

# Computational Mechanics '86

Theory and Applications

Volume 2

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## **Theory and Applications**

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**Volume 2**

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## Preface

It is often said that these days there are too many conferences on general areas of computational mechanics, mechanics, and numerical methods. While this may be true, the history of scientific conferences is itself quite short. According to Abraham Pais (in "Subtle is the Lord...", Oxford University Press, 1982, p.80), the first international scientific conference ever held was the Karlsruhe Congress of Chemists, 3-5 September 1860 in Karlsruhe, Germany. There were 127 chemists in attendance, and the participants came from Austria, Belgium, France, Germany, Great Britain, Italy, Mexico, Poland, Russia, Spain, Sweden, and Switzerland. At the top of the agenda of the points to be discussed at this conference was the question: "Shall a difference be made between the expressions molecule and atom?" Pais goes on to note: "The conference did not at once succeed in bringing chemists closer together... It is possible that the older men were offended by the impetuous behavior and imposing manner of the younger scientists" (see references cited in Pais' book). It may be observed that history, in general, repeats itself. However, at ICCM-86 in Tokyo, roughly 500 participants from both the West and the East were in attendance; there were only scholarly exchanges; the young tried to learn from the more experienced, and a spirit of international academic cooperation prevailed.

In the past 25 years, the field of computational mechanics has steadily emerged as a discipline that is poised to make revolutionary changes to the practice of engineering in developed countries as well as in emerging industrial societies. The field has become vast, encompassing the work of the engineer, the mechanician, the mathematician, the numericist, the computer scientist, the systems analyst, as well as the computer enthusiast. The aim of the present series of International Conferences on Computational Mechanics (ICCM), planned to be held every 2 years, is to become a forum for discussion and exchange of scholarly research in those areas of computational mechanics which involve and enrich the rational application of mechanics and numerical methods in the practice of modern engineering. The areas of research that are to be discussed include: solid and structural mechanics; constitutive modeling; inelastic and finite deformation response; transient analysis; structural control and optimization, fracture mechanics and structural integrity; computational fluid dynamics; compressible and incompressible flow; aerodynamics; transport phenomena;

heat transfer and solidification; electromagnetic field, related solid mechanics and MHD; and modern variational methods in general. It is believed that this diversity of topics will play a crucial role in the cross-fertilization of ideas.

That the above-stated objectives of ICCM were amply met at the first conference, held from 25 to 29 May 1986 at the Science University of Tokyo, is evidenced by the excellent work presented by distinguished scholars from all over the world and documented in these proceedings.

The Editors take great pleasure in expressing their sincere thanks to the members of the Organizing Committee, the International Steering Committee, and the National Organizing Committee of ICCM-86, Tokyo for their help in realizing the objectives of this conference. The Editors also thank their colleagues in many parts of the world who have kindly accepted the invitations to present their work at ICCM-86 and prepare their papers for inclusion in the conference proceedings.

It is the sincere hope of the Editors that the readers of these two volumes will find, recorded here, a kaleidoscopic picture of the state-of-the-art in diverse areas of computational mechanics, its theory, and its application in various parts of the world.

May 1986

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and

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## Table of Contents: Volume 1

### Chapter I Plates and Shells

Some Problems of Shearing and Twisting of Shallow Spherical Shells (E. Reissner) .....	I-3
Formulation of Reissner-Mindlin Moderately-Thick/Thin Plate Bending Elements (D.P. Chen, Y.S. Pan) .....	I-13
Deformations and Stresses in Shallow Spherical and Paraboloidal Domes with Polar Openings under Rotationally Symmetrical Loads (O.A. Fettahlioglu, A.M. Sayed).....	I-19
Algorithms for Nonlinear Contact Constraints with Application to Stability Problems of Rods and Shells (P. Wriggers, W. Wagner, E. Stein).....	I-33
A Quadrilateral Membrane Element with Rotational Freedoms (P.G. Bergan, M.K. Nygård) .....	I-41
The Finite Element Method of Viscoelastic Large Deformation Plane Problem with Kirchhoff Stress Tensors-Green Strain Tensors Constitutive Relation (Y-P. Shen, Y-H. Chen) .....	I-51
A Shape Function Routine for a Thin, Curved Beam Finite Element (L.F. Roswell) .....	I-57
Influence of Element Form on Accuracy in Isoparametric Elements (Y. Wu) .....	I-65
Two Shear Deformable Plate Theories Vis-a-Vis Two Discrete Methods (T. Kant') .....	I-69
Elasto-Plastic Analysis of Thick Walled Cantilevered Tubes (A.L. Deak) .....	I-77
Numerical Investigation of the Deformation Behavior of Elastic-Plastic Circular Thick-Walled Tubes under External Pressure and Axial Load (Y. Tomita, A. Shindo, Y.S. Kim) .....	I-83

