.

The many applications treated in this book, drawn from a variety of financial, engineering, and business professions, include insurance, pricing corporate loans and managing their risks, pricing safety and reliability, pricing franchises, operations risks, environmental quality and its control, infrastructure pricing, pricing water, pricing the insurance of rare events and uncommon risks, and more. These applications are used to establish a motivation and a background for a greater appreciation of finance and its risk engineering. Throughout the book, simplifications are made to focus greater attention on the problem-solving rationality financial engineers use. The required quantitative level needed for the book is kept at a consistent and introductory level. Some sections, however, require a slightly more advanced mathematical background; these are marked with an asterisk (*) in the table of contents and offer an added motivation to ambitious students. Additional extensions to each of the book chapters and problems solved are relegated to a web site companion, www.charlestapiero.com. This web site introduces as well in far greater detail

XVIII INTRODUCTION

facets of continuous-time finance that this book has sought to avoid as a price for simplicity.

The book is structured as follows. Chapters 1 and 2 provide an introduction to the business of finance, risk, and their many applications. Issues such as ethics and finance are discussed.

Chapters 3 and 4 are an introduction to risk measurement and to various statistical approaches to doing it. These chapters use data to measure risk and to estimate financial trends, financial volatility, and the many terms that make up the essential content of basic financial applications. These two chapters introduce the student to the need to confront the measurement, the *quantification* of finance, and to perform basic analyses using financial data. Chapter 4 is of a more advanced nature, however, and emphasizes the problems of dependence including statistical dependence, complexity, contagious risks, latent risks, and black swan risks. The rationale for introducing these complex issues prior to a thorough study of financial and economic constructs used by financial engineers is to point out the true complexity of quant finance, which cannot always be explained by available theories. Allowing students to grapple with complicated issues sooner rather than later offers a challenge that is similar to the concerns and the manner in which we proceed to financial risk management.

Chapters 5 and 6 introduce the concept of utility and financial risk management. Many theories applied in financial economics are applications of or interpreted in terms of utility concepts. These include risk aversion, portfolio selection, certain equivalents in financial valuation, the capital asset pricing model (CAPM), kernel pricing, insurance, and utility-based risk management. These applications are still profusely used (explicitly or implicitly) in many practical problems. The presumption that financial engineering is essentially concerned with options pricing is, I believe, misguided. These chapters will show through applications that underlying financial theory there are almost always three issues to reckon with: the rationality of the parties to a financial transaction, their private and common information, and the market price. In many cases, any two would imply the other. In other words, any model in fundamental finance implies in fact an underlying rationality—which when violated leads to model defaults.

Chapter 7 outlines the Arrow-Debreu framework in discrete states and time for assets and derivatives (options) pricing. An intuitive introduction to martingales and their importance for asset pricing is included in the appendix to Chapter 7. Chapter 8 provides a review of financial markets and optional portfolios used to manage and trade risks. These two chapters present the basic concept of fundamental finance. The theory is discussed, criticized, and applied to many examples. To keep this introduction tractable (without losing its essential implications and applications) simple binomial, multinomial, and discrete state models are used. Extensions to continuous-time finance are considered briefly, and specific problems are posted on the book web site, www.charlestapiero.com. Applications to a variety of problems including derivatives pricing, default bonds, pricing insurance contracts, stochastic volatility models, multiple sources of risks models, and a plethora of problems commonly treated in practice and in advanced texts are also presented simply to explain the rationale that the Arrow-Debreu financial framework uses to solve such problems. Throughout these chapters, issues and instruments of current interest, such as the financial meltdown of 2008, volatility and chaos, globalization, outsourcing, and so on, are used to explain these important facets of financial practice and the limits of the current theoretical models of finance.

Chapters 9, 10, and 11 can be seen as a whole that can be delivered as one course on credit risk. Chapters 9 and 10 deal with credit risk and scoring, multi-name credit risk, and credit derivatives. Several approaches to pricing credit risk are outlined. Following the credit crisis, a greater awareness has developed that these risks ought to be better regulated. Chapter 10 focuses on multi-name credit risk portfolios and structured financial products such as collateralized debt obligation (CDO), collateralized mortgage obligation (CMO), and collateralized loan obligation (CLO). Finally, Chapter 11 addresses the important and practical problems in calculating an implied volatility and an implied risk-neutral distribution. Three approaches are emphasized: parametric, a-parametric, and a utility-rationality-based approach.

Chapters also include:

- **Examples and problems.** These highlight both some of the techniques used in asset pricing and their very broad applications.
- "Test Yourself." Most chapters end with a series of questions to test your newfound knowledge.

WHAT'S ON THE COMPANION WEB SITE

At www.wiley.com/go/tapiero (password: risk) you will find a number of additional resources for this book, including:

- Additional examples, errata, and updates to the book.
- Links to the author's other publications.
- Recommended reading.
- Information about the author's classes at the New York University Polytechnic Institute.

The Instructor's site includes answers to the problems and "Test Yourself" material found in the book, as well as PowerPoint slides and other materials for classroom use.

