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Robotic Manipulator Design and construction

Design and synthesis of parallel robotic
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NOMENCLATURE

| | | |
|-----------------|---|--|
| A | - | Pole Area |
| A_{cap} | - | Area of spherical cap |
| A_i | - | Upper platform joint position |
| a_{ix} | - | Upper platform joint co-ordinates in x direction |
| a_{iy} | - | Upper platform joint co-ordinates in y direction |
| a_{iz} | - | Upper platform joint co-ordinates in z direction |
| b | - | Mobility number |
| B_i | - | Lower platform joint position |
| b_{ix} | - | Lower platform joint co-ordinates in x direction |
| b_{iy} | - | Lower platform joint co-ordinates in y direction |
| b_{iz} | - | Lower platform joint co-ordinates in z direction |
| b_{max} | - | Maximum expansion of actuator b_i |
| b_{min} | - | Minimum expansion of actuator b_i |
| B_r | - | Residual Flux density |
| B_t | - | Tool tip location |
| $C(J)$ | - | Condition number of Jacobian matrix |
| $C(J)_{dext}$ | - | Maximum condition number value for dexterous workspace boundary |
| $C(J)_{max}$ | - | Maximum condition number value |
| $C(J)_{total}$ | - | Maximum condition number value for total workspace boundary |
| C_1 | - | Condition number based on norm 1 |
| C_2 | - | Condition number based on norm 2 |
| C_{det} | - | Manipulability index |
| C_{fro} | - | Frobenius norm is denoted by C_{fro} |
| C_{inf} | - | Condition number based on norm infinity |
| c_{nk} | - | Error amount |
| d_{fixed} | - | Actuator fixed length |
| d_i | - | Actuator length |
| d_{ij} | - | Coefficient in n linear equations in β_j |
| d_{max} | - | Maximum expansion of actuator d_i |
| d_{min} | - | Minimum expansion of actuator d_i |
| F | - | Vector of force and moment |
| f | - | Vector of force |
| $F(x)$ | - | Target system |
| F_A | - | Applied force |
| $F_{applied}$ | - | Force applied on the end-effector |
| F_B | - | Magnetic holding force |
| F_{Bi} | - | Tangential component of magnetic holding force |
| f_{def} | - | DOF of i^{th} joint |
| F_{fric} | - | Frictional force |
| f_i | - | Linear actuator force (Only defined for chapter 8 and 10) |
| F_M | - | Frictional force between ball and magnet |
| F_{MN} | - | Normal reaction to the forces exerted from the upper ring and the ball |
| f_p | - | Passive DOF |
| F_{piezo} | - | Output force provided by piezo actuator |
| F_R | - | Frictional force due to the upper ring |
| F_{RN} | - | Normal reaction of frictional force F_R |
| F_{sol} | - | Solenoid force |
| F_x | - | x -component of the manipulator output force |
| F_y | - | y -component of the manipulator output force |
| F_z | - | z -component of the manipulator output force |
| g | - | Number of joints |
| $G(x)$ | - | Start system |
| h | - | Initial height of the manipulator |
| h_c | - | Spherical cap height |
| $H(x,t)$ | - | Homotopy function |
| h_{geom} | - | Manipulator height from the pre-selected actuator geometry |
| $h_{isotropic}$ | - | Manipulator height calculated from isotropic conditions |
| I | - | Identity matrix |
| J | - | Overall Jacobian |