Practical Method of Analysis of Rectangular Plates with Holes and Complicated Boundary Conditions by the Use of Spline Functions (R. Zhou, G. He) .....	I-89
A Mixed Finite Element Method for Layered Composite Plates (J.E. Akin, Y.W. Kwon) .....	I-95
On the Selection of Stress Parameters for Hybrid/Mixed Finite Elements (T.Y. Chang, A.F. Saleeb) .....	I-103
Quadratic Spline Thick/Thin Plate Triangular Hybrid Elements (S. Yuan) .....	I-111
Reasonable Selection of the Stress Modes in a Hybrid Stress Element (J. Zhao) .....	I-117
Development of Hierarchical Finite Element Methods at BIAA (D-C. Zhu) .....	I-123
Reduced Integration, Nonconforming Modes, and their Coupling in Finite Elements (C-K. Choi, S-H. Kim) .....	I-129
Thick Shell Elements with Optimal Transverse Shear Interpolation (M. Tateishi, J.C. Nagtegaal, S. Nakazawa) .....	I-135
Stiffened and Continuous Annular Sector Plates (I.E. Harik, B.F. Haddad) .....	I-143
The Finite Strip-Element Method (H. Wang, J. Zhang) .....	I-151
An Optimally Controlled Four-Node Quadrilateral Element for Reissner-Mindlin Plate (L-Y. Tong) .....	I-157
The Recent Advances of MWR for Solid Mechanics in China (C. Xu) .....	I-163
A Study of the Isoparametric Timoshenko Beam Element with Reduced Integration (T. Yokoyama, K. Kishida, K. Nakagawa) .....	I-173
Finite Element Models Based on the Method of Weighted Residuals (H.Y. Yang, Z.G. Zhao, L.J. Ni) .....	I-179
On Simple Finite Element Methods for Mindlin Plates (J. Pitkäraanta) .....	I-187
Panpenalty Finite Element Method (Y. Gao, K-C. Hwang) .....	I-191
Further Discussion of the New Lagrangian and Serendipity Degenerated Shell Elements (H.C. Huang) .....	I-197

**Chapter II**  
**Solid and Structural Mechanics**

On a Combined Stability and Contact Problem Concerning Multi-Lamellae Compression Flanges of I-Beams (Z.S. Chen, H.A. Mang) .....	II-3
A Variational Framework for n-th Order Invariant Continuum Mechanics (R. Segev) .....	II-11
The Formulation and Solution of the Governing Equations of Motion for Three-Dimensional Linear Viscoelastodynamics (P.K. Wong) .....	II-17
Quasi-Generalized Virtual Work Principle and 3-Kind Variable of Generalized Variational Principle in Elastic Theory (R-S. Tang) .....	II-23
The Buckling Problem of Non-Homogeneous Beam (S.J. Zhou) .....	II-29
The Exact Solution of Unequal Thickness Plate Problem (C.Z. Li) .....	II-33
Automatic Input of Computer Analysis in the Saw-tooth Transverse Bents (J.K. Zhong) .....	II-39
Computer-Aided Nondestructive Measurements of Plastic Strains from Surface Displacements (T. Mura, B. Cox, Z. Gao) .....	II-43
Approximate Modal Coupling of Multi Degree of Freedom Substructures: Primary and Secondary Systems (B. Zastraub) .....	II-49
Aero-Hydroelasticity and Stress of Spacers for Fuel Elements as Structural Anisotropic Domes Composed of Cylindrical Shells (V. Kuželka) .....	II-55
A Finite Element Model for the Lateral Strength of Railroad Track Structures (J.E. Jackson, Jr., N.R. Bauld, M. Ramesh) .....	II-61
Edge Effect of Hyperbolic Cooling Tower Supported by Column System (W. Lu, R. Shao, Z. Xu) .....	II-67
Effect of Structural Twisting on the Optimal Stiffness of Shear Wall in Tall Building (Q. Wang) .....	II-73
A Minimum Principle on Displacements and a Related NLP Formulation for the Elastostatics of Cable Systems (M. Cannarozzi, R. Contro) .....	II-79
An Adaptive Dynamic Relaxation Method for Static Problems (P. Tong) .....	II-89

