

MERVIN L. KEEDY

Purdue University

MARVIN L. BITTINGER

Indiana University - Purdue University at Indianapolis

INTERMEDIATE ALGEBRA A MODERN APPROACH

SECOND EDITION



ADDISON-WESLEY PUBLISHING COMPANY

Reading, Massachusetts • Menlo Park, California Amsterdam • London • Don Mills, Ontario • Sydney

Third printing, May 1976

Copyright © 1975, 1971 by Addison-Wesley Publishing Company, Inc. Philippines copyright 1975, 1971 by Addison-Wesley Publishing Company, Inc.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise, without the prior written permission of the publisher. Printed in the United States of America. Published simultaneously in Canada. Library of Congress Catalog Card No. 74-10357.

ISBN 0-201-03729-7 EFGHIJK-MU-798

centimeter

Centimeters (cm); Γ millimeter = $\frac{1}{10}$

INTERMEDIATE ALGEBRA A MODERN APPROACH

SECOND EDITION

PREFACE TO SECOND EDITION

The users of the first edition have been so enthusiastic in their response and so helpful in offering constructive criticism, the authors first wish to say "thank you."

WHAT'S NEW IN THE SECOND EDITION?

Suggestions from Users. In various places errors have been corrected, changes in wording have been made, boldface type has been used, and exercises have been added, deleted, or changed. Chapter 2 in the first edition, which was rather long, has been divided into two chapters. There is also a new, more detailed index, and the headings of chapters, sections, exercise sets, and answers have been redesigned to make them easier to use.

The Metric System. To aid transition to the metric system, we have used metric units in approximately 50% of the applied problems. Students do not need to know what the metric units are in order to solve the problems, but if they wish they can take a "short course" on the metric system using the newly-added Appendix B: "The Metric System," and the familiarization material on the inside front cover.

SUGGESTIONS FOR USING THIS BOOK

In the preface to the first edition, it was pointed out that there are many ways in which this book can be used, and flexibility in that regard is one of the book's important features. The book has been very effective in lecture, math lab, and independent study situations.

Worth special mention is a teaching method developed by some users that works well in classes of all sizes, notably large ones. The instructor does not lecture, but makes assignments which students do on their own, including working exercise sets. The following class period the instructor spends answering questions. Students have an additional day or two to polish their homework before handing it in. In the meantime, they are working on the next assignment. This method has the advantage of providing individualization while at the same time keeping the class together and working as a group. It also minimizes the number of instructor man-hours required.

SUPPLEMENTS THAT ACCOMPANY THE SECOND EDITION

In order to further enhance flexibility in using this book, the following (optional) supplements are now available:

- Audio-Tape Cassettes are available for use in audio-tutorial or math lab situations.
- An Instructor's Manual contains commentary and a sample course syllabus.
- A Test Booklet contains five alternate forms of each chapter test and the final examination, with answers spaced for easy grading.
- An Answer Booklet contains the answers to all of the exercises.
- A Student's Solutions Booklet contains worked out solutions to all of the margin exercises.

ACKNOWLEDGEMENTS

The authors especially wish to thank Donald Evans, Betty Crawshaw, Dave Buckley, and Don Knorr of Polk Community College for their detailed and helpful suggestions for revision. Thanks also to Richard Spangler, Tacoma Community College; Matt Hassett and Paul Livermore, Arizona State University; Richard Thompson, Arizona University; Wilson Brumley, Colorado State University; Lucille Park, Pima Community College; Murphy Johnson, Arnie Stephensen, and Charles Little, Northern Arizona University; and Howard Beckwith, California State University, Long Beach, for their recommendations. In addition to Professor Hassett, Wayne McDaniel and Cynthia Siegal, University of Missouri, St. Louis; Carl Diekhans, Treasure Valley Community College; and Milton Legg, Moorhead State College, helped develop scripts for the audio-tape cassettes, for which we are grateful.