| | | |
|-----------------|---|---|
| $J_{m,n}$ | - | Jacobian matrix of size $m \times n$ |
| J_q | - | Jacobian of actuators |
| J_x | - | Jacobian matrix for end-effector location |
| J_θ | - | Jacobian of twists |
| K | - | Stiffness matrix |
| $k(J)$ | - | Condition number |
| k_d | - | Stiffness of linear actuator |
| k_i | - | Stiffness of individual limb |
| k_{ij} | - | Dimensionless constant |
| k_{sp} | - | Rotational stiffness of joint |
| k_x | - | x -component of manipulator stiffness |
| k_y | - | y -component of manipulator stiffness |
| k_z | - | z -component of manipulator stiffness |
| k_θ | - | θ -component of manipulator stiffness |
| k_ψ | - | ψ -component of manipulator stiffness |
| k_ϕ | - | ϕ -component of manipulator stiffness |
| l_i | - | Constant limb length |
| L_m | - | Magnet length |
| M | - | Mobility or Degree of freedom |
| m | - | Number of rows in Jacobian |
| mg | - | Weight of the inner ball |
| n_c | - | Number of connectors |
| n | - | Number of columns in Jacobian |
| n_e | - | Vector of moment |
| n_{slices} | - | Number of slices in z height |
| O | - | Lower platform centre |
| P | - | Upper platform centre |
| P_o | - | Tightening force of the upper ring |
| $P_{iActual}$ | - | Actual joint location |
| P_{iIdeal} | - | Ideal joint location |
| q | - | Vector for actuators |
| R | - | Transformation rotation matrix |
| r | - | Radius of spherical cap |
| R_b | - | Ball radius |
| $r(J)$ | - | Rank of the Jacobian matrix |
| r_b | - | Radius of base platform |
| r_i | - | Ball radius (Only defined for chapter 10) |
| r_{ix} | - | x co-ordinate of the vector position of the upper joint w.r.t. GCS |
| r_{iy} | - | y co-ordinate of the vector position of the upper joint w.r.t. GCS |
| r_{iz} | - | z co-ordinate of the vector position of the upper joint w.r.t. GCS |
| R_L | - | Pre-defined limits of rotations |
| r_p | - | Upper platform radius |
| $R_{u(\psi)}$ | - | Transformation rotation matrix for ψ direction |
| $R_{v(\theta)}$ | - | Transformation rotation matrix for θ direction |
| $R_{w(\phi)}$ | - | Transformation rotation matrix for ϕ direction |
| S | - | $m \times n$ diagonal matrix consisting of the square roots of the eigenvalues of J_J^T arranged in descending order. |
| s_{bi} | - | Unit vector in the direction b_i |
| s_i | - | Unit vector in the direction d_i |
| s_{ix} | - | Projection in x for unit vector in the direction d_i |
| s_{iy} | - | Projection in y for unit vector in the direction d_i |
| s_{iz} | - | Projection in z for unit vector in the direction d_i |
| s_{li} | - | Unit vector in the direction l_i |
| S_p | - | Twist of the moving platform |
| S_r | - | Reciprocal screw |
| t | - | Continuation parameter |
| T | - | Applied torque |
| T_{error} | - | transformation matrix including the pose errors for the moving platform with respect to the fixed platform |
| T_j | - | Pre-selected random points making the plane |
| T_L | - | Pre-defined limits of translations |
| u | - | Upper platform translation in x direction |
| U | - | $m \times m$ orthogonal matrix consisting of the eigenvectors of JJ^T |