Elastic Analysis of a Cylindrical Storage Tank by the Coupling Method of Boundary and Finite Elements (S. Yoshida, T. Miyoshi) .....	II-103
A Semi-Analytical Finite Strip for Continuous Plate Structures (B.W. Golley, M.A. Hamstead) .....	II-109
Use of Off-Set Beam Elements in a Model for Torsional Deflection Analysis of a Grid Structure of Open Cross Sections (N. Toda, N. Yoshimura) .....	II-115
Transient Response of a Bent Boom of Variable Cross Section with Link Joints Subjected to General Transient Loads (K. Nagaya) .....	II-121
Materially Nonlinear Large Displacement Analysis of Structures Using Reduced Basis Technique (L.R. Savić) .....	II-127
The Limit Analysis of Spatial Frames (T. Chen, W. Shen) .....	II-133
Indentation of a Plane Membrane with a Rigid Paraboloid (W.W. Feng) .....	II-139
Finite Element Modelling of Dynamic Contact Application for Blade Root Damping Estimation (C.V. Ramakrishnan, M.A.W. Usmani) .....	II-147
An Extended Penalty Function Method and its Application to a Virtual Work Principle for Impact Contact of Two Bodies (N. Asano, K. Funatsu) .....	II-155
Contact Forces and Stresses in Cables (C-H. Chien, G.A. Costello, L-C. Chang) .....	II-161
On Numerical Methods in Three-Dimensional Theory of Deformable Bodies Stability (A.N. Guz) .....	II-169
A Finite Element Approach for Repeated Elastic-Plastic Rolling Contact (V. Bhargava, G.T. Hahn, C. Rubin) .....	II-177
A Variational Approach to Plates on Elastic Foundations (N.S.V. Kameswara Rao) .....	II-187
Numerical Treatment of Singularities in Elastic Contact Problems and Applications (V.I. Fabrikant, T.S. Sankar) .....	II-195
Finite Element Analysis of Beams on Two-Parameter Tensionless Foundations (Z.. Feng) .....	II-205
The Finite Element Analysis of the Contact Problem in Bearing (R. Yu, Y. Liu) .....	II-211