Contents

Introduction	X
Who This Book Is For	xv
How This Book Is Structured	xvi
What's on the Companion Web Site	xix
CHAPTER 1	
Risk, Finance, Corporate Management, and Society	1
Overview	1
Risks Everywhere—A Consequence of Uncertainty	1
Risk and Finance: Basic Concepts	4
Finance and Risks	6
Financial Instruments	7
Securities or Stocks	5
Example: An IBM Day-Trades Record	5
Bonds	9
Portfolios	10
Example: Constructing a Portfolio	11
Derivatives and Options	12
Real and Financial Assets	15
Financial Markets	16
Option Contracts	16
Problem 1.1: Options and Their Prices	17
Options and Specific Needs	18
Example: Options and The Price of Equity	19
Example: Management Stock Options	19
Options and Trading in Specialized Markets	20
Trading the CO ₂ Index	20
Trading on Commodities (Metal, Gold, Silver, Corn, Oil)	20
Trading the Weather and Insurance	21
Securitization, Mortgage-Backed Securities, and Credit Derivatives	21
Real-Life Crises and Finance	22
The ARS Crisis	22
The Banking-Money System Crisis	23
The 2008 Meltdown and Financial Theory	24
Finance and Ethics	27
Crime and Punishment	29
Summary	30

CONTENTS

CHAPTER 2	
Applied Finance	35
	35
• ••••••	35
Risk Finance and Insurance	35
Infrastructure Finance	36
Finance, the Environment, and Exchange-Traded Funds Indexes	37
Finance and Your Pension	38
Contract Pricing and Franchises	39
Catastrophic Risks, Insurance and Finance	40
The Price of Safety	41
The Price of Inventories	42
Pricing Reliability and Warranties	42
The Price of Quality Claims	43
Financial Risk Pricing: A Historical Perspective	44
Essentials of Financial Risk Management	47
Comprehensive Financial Risk Management	49
Technology and Complexity	49
Retailing and Finance	51
Finance, Cyber Risks, and Terrorism	52
IT and Madoff	52
Virtual Markets	52
Virtual Products	52
Virtual Markets Participants	53
Virtual Economic Universes	53
Market Making and Pricing Practice	53
Market Makers, Market Liquidity, and Bid-Ask Spreads	55
Alternative Market Structures	56
Summary	57
CHAPTER 3	
Risk Measurement and Volatility	63
Overview	63
Risk, Volatility, and Measurement	63
Moments and Measures of Volatility	66
Expectations, Volatility, Skewness, Kurtosis, and the Range	67
Example: IBM Returns Statistics	69
Example: Moments and the CAPM	70
Problem 3.1: Calculating the Beta of a Security	72
Modeling Rates of Return	72
Models of Rate of Returns	73
Statistical Estimations	77
Least Squares Estimation	77
Maximum Likelihood	79
ARCH and GARCH Estimators	80
Example: The AR(1)-ARCH(1) Model	81

Contents	Хi
	

Example: A GARCH (1,1) Model	83
High-Low Estimators of Volatility	83
Extreme Measures, Volume, and Intraday Prices	84
Statistical Orders, Volume, and Prices	85
Problem 3.2: The Probability of the Range	87
Intraday Prices and Extreme Distributions	87
Data Transformation	88
Example: Taylor Series	89
Value at Risk and Risk Exposure	90
VaR and Its Application	92
Example: VaR and Shortfall	94
Example: VaR, Normal ROR, and Portfolio Design	95
The Estimation of Gains and Losses	97
Summary	99
CHAPTER 4	
Risk Finance Modeling and Dependence	109
Overview	109
Introduction	109
Dependence and Probability Models	111
Statistical Dependence	111
Dependence and Quantitative Statistical Probability Models	113
Many Sources of Normal Risk: Aggregation and Risk Factors	
Reduction	114
Example: Risk Factors Aggregation	115
Example: Principal Component Analysis (PCA)	116
Example: A Bivariate Data Matrix and PCA	117
Example: A Market Index and PCA	119
Dependence and Copulas	120
Example: The Gumbel Copula, the Highs and the Lows	123
Example: Copulas and Conditional Dependence	124
Example: Copulas and the Conditional Distribution	125
Financial Modeling and Intertemporal Models	126
Time, Memory, and Causal Dependence	127
Quantitative Time and Change	129
Persistence and Short-term Memory	130
The R/S Index	133
Summary	135
CHAPTER 5	
Risk, Value, and Financial Prices	141
Overview	141
Value and Price	141
Utility, Risk, and Money	143
Utility's Normative Principles: A Historical Perspective	144
Prelude to Utility and Expected Utility	145
Lotteries and Utility Functions	147