January 1975

PREFACE TO FIRST EDITION

The scope of this book is intermediate algebra. It is intended for use by students who have just finished a course in introductory algebra and also for students who have studied algebra at some earlier time but still need a course which starts "at the beginning," yet gets quickly into the topics of intermediate algebra. There is strong emphasis on the development of algebraic skills, but the "whys" of algebra also receive significant attention—more than is usual in developmental courses. The emphasis on understanding is what we feel makes this a modern book. We have not cluttered things with set notation and other distractions which many call modern, but do not really contribute to the student's skill or understanding. In this book as well as its companion volumes, the authors bring to bear not only their own experience in teaching remedial courses but also the suggestions and recommendations of instructors in scores of two-year colleges across the country.

One of the principal and distinguishing features of the book is its design and format. Each page has an outer margin, which is used for materials of several types. For each lesson the objectives are stated in behavioral terms at the top of the page. These can easily be seen by the student and they tell him clearly what is expected of him in terms of performance. We hope that this will help answer the question all-too-often heard, "What material are we responsible for?" The most important items in the margins, however, are the sample, or developmental, exercises. These are placed with the text development so that the student can become involved actively in the development of the topic and gain some practice on exercises of the type he will be expected to do as homework for the lesson. The text refers the student to these exercises in the margins at the appropriate places.

There are many ways in which this book can be used. Flexibility in this regard is indeed one of its important features. The instructor who wishes to use it as he would an ordinary textbook can do so very easily. All he need do is ignore, and have students ignore, the exercises in the margins. If an instructor wishes to use the lecture method primarily, but would like to bring some student-centered activity into the class, he can very easily do so. He would merely stop lecturing and have the students do the exercises in the margins at the appropriate times. On the other hand, the book is well suited for use in a learning laboratory situation. Because of its design, it can be used by a student with minimal instructor guidance. Yet it retains the flavor of the ordinary textbook, without the often deadly quality of the programmed text. This book contains some other features not usually found in a college textbook. There are tests at the ends of chapters, in addition to a final examination. Besides these, there is a pretest which can be used diagnostically, for placement. The exercise sheets which the student removes from the book are designed for quick and easy grading or scoring. The answers in the *Instructor's Manual* are arranged so that they match the spacing on the exercise sheets. The *Manual* also contains alternative forms of the chapter tests and the final examination. The book contains a great number of exercises (about 4000), and the authors have attempted to use language sparingly, so that the student has a maximal chance to learn the mathematics by reading it.

The material herein is suitable for a semester or quarter course for most students needing intermediate algebra in college. This is the third in a series of books written in the same style. The two which precede it are *Arithmetic: A Modern Approach* and *Introductory Algebra: A Modern Approach*.

The authors wish to thank the numerous people who helped make this book what it is. These include the many instructors in two-year colleges with whom they visited and who made many helpful suggestions. Professors Jerry Ball of Chabot College, Ralph Mansfield of Chicago City College, Loop Campus, and Mathew Graber of New York City Community College made many helpful suggestions for improving the manuscript, and the staff of the Addison-Wesley Publishing Company has prodded and encouraged us most appropriately. Last, but not least, we thank our wives for their patience and helpful encouragement.

January, 1971

M. L. K. M. L. B. The purpose of this test is to help identify weak points. When you have completed the test, read the test analysis on the answer page at the end of the book. The answers are given along with page numbers to indicate where you need to study. Remove the test from the book and begin.

ANSWERS

1.

3.

5.

6.

7.

Chapter 1

1. Simplify. |-28|

2. Evaluate $\frac{ab + ac}{bc}$ when a = -2, b = 3,

•

3. Remove parentheses and simplify.

$$-2[7x - 3(5 - 4x)] - 9x$$

4. Simplify. $\frac{42y^7x^6z^{-5}}{21y^8x^4z^2}$

c = -4.

Chapter 2

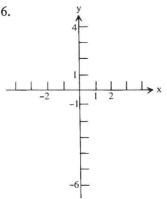
5. Solve. 3(x + 5) - 7x = 2(x - 4)

6. The sum of two consecutive odd integers is 40. What are the integers?

7. Solve $A = \pi(H - h)$, for H.

8. Find an equation of the line containing the point (-1, 3) and parallel to the line whose equation is 2x + 7y = 10.

9. Graph 4x - y = 6.



8.

9.

See graph.