**Chapter III**  
**Nonlinear Structural Problems**

Plastic Deformation of Inhomogeneous Materials with Elliptic Inclusions (T. Abe, S. Nagaki, N. Nagayama) .....	III-3
A New Analytical Model of Necking Phenomenon (Z-B. Kuang, N. Su, Z-H. Li) .....	III-9
The Plastic Strain Modes and their Application in Elasto-Plastic Analysis (D. Zhu) .....	III-17
A Finite Element Analysis of the Punch Press Forming of Thin Elastic-Plastic Plates (E. Nakamachi) .....	III-23
FE-Modelling of Continuous Casting Problem (P. Koikkalainen, E. Laitinen, S. Louhenkilpi, P. Neittaanmäki, L. Holappa) .....	III-29
On the Relations between the 'Flow' and 'Solid' Approaches in the Metal Forming Process (W-C. Zhang) .....	III-37
Thin Extensional Beams under Large Deformations: Variational Principles, Global Bounds, Stability (H. Bufler, R. Lautenbach, H. Schneider) .....	III-45
Some Considerations on Variational Principle for Elastic Rods with Finite Rotations in Space (M. Iura) .....	III-53
A Practical Large Displacements In-Plane Analysis of Elastic Beams (K.M. Hsiao, F.Y. Hou) .....	III-59
Large Deflection Analysis of Elastoplastic Bending (Z.E. Ma) .....	III-65
Finite Deformation of a Bar Bent through Finite Circular Supports (B.W. Golley) .....	III-71
A Recurrence Formula for Viscoelastic Constitutive Equations (W.W. Feng) .....	III-77
Effect of Elastic Strains in Steady-State Elasto Visco-Plastic Flow (Y. Shimazaki, T. Shiojima) .....	III-83
An Approach to the Numerical Analysis of a Generalized Plane Elastica (Z.E. Ma) .....	III-89
Large Deflection Geometrically Nonlinear Behaviour of Laterally Loaded Segmental Plates (A.B. Sabir, H.G.V. Avanessian) .....	III-97
Large Deflection of Plates Using Charge Simulation Method (J. Raamachandran) .....	III-103

A Finite Element Formulation for Geometrically Non-Linear Problems Using a Secant Matrix: Application to 3-D Trusses (S. Rizate, J. Oliver, J. Miquel-Canet, B. Suarez) ... III-109
The Relationship between Twist Axis and Effective Torsional Stiffness of a Motorcycle Frame (M. Raines, G.E. Roe, T.E. Thorpe) ..... III-117
Elastic Buckling of Plates with Reinforced Square Holes (A.B. Sazir, F.Y. Chow) ..... III-125
Collapse, Progressive Buckling and Fatigue Strength of Cylindrical Tubes in Offshore Structures (T. Nomoto, M. Enosawa) ..... III-131
Buckling of Eccentrically Stiffened and Framed Orthotropic Spherical Shells under External Pressure (M. Yamada) ..... III-137
Inelastic Stability Response of Thin Shells (A. Tésář) ..... III-143
Bifurcation and Postbuckling Analysis of Columns with Consideration of Pointwise Elastic-Plastic Deformation History (L. Cheng, W. Yang, K-C. Hwang) ..... III-149
Finite Element Analysis of the Stability of Open Thin-Walled Structure with Diaphragms (X. Yuan, T. Jin, M.X. Liu, L. Li) ..... III-155
Numerical Analyses of Dynamic Contact Buckling Problems Using the Penalty Finite Element Method (Y. Kant, G. Yagawai) ..... III-161
Reissner-Mindlin Plate Element for Large Deflection Problem (Y. Ueda, H. Murakawa, H. Masuda) ..... III-167
Bifurcation and Post-Bifurcation Phenomena of Elastic-Plastic Circular Tubes Subjected to External Shrinking under Plane Strain Condition (Y.S. Kim, Y. Tomita, A. Shindo) ..... III-173
Contribution to Nonlinear Finite Element Analysis of Structures with Emphasis on Buckling and Post-Buckling Problems (J. Chróściszewski, R. Schmidt) ..... III-179
Numerical Analysis of Post-Buckling Behavior of Elastic Plastic Arches (T. Ito, K. Kawashima) ..... III-185
Large Deformation and Post-Buckling Analyses of Plane and Space Truss Structures: Simplified Finite Element Analysis Considering Member's Buckling (K. Kondoh, K. Tanaka) ..... III-191
Finite Element Analysis of Creep Crack Growth Based on Anisotropic Creep Damage Theory (S. Murakami, M. Kawai, H. Rong) ..... III-197

Computer Simulation of Deformation and Fracture of Small Metal Crystals (M. Doyama, R. Yamamoto) .....	III-203
Computational Method of Continuous Dislocations Model (T. Shioya, K. Fujimoto) .....	III-209
The Statistical Fracture Mechanics Analysis of Spherical Tank Failure Probability (Z. Zhou, X. Lu) .....	III-215
Modelling of Fracture Processes Occurring in the Focal Zone of a Tectonic Earthquake (A.S. Bykovtsev) .....	III-221