X CONTENTS

Example: The Utility of a Lottery	148
Quadratic Utility and Portfolio Pricing	149
Utility and an Insurance Exchange	150
Example: The Power Utility Function	151
Example: Valuation and the Pricing of Cash Flows	152
Example: Risk and the Financial Meltdown	153
Utility Rational Foundations	155
The Risk Premium	155
Utility and Its Behavioral Derivatives	156
Examples: Specific Utility Functions	159
The Price and the Utility of Consumption	161
Example: Kernel Pricing and the Exponential Utility Function	164
Example: The Pricing Kernel and the CAPM	165
Example: Kernel Pricing and the HARA Utility Function	166
The Price and Demand for Insurance	167
Summary	170
CHAPTER 6	
Applied Utility Finance	177
Overview	177
Risk and the Utility of Time	177
Expected Utility and the Time Utility Price of Money	177
Risk, Safety, and Reliability	178
Asset Allocation and Investments	180
Example: A Two-Securities Problem	182
Example: A Two-Stocks Portfolio	184
Problem 6.1: The Efficiency Frontier	185
Problem 6.2: A Two-Securities Portfolio	187
Conditional Kernel Pricing and the Price of Infrastructure Investments	188
Conditional Kernel Pricing and the Pricing of Inventories	191
Agency and Utility	193
Example: A Linear Risk-Sharing Rule	194
Information Asymmetry: Moral Hazard and Adverse Selection	195
Adverse Selection	196
The Moral Hazard Problem	197
Signaling and Screening	199
Summary	200
CHAPTER 7	
Derivative Finance and Complete Markets	205
Overview	205
The Arrow-Debreu Fundamental Approach to Asset Pricing	206
Example: Generalization to n States	210
Example: Binomial Option Pricing	212
Problem 7.1: The Implied Risk-Neutral Probability	213
Example: The Price of a Call Option	213

Contents	
Contante	Χĺ
	w

Example: A Generalization to Multiple Periods	215
Problem 7.2: Options and Their Prices	218
Put-Call Parity	218
Problem 7.3: Proving the Put-Call Parity	219
Example: Put-Call Parity and Dividend Payments	219
Problem 7.4: Options Put-Call Parity	220
The Price Deflator and the Pricing Martingale	220
Pricing and Complete Markets	222
Risk-Neutral Pricing and Market Completeness	224
Options Galore	226
Packaged and Binary Options	227
Example: Look-Back Options	227
Example: Asian Options	227
Example: Exchange Options	228
Example: Chooser Options	228
Example: Barrier and Other Options	228
Example: Passport Options	229
Options and Their Real Uses	229
Fixed-Income Problems	231
Example: Pricing a Forward	231
Example: Pricing a Fixed-Rate Bond	232
Pricing a Term Structure of Interest Rates	232
Example: The Term Structure of Interest Rates	234
Problem 7.5: Annuities and Obligations	235
Options Trading, Speculation, and Risk Management	235
Option Trading Strategies	237
Problem 7.6: Portfolio Strategies	240
Summary	245
Appendix A: Martingales	246
Essentials of Martingales	246
The Change of Measures and Martingales	248
Example: Change of Measure in a Binomial Model	249
Example: A Two-Stage Random Walk and the Radon Nikodym	
Derivative	251
Appendix B: Formal Notations, Key Terms,	
and Definitions	253
CHAPTER 8	
Options Applied	259
Overview	259
Option Applications	259
Risk-Free Portfolios and Immunization	260
Selling Short	261
Future Prices	262
Problem 8.1: Pricing a Multiperiod Forward	264
Pricing and New Insurance Business	20 1

XII CONTENTS

Example: Options Implied Insurance Pricing	266
Option Pricing in a Trinomial Random Walk	267
Pricing and Spread Options	269
Self-Financing Strategy	270
Random Volatility and Options Pricing	271
Real Assets and Real Options	273
The Option to Acquire the License for a New Technology	275
The Black-Scholes Vanilla Option	276
The Binomial Process as a Discrete Time Approximation	277
The Black-Scholes Model Option Price and Portfolio Replication	278
Risk-Neutral Pricing and the Pricing Martingale	281
The Greeks and Their Applications	284
Summary	287
CHAPTER 9	
Credit Scoring and the Price of Credit Risk	291
Overview	291
Credit and Money	291
Credit and Credit Risk	294
Pricing Credit Risk: Principles	296
Credit Scoring and Granting	299
What Is an Individual Credit Score?	299
Bonds Rating or Scoring Business Enterprises	300
Scoring/Rating Financial Enterprises and Financial Products	301
Credit Scoring: Real Approaches	304
The Statistical Estimation of Default	305
Example: A Separatrix	310
Example: The Separatrix and Bayesian Probabilities	311
Probability Default Models	312
Example: A Bivariate Dependent Default Distribution	314
Example: A Portfolio of Default Loans	315
Example: A Portfolio of Dependent Default Loans	316
Problem 9.1: The Joint Bernoulli Default Distribution	317
Credit Granting	317
Example: Credit Granting and Creditor's Risks	319
Example: A Bayesian Default Model	322
Example: A Financial Approach	323
Example: An Approximate Solution	326
Problem 9.2: The Rate of Return of Loans	327
The Reduced Form (Financial) Model	327
Example: Calculating the Spread of a Default Bond	328
Example: The Loan Model Again	329
Example: Pricing Default Bonds	330
Example: Pricing Default Bonds and the Hazard Rate	331
Examples	332
Example: The Bank Interest Rate on a House Loan	333