



K. T. Chau • Zheng Wang

# Chaos in Electric Drive Systems

**Analysis, Control  
and Application**

# CHAOS IN ELECTRIC DRIVE SYSTEMS

## ANALYSIS, CONTROL AND APPLICATION

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*To our parents, families, colleagues and friends worldwide*

# Preface

Chaos is a phenomenon that occurs in nature, from as large as the universe to as tiny as a particle. The concepts of chaology have penetrated into virtually all branches of science and engineering. In the field of electrical and electronic engineering, recent research has covered a wide spectrum, including the analysis of chaos, the stabilization of chaos, the stimulation of chaos, and the application of chaos.

There are many books that deal with the field of chaology, focusing on the theoretical analysis of chaotic systems and the mathematical formulation of chaotic behaviors. In recent years, some books have begun to deal with chaos in electronic engineering, especially in the areas of electronic circuits and telecommunications. Although chaos and its practical application in electric drive systems have been widely published as papers in learned journals, a book that comprehensively discusses chaos in electric drive systems is highly desirable.

The purpose of this book is to provide a comprehensive discussion on chaos in electric drive systems, including the analysis of their chaotic behaviors, the control of their chaotic characteristics, and the application of their chaotic features. Contrary to other books which usually involve intensive mathematics or idealized experiments, this book aims to use a minimum of mathematical treatments, extensive computer simulations, and realistic experimentations to discuss chaos in various electric drive systems, including DC drive systems, AC drive systems, and switched reluctance drive systems. Also, while other books consider that the relevant application of chaos or chaos theory is to model or simply explain some strange behaviors, this book aims to discuss and explore the realistic application of chaos in electric drive systems, especially the utilization of chaotic motion for compactors, mixers, washers, HVAC devices, and grinders.

While an electric drive can be chaoized by a simple parameter and stabilized by a feedback controller, my life is also chaoized by a naughty boy and stabilized by a wonder woman. I would therefore like to take this opportunity to express my heartfelt gratitude to my son, Aten Man-ho, and my wife, Joan Wai-yi, for their existence in my life.

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Since its first introduction by Poincaré in the 1890s, chaos has been discovered in many disciplines. Although it was previously identified as a scientific problem, chaos is being paid more and more attention by engineers today. As a person engaged in electrical engineering, I got to know chaos when I read a book about nonlinearity in power systems. My first impression was that chaos was interesting, but so complicated, and with increasing knowledge I began to realize that chaos was actually a “conservative” guy with a messy outlook but a beautiful intrinsic property.

I became familiar with chaos when I started my PhD study at The University of Hong Kong (HKU) in 2004. Encouraged by my supervisor, Professor K.T. Chau, I was connected closely with the area of chaos in electric drives. By that time, Professor Chau had already developed a lot of pioneering work on the identification, analysis, and stabilization of chaos in electric drives. As in other disciplines, the innovative idea of the positive utilization of chaos in electric drives had just started in Professor Chau’s group. My work then focused on chaotic drives, in particular on their industrial applications. When Professor Chau told me about his book proposal, I felt very happy as some of the creative work by our group on this topic could be introduced systematically worldwide. Most importantly, we hope that more people might pay attention to this multidisciplinary area, not only scientifically, but also in an engineering capacity. We also hope that more colleagues join us in this area!

Finally, I would like to take this opportunity to express my appreciation to Professor Chau for his guidance and for allowing me to participate in the writing of this book; to Professors Jie Wu and Ming Cheng for their support during my master’s degree and work at the Southeast University of China (SEU); and to my group fellows in HKU and SEU, whose work has greatly excited me. I also wish to acknowledge the genuine support and unselfish care I have received from my parents at all times.

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*Southeast University, China*

# Organization of this Book

This book is a happy marriage of two fields of research – chaology and electrical engineering. Chaology has always been tagged as an abstract field that involves intensive mathematics but lacks practical application. On the other hand, electrical engineering has been well recognized as a practical field that usually transforms innovative technology into commercial products, thus improving our living standards. Chaos in electric drive systems is a representative of this marriage, enabling chaos to exhibit realistic behavior and provide a practical application. It also fuels electrical engineering with a new breed of technology.

The book covers the multidisciplinary aspects of chaos and electric drive systems, and is written for a wide range of readers, including students, researchers, and engineers. It is organized into four parts:

- Part I presents an introduction to the book. It contains Chapters 1 and 2, which will provide an overview of chaos with an emphasis on electric drive systems. These chapters will also introduce the basic theory of chaos and a fundamental knowledge of electric drive systems.
- Part II is a core section of the book – namely, how to analyze chaos in various electric drive systems. It consists of Chapters 3, 4, and 5, which will discuss the analysis of chaos in DC drive systems, AC drive systems, and switched reluctance drive systems.
- Part III is another core section which explains how chaos in various electric drive systems can be controlled. It comprises two chapters, Chapters 6 and 7, which will discuss various methods of controlling chaos, including the stabilization and stimulation of chaos. It should be noted that this book adopts the general perception of the meaning of control, rather than use the jargon of chaos theory where ‘control’ and ‘anticontrol’ represent ‘stabilize’ and ‘destabilize’, respectively.
- Part IV – which is probably the most influential part of the book – unveils and proposes some promising applications of chaos for electric drive systems. It contains three chapters (Chapters 8–10) that will be devoted to describing various applications of chaos, including the application of chaos stabilization, the application of chaotic modulation, and the application of chaotic motion.