#### **Chapter IV Material Modeling and Analysis**

Mechanical Sublayer Model for Elastic-Plastic Analyses (T.H.H. Pian) .....	IV-3
Coupling between Temperature, Stress and Metallic Structures during Phase Transformation and the Analysis of Carburized Quenching of a Steel Gear (T. Inoue, Z.G. Wang) .....	IV-11
Time Integration of Stiff Inelastic Constitutive Equations (F.G. Kollmann) .....	IV-17
Analytical Representation for the Cyclic Stress-Strain Hysteresis Loops of Type 304 Austenitic Stainless Steel (Y. Wada, K. Iwata, K. Aoto, Y. Kawakami) .....	IV-25
Elastic-Plastic Constitutive Equation Using Non-Orthogonal Curvilinear Coordinates and its Application in Numerical Methods (X. Ren) .....	IV-31
A Method to Estimate Isothermal Creep under Arbitrary Uniaxial Stress-Reversals (M. Partl, A. Rösli) .....	IV-39
On the Elastic-Plastic Constitutive Equations in Incremental Form (M. Gotoh) .....	IV-45
Constitutive Modeling of Cyclic Plasticity Considering Induced Anisotropy (H. Ishikawa, K. Sasaki) .....	IV-51
Finite Element Formulation for an Elasto-Viscoplastic Anisotropic Strain Hardening Material (C.F. Yen, K.F. Wang, S.H. Kuo) .....	IV-57
Elastoplastic Constitutive Model with a Subloading Surface (K. Hashiguchi) .....	IV-65

An Integral Representation for Plastic Strain of an Elastic-Plastic Solid (S. Ogawa) .....	IV-71
Jet Locality as Implied by Body Self-Determinism and Continuity (R. Segev, A. Ailon) .....	IV-77
The Variations of Flow Stress and Coercivity of Dual Phase Steel during the Reverse Flow (M.T. Ma, Z.B. Sun) .....	IV-83
An Iterative Method for Elastic-Plastic Stress Analysis (T. Miyoshi, K. Kaminishi, S. Kawano, S. Shimizu) ...	IV-89
Constitutive Modeling under High Temperature and High Strain Rate Loading Conditions (A.M. Rajendran, S.J. Bless) .....	IV-95
Elaboration of a Constitutive Model of Cyclic Plasticity under Non-Proportional Loading (E. Tanaka, S. Murakami, M. Ooka) .....	IV-101
Computer-Aided Systematic Formulation of Inelastic Constitutive Equations of Polycrystalline Metals (M. Tokuda, K. Yamada) .....	IV-107
Finite Element Analysis for Shape Memory Alloy (E. Tachibana, M. Nishikawa, K. Watanabe) .....	IV-113
The Prediction of Transient Responses of Spinal Motion Segments Using Finite Elements Based on Porous Medium Theory (J.S.S. Wu, J.C. Huang, T.M. Lee, B.R. Simon) .....	IV-119
Axial Cyclic Hardening Behavior of Metallic Materials under a Constant Shear Stress (M-C. Yip, C. Yu) .....	IV-125
Constitutive Equations of Arterial and Ventricular Wall Tissues Based on Pressure-Volume Relations (H. Abé) .....	IV-131
On the Simulation of Respiratory Dynamics (Y. Seguchi, Y.C. Fung, H. Nagatani) .....	IV-137
An Analysis of Refractive Surgery by the Finite Element Method (M. Bercovier, K. Hanna, F. Jourve) .....	IV-143
Constitutive Law of the Arterial Wall and Stress Distribution (K. Takamizawa, K. Hayashi) .....	IV-149
Analysis of Fibre Reinforced Composite Structures Using Finite Element Method (K.P. Rao) .....	IV-155
Stability Analysis of Composite Plates (O.O. Ochoa, F. Kozma, J.J. Engblom) .....	IV-161
Stress Analysis of FRP Bonded Structure and its Considerations (J. Oda, M. Ushiroji) .....	IV-167