
Economics and consumer behavior

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Cambridge University Press
Cambridge
London · New York · New Rochelle
Melbourne · Sydney

Published by the Press Syndicate of the University of Cambridge
The Pitt Building, Trumpington Street, Cambridge CB2 1RP
32 East 57th Street, New York, NY 10022, USA
296 Beaconsfield Parade, Middle Park, Melbourne 3206, Australia

© Cambridge University Press 1980

First published 1980

Printed in the United States of America

Typeset by Progressive Typographers, Inc., Emigsville, PA

Printed and bound by Vail-Ballou Press, Inc., Binghamton, NY

Library of Congress Cataloging in Publication Data

Deaton, Angus.

Economics and consumer behavior.

Bibliography: p.

Includes index.

1. Consumption (Economics) 2. Consumers.

3. Utility theory. I. Muellbauer, John, joint author.

II. Title.

HB801.D36 658.8'34 79-17090

ISBN 0 521 22850 6 hard covers

ISBN 0 521 29676 5 paperback

PREFACE

This book is about the economic theory of consumer behavior and its uses in economic analysis. It is about the tools and language of utility theory and their application to a field that ranges from empirical work on commodity demand to abstract questions of social choice. The basic theory is the familiar one, *although we have made extensive use of cost functions and related "duality" concepts to present it in a way that simplifies what is often seen as difficult or inaccessible material.* This, and the range of subject matter, broader than any *previous book on consumer behavior,* are the most distinctive features of the book. Our main purpose in writing it is to provide in one place a complete toolbox of utility theory together with a demonstration of the power of these tools in action over a wide front of economics. Although the use of utility theory runs as a common thread throughout the book, *only a fraction of the space deals with the standard textbook model of choice subject to a linear budget constraint.* In recent years, *important work has been done in many areas of economics by applying consumer theory to nonstandard situations, for example, to discrete choice, to rationing, to labor supply, to fertility, to quality choice, to choice with complex nonlinear budget constraints resulting from tax and benefit systems, liquidity constraints, uncertainty, and so on.* Most of this work emphasizes careful modeling of the *constraints* that consumers face, including the statistical and econometric consequences. We believe this to be a productive approach and much of the book is concerned with it. There is a further area of economics that uses consumer theory as an essential input and that has progressed rapidly in recent years. This is the field of welfare economics, including index number theory and social choice. Many of the important developments in that field are based on straightforward applications of the theory discussed in this book, and we include these examples as part of our catalog of the usefulness of utility theory in economics.

The book is designed to be used in courses teaching theoretical and applied economics at the level of final year undergraduates (particularly Part One) and of graduate courses leading to M.A. and Ph.D. degrees. It should also be of use to professional economists who have a direct or indirect interest in consumer behavior. The structure of the book is designed to permit maximum flexibility in use. Part One, which covers the basic theory and its applications,

including the consumption function, durable goods and labor supply, is a self-contained module. Except where indicated, this material is written to be accessible to final year undergraduates and can be used as an introductory complete course or as a refresher for those who want a straightforward presentation of duality in demand theory. Part One is also a prerequisite for other sections of the book. Part Two is a largely theoretical discussion of aggregation and separability; this will be of greatest interest to specialists in economic theory (e.g., in a graduate theory course), but the main issues are discussed informally in the early sections of both chapters. Part Three is on welfare economics; the chapters on index numbers and household welfare comparisons are straightforward and form a natural extension to Part One for undergraduate use. The chapter on social choice and inequality is inevitably more difficult and is at a similar level to the material on separability. Part Four is more heterogeneous and is designed largely for graduate use. In each of the topics discussed we have attempted to face the subject matter on its own terms, going well beyond traditional confines when the material demands it. If the discussion occasionally becomes difficult, we hope it will be rewarding, because it is in these chapters that many of the most interesting applications of consumer theory are to be found. Given Part One, Chapters from 10 through 14 can be combined in numerous combinations with blocks from Parts Two and Three. We also envisage much of this material, particularly Chapters 11, 12, and 13 on labor supply, the consumption function, and durable goods, as well as Chapter 3 of Part One, being used as parts of applied econometrics courses. Even so, although we frequently discuss the formulation of likelihood functions and present empirical results, we have spent little time on specifically econometric issues, mostly for reasons of space.

There are no mathematical prerequisites for this book other than a good knowledge of calculus, including partial differentiation, and a familiarity with notions of concavity and the basic concepts of mathematical statistics. Unlike many texts on consumer theory, this book makes little use of matrix algebra apart from the largely notational use of vectors and dot products. In Chapters 1 through 8, which contain the material that is generally suitable for undergraduate work, harder sections are starred (*) or double starred (**); the latter can be omitted at first reading even by a reader continuing to Part Four. We have included over three hundred exercises that seek to complete, reinforce, or extend the material in the text. Those which are more difficult than their immediate neighbors are starred; some of these are very difficult indeed. Each chapter ends with a guide to further reading and all works cited are listed together at the end of the book.