ANSWERS

10.

See graph.

11.

12.

13.

()

14.

.....

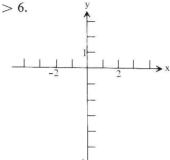
15.

16.

17.

Chapter 3

10. Graph 4x - y > 6.



11. Solve |x-1| > 2.

Chapter 4

Evaluate.

12.
$$\begin{vmatrix} 7 & 10 \\ 9 & 8 \end{vmatrix}$$

13.
$$\begin{vmatrix} 1 & 2 & 0 \\ 3 & -1 & -2 \\ 4 & -3 & -4 \end{vmatrix}$$

14. Solve
$$2x + 3y = 11$$

 $3x + 2y = 9$

15. Solve. x + y - z = -3 x + y + z = 1x - y + 2z = 7

16. Car A leaves a city traveling at a speed of 36 mph. Car B leaves the same city $\frac{1}{2}$ hr later traveling 48 mph in the same direction as Car A. How long does it take Car B to overtake Car A?

17. Rick Rapp weighs 150 lb and is sitting 9 ft from Gil Gruv on a see-saw. Gil weighs 120 lb. The see-saw is balanced. How far is each from the fulcrum?

NAME CLASS

ANSWERS

18.

19.

20.

21.

22.

23.

24.

25.

Chapter 5		
	- 4 - 5	
	anter 🤊	(n

$$4x^3 - 3x^2 - 5x - 1$$
 and $-4x^2 - x - 8$ $(a^3 + 5a^2 - ab) - (-ab^3 + 3a^3 + 4a^2 - a)$

Multiply.

20.
$$(7x + 5)(x - 4)$$

21.
$$(4a - b^3)^2$$

Factor.

22.
$$x^3 + 13x^2 + 12x$$

23.
$$8x^3 - 1$$

24.
$$a^2 - 2ab + b^2 - 16$$

$$a^2x + bx = a - b$$

26. Given a function described by
$$f(x) = x^2 - x$$
, find $f(2 - a)$.

Chapter 6

27. One mixture of saltwater is 20% salt. Another is 50% salt. How many gallons of each should be used to make 6 gallons of saltwater which is 40% salt?

27.

ANSWERS

28. The speed of a boat in still water is 12 mph. The boat trave¹ 3 miles upstream in the same time that it takes to travel 5 miles downstream. What is the speed of the stream?

28.

29.

29. Man A and Man B, working together, can complete a certain job in 2 hours. Man B can do the same job alone twice as fast as Man A can do the job working alone. How long would it take Man B to do the job alone?

30.

Perform the following operations and simplify.

30. $\frac{1}{v^2-v^2}$

30.
$$\frac{1}{x^2 - y^2} + \frac{1}{x + y} - \frac{1}{x - y}$$

31.
$$\frac{a^3+b^3}{5} \cdot \frac{5}{a+b}$$

31.

32.

32.
$$\frac{x^2 - 7x + 12}{x - 2} \div \frac{3x - 12}{x^2 - 4x + 4}$$

33.
$$\frac{\frac{1}{a^2} - \frac{1}{b^2}}{\frac{1}{a} - \frac{1}{b}}$$

33.

 $\frac{2}{x} + \frac{2}{x - 3} = 1$

35. Solve
$$R = \frac{v^2}{2c} + h$$
, for *c*.

NAME

CLASS

ANSWERS

34.

36. Use synthetic division to find the quotient and remainder.

$$(x^3-4x^2-5)\div(x+3)$$

35.

36.

Chapter 7

37. Divide. Write scientific notation for the answer.

$$\frac{2.21 \times 10^5}{6.5 \times 10^8}$$

38. Multiply and simplify.

$$\sqrt{5ab} \cdot \sqrt{10a^3}$$

39. Divide and simplify.

$$\frac{\sqrt[3]{a}}{\sqrt[3]{5b^2}}$$

38.

37.

39.

40. Rationalize the numerator.

$$\frac{\sqrt{5}-1}{3}$$

41. Write a single radical expression.

$$\frac{\sqrt{(a+b)^3}}{\sqrt[4]{(a+b)^5}}$$

40.

