

# QUANTITATIVE METHODS FOR BUSINESS DECISIONS

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# PREFACE

"Learning without thought is labor lost; thought without learning is perilous."

Confucius

The purpose of this book is to provide a basic learning resource for the study of quantitative methods. To this end we have incorporated a number of unique features designed to make the book interesting, readable, and useful:

Thorough explanations that appeal to intuition rather than use mathematical proof

Behavioral learning objectives for each chapter

In-chapter practice exercises with complete solutions

Case studies to expand learning horizons

Chapter sections on "real world" experiences that illustrate the implementation of quantitative methods

Many end-of-chapter exercises

Part I, Fundamentals of Quantitative Methods, sets the stage with discussions of quantitative methods, models, and data. It reflects our philosophy that quantitative methods can assist managerial decision making but cannot replace experienced judgment.

Part II, Making Rational Decisions, looks at elements of statistical decision theory. A treatment of the payoff matrix and decision trees is provided. Game Theory is also included here for its conceptual contributions to decision making.

Part III, Planning Business Activities, includes explanations of the methods most commonly used to aid managerial planning, together with examples of their application. Topics include forecasting, linear programming, Markov analysis, and project planning.

Part IV, Balancing Cost and Service, focuses on two common decision areas: inventory control and waiting lines. In these areas we have tried to develop the reader's intuitive understanding of the decisions to be made. This is important if quantitative methods are to be truly effective.

Part V, Solving Problems by Modeling System Behavior, focuses on the important topic of simulation. We close with Part VI, Maintaining a Managerial Perspective, a title which expresses one of our goals throughout the book.

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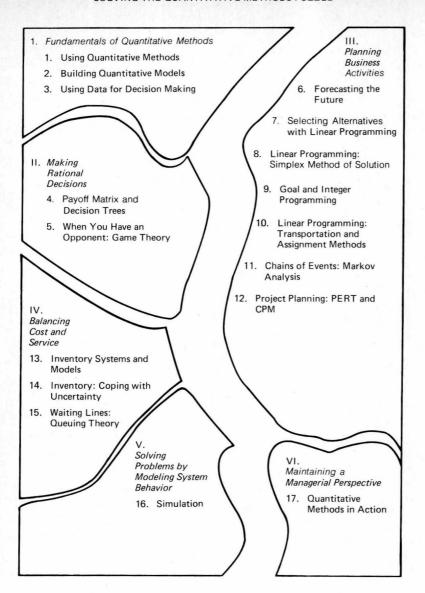
The level of mathematics has been held to a minimum throughout. Neither calculus nor matrix algebra is used. Algebra plus an elementary knowledge of probability and statistics are all that will be needed.

There is sufficient material in the book for a one-semester or twoquarter course at either the undergraduate or graduate level. Selective material could be ommitted if only a one-quarter course is desired. The order in which chapters are covered can be greatly varied since many of the chapters are independent of the others.

We have been fortunate in receiving important help from many people. Our thanks go, especially, to Samuel Newman for his help in planning the book. Also to Eugene T. Byrne, Janet C. Goulet, David C. Murphy, and Diane R. Walker for their help in review; and to Paul R. Merry who made many excellent comments and helpful criticisms. Last but not least, our thanks go to Susie Findell, Cynthia Downing, Martha Simkins, Martha Tyler, and Nicky O'Hair for their help in typing the manuscript. Of course, the authors are solely responsible for errors in content.

Charles A. Gallagher Hugh J. Watson

#### SOLVING THE QUANTITATIVE METHODS PUZZLE



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