Writing this book, we have accumulated debts to many people. Intellectual debts are the most important and the hardest to quantify, but the influence, work, and example of both Richard Stone and Terence Gorman have had

great effects over the years on the way we have come to approach the subject. More specifically, we have been heavily dependent on the advice and comments of colleagues who read preliminary drafts of chapters on specialist subjects. In this context we should like to thank David Demery, Peter Hammond, Oliver Hart, Tony Jackson, Richard Layard, Richard Lecomber, and Amartya Sen. General comments, particularly on drafts of the early chapters, were made by Erwin Diewert, Avinash Dixit, Ben Fine, the late Miles Fleming, Arnold Merkies, Jan van Overhagen, and Henri Theil. We are especially grateful to Gerald Kennally who read and commented on it all. Not least, several groups of students at the universities of Amsterdam, Bristol, and Birkbeck, London, suffered through early versions; the protests of John Wrigglesworth, in particular, were most effective in securing remedial action. The typing was done with great speed, precision, and unfailing pleasantness by Mary Harthan and Gillian Baker in Bristol. Finally, our greatest thanks go to Helge and to Catherine who put up with us while we wrote it.

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Consumer demand analysis

The limits to choice • Preferences and demand
• The theory at work • Extensions to the basic
model

The limits to choice

Consumer behavior is frequently presented in terms of preferences, on the one hand, and possibilities on the other. The emphasis in the discussion is commonly placed on *preferences*, on the axioms of choice, on utility functions and their properties. The specification of which choices are actually available is given a secondary place and, frequently, only very simple possibilities are considered. In this book, we shall have a great deal to say about preferences, and discussion of them begins in Chapter 2. We begin, however, with the *limits to choice* rather than with the choices themselves. Unlike preferences, the opportunities for choice are often directly observable so that, to the extent that variations in behavior can be traced to variations in opportunities, we have a straightforward and objective explanation of observed phenomena. It is our view that much can be so explained and that the part played by preferences in determining behavior tends to be overestimated. Hence, this first chapter considers what can be said about behavior without detailed consideration of how choices are made. A large part of this book, from Chapters 2 to 9, works with one very special assumption about the opportunity set, namely that choices are constrained by fixed, known prices in such a way that the total value of the objects chosen should not exceed some predetermined total. In this case, we say that the consumer faces a linear budget constraint. A detailed examination of more complex situations is postponed until Chapters 10 to 14 by which stage the basic material will have been covered. Although this later analysis is technically more difficult, nonlinear budget constraints arise frequently in practice and in §1.1 we present a largely diagrammatic survey of both the linear and nonlinear cases. This provides an elementary introduction to the later material as well as providing a preview of the topics to be covered in the rest of the book. For uniformity of usage, the limits to choice will be described through the “constraints” facing consumers even though, for the moment, nothing is being optimized. Indeed, no formal assumptions are made about choice itself; for the most part, the likely implications of the constraints under consideration will be obvious enough.

Section 1.2 focusses on the simple linear budget constraint that underlies much of the subsequent analysis. Again, without specific assumptions about choices, we can make quite far-reaching deductions about behavior and we

explore the consequences of these for empirical analysis. Finally, as a preparation for Chapter 2, we use a model of *irrational* choice proposed by Becker (1962) to suggest that the use of preference orderings is only one way in which models of consumer behavior may be completed.

1.1 The nature of opportunity sets

The linear budget constraint

The simplest and single most important type of opportunity set is that which arises when the household has an exogenous budget, outlay or total expenditure x , which is to be spent within a given period on some or all of n commodities. These can be bought in nonnegative quantities q_i at given fixed prices p_i . The constraint can then be written

$$x \geq \sum_{i=1}^n p_i q_i \quad (1.1)$$

When $n = 2$, (1.1) is illustrated in Figure 1.1 by the area in the triangle $A0B$ since q_1 and q_2 must be nonnegative. The coordinates of the points A and B are marked; at A all of the budget is spent on good 2 so that $q_2 = x/p_2$ and $q_1 = 0$ and conversely at B . Note an immediate complication which arises if there is a basic survival constraint. An example is illustrated in the diagram.

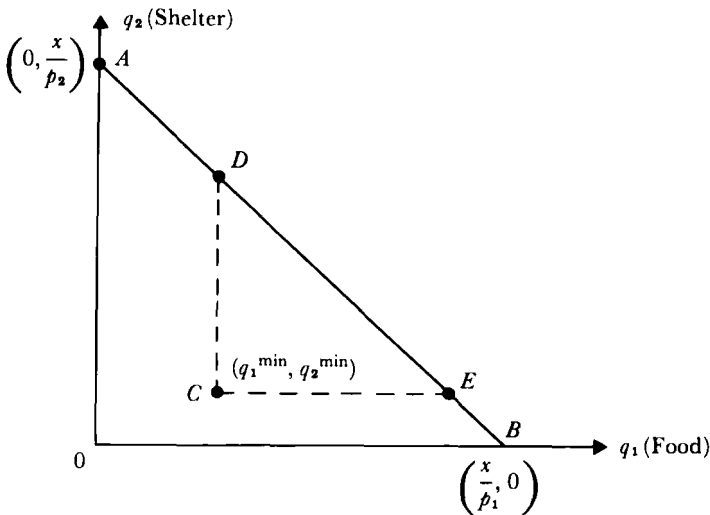


Figure 1.1. A linear budget constraint with a survival constraint.