41.

47.

48.

ANSWERS	42. Solve.
	$\sqrt[4]{3y+7}=2$
42.	
43.	
	Chapter 8
	Solve.
	44. $8x^2 + 24 = 0$
44.	
45.	
	46. Write a quadratic equality solutions are $2\sqrt{5}$ and $-$
46.	

43. Multiply these complex numbers.

$$(5-2i)(4+3i)$$

45.
$$4x^2 = 20x - 23$$

- uation whose $-2\sqrt{5}$.
- **47.** Solve. $x 9\sqrt{x} + 20 = 0$

48. In a right triangle the length of one leg is 1 yd longer than the length of the other leg. The length of the hypotenuse is 29 yd. Find the lengths of the legs.

CONTENTS

		Pretest		3.4	Inequalities in Two Variables —Graphs on a Plane
Chapter	1	Real Numbers and Their Properties			Exercise Set 3.1
	1.1	Real Numbers and Algebra	3		Exercise Set 3.2
	1.2	Properties of Addition and Subtraction	7		Exercise Set 3.3
	1.3	Properties of Multiplication and Division.	11		Exercise Set 3.4
	1.4	The Distributive Laws and Their Use	. 16		Chapter 3 Test
	1.5	Multiplying by —1 and Simplifying	19	~	2.00
	1.6	Exponents	22	Chapter 4	Systems of Equations
	1.7	Order and Properties of Absolute Value	27	4.1	Systems of Equations
		Exercise Set 1.1	29		in Two Variables
		Exercise Set 1.2	31	4.2	Other Methods for Solving
		Exercise Set 1.3	33		Systems of Equations 129
		Exercise Set 1.4	35	4.3	Systems of Equations in
		Exercise Set 1.5	37		Three Variables
		Exercise Set 1.6	39	4.4	Using Second Order Determinants,
		Exercise Set 1.7	43	4.5	Cramer's Rule (Optional)
		Chapter 1 Test	45	4.5	Applied Problems
Chamban	2	Lincon Equations		4.6	Lever or Torque Problems (Optional)
Chapter	2	Linear Equations		4.7	Three-by-Three Determinants
	2.1	Solving Equations	49	3.7	(Optional)
	2.2	Applied Problems	56	4.8	Using Third Order Determinants,
	2.3	Formulas	59		Cramer's Rule (Optional)
	2.4	Graphs of Equations	60	4.9	Applied Problems
	2.5	Linear Equations	66		Exercise Set 4.1
	2.6	Slope	69 73		Exercise Set 4.2
	2.7 2.8	More Equations of Lines	76		Exercise Set 4.3
	2.0	Exercise Set 2.1	79		Exercise Set 4.4
		Exercise Set 2.2	83		Exercise Set 4.5
		Exercise Set 2.3	85		Exercise Set 4.6
		Exercise Set 2.4	87		Exercise Set 4.7
		Exercise Set 2.5	89		Exercise Set 4.8
		Exercise Set 2.6	91		Exercise Set 4.9
		Exercise Set 2.7	93		Chapter 4 Test
		Exercise Set 2.8	95	Chamton 5	Dolumentials and Eurotians
		Chapter 2 Test	97	Chapter 5	Polynomials and Functions
				5.1	Some Properties of Polynomials 181
Chapter	3	Inequalities		5.2	Calculations with Polynomials 185
Chapter				5.3	Multiplication of Polynomials 188
	3.1	Solving Inequalities;	101	5.4	Special Products of Polynomials 191
	2.2	the Addition Principle	101	5.5	Factoring
	3.2	Solving Inequalities;	106	5.6	Factoring Trinomials
	2 2	the Multiplication Principle	100	5.7 5.8	Completing the Square
	3.3	Equations and Inequalities with Absolute Value	108	3.0	of Two Cubes
		WITH AUSUILLE VALUE	100		01 1 wo Cubes