| | | |
|-----------------|---|--|
| U_p | - | Local upper platform co-ordinates w.r.t. point P |
| u_x | - | Upper platform projection of u -axis w.r.t. global x -axis |
| u_y | - | Upper platform projection of u -axis w.r.t. global y -axis |
| u_z | - | Upper platform projection of u -axis w.r.t. global z -axis |
| v | - | Upper platform translation in y direction |
| V | - | $n \times n$ orthogonal matrix consisting of the eigenvectors of $J^T J$. |
| v_p | - | Velocity vector of point ' P ' |
| v_x | - | Upper platform projection of v -axis w.r.t. global x -axis |
| v_y | - | Upper platform projection of v -axis w.r.t. global y -axis |
| v_z | - | Upper platform projection of v -axis w.r.t. global z -axis |
| w | - | Upper platform translation in z direction |
| W | - | Weight of the ball |
| w_A | - | Angular velocity of upper platform |
| w_i | - | Angular velocity of i^{th} limb |
| w_p | - | Angular velocity of the moving platform |
| w_x | - | Upper platform projection of w -axis w.r.t. global x -axis |
| w_y | - | Upper platform projection of w -axis w.r.t. global y -axis |
| w_z | - | Upper platform projection of w -axis w.r.t. global z -axis |
| x | - | x direction |
| X | - | End-effector location and orientation vector |
| y | - | y direction |
| Y | - | An example vector |
| z | - | z direction |
| z_{end} | - | End of z height of the manipulator workspace |
| z_{start} | - | Start of z height of the manipulator workspace |
| α | - | Second limb placement angle with respect to the first limb |
| β | - | Third limb placement angle with respect to the first limb |
| β_j | - | Number of groups of variables |
| Γ | - | Random complex constant |
| γ_i | - | Base inclination angle with respect to ground |
| δ | - | Linear actuator travel range |
| δL_i | - | Change in actuator length |
| δp | - | Change in kinematic parameters |
| Δq | - | Small change in the vector of actuators |
| δq | - | Virtual displacement associated with actuators |
| ΔX | - | Small change in position and orientation vector of the end-effector |
| δX | - | Virtual displacement associated with the end-effector |
| ε | - | Angular increment |
| ε_i | - | General variable for α and β |
| ζ | - | Inclination of legs over the base platform |
| θ | - | Angular rotation about v axis |
| θ_d | - | Actuator inclination over base |
| θ_c | - | Angular range in spherical cap |
| θ_{sp} | - | Ball rotation angle |
| λ_{max} | - | Largest eigenvalue of Jacobian matrix |
| λ_{min} | - | Smallest eigenvalue of Jacobian matrix |
| τ | - | Vector of actuated joint torque |
| ψ | - | Angular rotation about u axis |
| ϕ | - | Angular rotation about w axis |
| $[T]_L^U$ | - | Upper platform transformation w.r.t. Lower platform |
| x | - | Velocity vector for end-effector location and orientation |
| \dot{q} | - | Velocity vector of actuators |
| b_i | - | Velocity vector of actuators |
| $\theta_{j,i}$ | - | Magnitude of the twist of the j^{th} joint of the i^{th} limb |
| $\hat{S}_{j,i}$ | - | Unit screw associated with the j^{th} joint of the i^{th} limb |
| $\ \cdot\ $ | - | Matrix norm |
| μ | - | Coefficient of friction |
| μ_M | - | Coefficient of friction between magnet and the ball |
| μ_R | - | Coefficient of friction between upper ring and the ball |

LIST OF ABBREVIATIONS

| | | |
|-------------|---|---|
| <i>D.C.</i> | - | Duty Cycle of the solenoid |
| <i>DOF</i> | - | Degree of Freedom |
| <i>EDM</i> | - | Electro-discharge machining |
| <i>GCS</i> | - | Global co-ordinate system |
| <i>GK</i> | - | Grubler Kutzbach equation |
| <i>LCS</i> | - | Lower co-ordinate system |
| <i>PKM</i> | - | Parallel Kinematic machine |
| <i>PRPS</i> | - | Prismatic-Revolute-Prismatic-Spherical |
| <i>PRS</i> | - | Prismatic-Revolute-Spherical |
| <i>PSPS</i> | - | Prismatic-Spherical-Prismatic-Spherical |
| <i>PSS</i> | - | Prismatic-Spherical-Spherical-Spherical |
| <i>RP</i> | - | Rapid prototype |
| <i>RPS</i> | - | Revolute-Prismatic-Spherical |
| <i>SPS</i> | - | Spherical-Prismatic-Spherical |
| <i>SVD</i> | - | Singular Value Decomposition |
| <i>UCS</i> | - | Upper co-ordinate system |
| <i>UPU</i> | - | Universal-Prismatic-Universal |
| <i>UPS</i> | - | Universal-Prismatic-Spherical |

DEDICATION

Dedicated to my wife, Tayyaba