x Contents

5.9	Factoring: a General Strategy 205		Exercise Set 6.12	31
5.10	Solving Equations 206		Chapter 6 Test	313
5.11	Formulas		-	
5.12	Solving Equations by Factoring 209	Chapter 7	Exponents, Powers, and Roots	
5.13	Functions	7.1		244
5.14		7.1	Properties of Integer Exponents	
	Functions	7.2	Scientific Notation	
5.15	More About Functions	7.3	Radicals	322
	Exercise Set 5.1	7.4	Multiplying and Simplifying	
	Exercise Set 5.2		with Radicals	
	Exercise Set 5.3	7.5	Simplifying and Dividing with Radicals	329
	Exercise Set 5.4	7.6	Addition and Subtraction	
	Exercise Set 5.5		Involving Radicals	
	Exercise Set 5.6	7.7	More Multiplication Involving Radicals	333
	Exercise Set 5.7	7.8	Rationalizing Denominators	
	Exercise Set 5.8		or Numerators	334
	Exercise Set 5.9	7.9	Rational Numbers as Exponents	338
	Exercise Set 5.10	7.10	Solving Radical Equations	341
	Exercise Set 5.10	7.11	The Complex Numbers	344
	Exercise Set 5.12	7.12	More on the Complex Numbers	347
			Exercise Set 7.1	349
	Exercise Set 5.13		Exercise Set 7.2	351
	Exercise Set 5.14		Exercise Set 7.3	353
	Exercise Set 5.15		Exercise Set 7.4	355
	Chapter 5 Test		Exercise Set 7.5	359
			Exercise Set 7.6	361
Chapter 6	Fractional Expressions and Equations		Exercise Set 7.7	363
6.1	Multiplying and Simplifying		Exercise Set 7.8	365
	Fractional Expressions		Exercise Set 7.9	369
6.2	Division and Reciprocals		Exercise Set 7.10	371
6.3	Least Common Multiples		Exercise Set 7.11	
6.4	Addition		Exercise Set 7.12	
6.5	Subtraction		Chapter 7 Test	
6.6	Complex Fractional Expressions		-	
6.7	Division of Polynomials	Chapter 8	Quadratic Equations and Functions	
6.8	Synthetic Division	8.1	Quadratic Equations	381
6.9	Solving Fractional Equations	8.2	Fractional Equations	
6.10	Formulas	8.3	Completing the Square	
6.11	Applied Problems	8.4	The Quadratic Formula	
	Variation		More about the Solutions	305
0.12	Exercise Set 6.1	0.5	of a Quadratic Equation	307
	Exercise Set 6.1	8.6	Formulas	
	Exercise Set 6.3	8.7	Equations Quadratic in Form	
	Exercise Set 6.4		-	393
	Exercise Set 6.4	8.8	The Pythagorean Theorem and the Distance Formula	200
		9.0		
	Exercise Set 6.6	8.9	Quadratic Variation	
	Exercise Set 6.7	8.10	Graphs of Quadratic Functions	
	Exercise Set 6.8		Exercise Set 8.1	
	Exercise Set 6.9		Exercise Set 8.2	
	Exercise Set 6.10		Exercise Set 8.3	
	Exercise Set 6.11		Exercise Set 8.4	417

xi

47 48 48 ions 49
48 48 ions . 49 49
48 48 ions . 49 49
48 ions . 49 49
ions . 49 49
49
49
49
49
50
50
50
51
51
51
51
5.3
52
52
1- F.1
cals . 54
54
A-
A-
)

- 49. The stopping distance of a car after the brakes are applied varies directly as the square of the speed r. If a car traveling 60 mph can stop in 240 ft, how long will it take the same car to stop when it is traveling 90 mph?
- ANSWERS 49.
- **50.** A rocket is fired into the air. Its height h, in feet, t seconds after blastoff is given by $h = -16t^2 + 96t + 880.$

Find its maximum height and when it attains it.

50.

Chapter 9

51. Solve.

$$3x^2 + y^2 = 7$$

y - x = 1

52. The length of a rectangle is 1 ft greater than the width. The length of a diagonal is 29 ft. Find its dimensions.

52.

51.

53. Find the center and radius of the circle

 $x^2 + y^2 + 8x - 10y - 8 = 0$

54. Graph. $\frac{x^2}{9} - \frac{y^2}{25} = 1$.

53.

54.

See graph.