Since these four parts have their individual themes, readers have the flexibility to select and read those parts that they find most interesting. The suggestions for reading are as follows:

- Undergraduate students taking a course dedicated to electric drive systems may be particularly interested in Parts I, II, and IV.
- Postgraduate students taking a course dedicated to advanced electric drive systems may find all parts interesting.
- Researchers in the areas of chaos and/or electric drive systems may also be interested in all parts. In particular, they may have special interest in Parts III and IV, which involve newly explored research topics.

- Practicing engineers for product design and development may be more interested in Parts I and IV, in which new ideas can be triggered by the overview, and commercial products can be derived from the proposed applications.
- General readers may be interested in all parts. They are advised to read the book from beginning to end, page by page, and will find the book to be most enjoyable.

The book contains 10 chapters, each of which has various sections and subsections. In order to facilitate a reading selection, an outline of each chapter is given below:

- Chapter 1 gives an overview of chaos, including the definition of chaos, the development of chaology, and the research of chaos in the field of electrical engineering, with an emphasis on electric drive systems.
- Chapter 2 introduces the necessary background knowledge for this book – namely, a description of the basic theory of chaos and the fundamentals of electric drive systems.
- Chapter 3 is devoted to analyzing chaos in DC drive systems, including both of the voltage-controlled mode and the current-controlled mode. The corresponding modeling, analysis, simulation, and experimentation will be discussed.
- Chapter 4 is devoted to analyzing chaos in AC drive systems, including the induction drive system, the permanent magnet synchronous drive system, and the synchronous reluctance drive system. The corresponding modeling, analysis, simulation, and experimentation will be discussed.
- Chapter 5 is devoted to analyzing chaos in switched reluctance drive systems, including the voltage-controlled mode and the current-controlled mode. Relevant discussion with verification will be given.
- Chapter 6 describes various control approaches to stabilize the chaos that occurs in both DC and AC drive systems. A relevant discussion with verification will be given.
- Chapter 7 describes various control approaches to stimulate chaos operating at various electric drive systems. Both of the control-oriented chaos and the design-oriented chaos will be discussed.
- Chapter 8 presents the stabilization of chaos in various applications, including automotive wiper systems, centrifugal governor systems, and rate gyro systems. The corresponding modeling, analysis, and stabilization will be elaborated.
- Chapter 9 presents how to apply chaotic modulation to PWM inverter drive systems, hence reducing the corresponding audible noise and mechanical vibration. Open-loop and closed-loop control will both be discussed.
- Chapter 10 presents a new breed of chaos application, namely the electrically-chaotized motion – simply known as chaotic motion. Various promising applications of chaotic motion, including compaction, mixing, washing, HVAC, and grinding, will be unveiled and elaborated.

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The material presented in this book is a collection of many years of research and development by the authors in the Department of Electrical and Electronic Engineering, The University of Hong Kong.

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We are deeply indebted to our colleagues and friends worldwide for their continuous support and encouragement over the years. We appreciate the reviewers of this book for their thoughtful and constructive comments, and thank the editors at John Wiley & Sons for their patience and effective support.

Last but not least, we thank our families for their unconditional support and absolute understanding during the writing of this book.

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# Contents

<b>Preface</b>	<b>xi</b>
<b>Organization of this Book</b>	<b>xiii</b>
<b>Acknowledgments</b>	<b>xv</b>
<b>About the Authors</b>	<b>xvii</b>
 <b>PART I INTRODUCTION</b>	
<b>1 Overview of Chaos</b>	<b>3</b>
1.1 What is Chaos?	3
1.2 Development of Chaology	4
1.3 Chaos in Electrical Engineering	8
1.3.1 Chaos in Electronic Circuits	9
1.3.2 Chaos in Telecommunications	10
1.3.3 Chaos in Power Electronics	11
1.3.4 Chaos in Power Systems	12
1.3.5 Chaos in Electric Drive Systems	13
References	16
 <b>2 Introduction to Chaos Theory and Electric Drive Systems</b>	 <b>23</b>
2.1 Basic Chaos Theory	23
2.1.1 Basic Principles	23
2.1.2 Criteria for Chaos	28
2.1.3 Bifurcations and Routes to Chaos	29
2.1.4 Analysis Methods	37
2.2 Fundamentals of Electric Drive Systems	45
2.2.1 General Considerations	45
2.2.2 DC Drive Systems	50
2.2.3 Induction Drive Systems	56
2.2.4 Synchronous Drive Systems	61
2.2.5 Doubly Salient Drive Systems	68
References	77

## PART II ANALYSIS OF CHAOS IN ELECTRIC DRIVE SYSTEMS

<b>3</b>	<b>Chaos in DC Drive Systems</b>	<b>81</b>
3.1	Voltage-Controlled DC Drive System	81
3.1.1	Modeling	81
3.1.2	Analysis	83
3.1.3	Simulation	87
3.1.4	Experimentation	94
3.2	Current-Controlled DC Drive System	96
3.2.1	Modeling	96
3.2.2	Analysis	98
3.2.3	Simulation	102
3.2.4	Experimentation	108
	References	110
<b>4</b>	<b>Chaos in AC Drive Systems</b>	<b>113</b>
4.1	Induction Drive Systems	113
4.1.1	Modeling	113
4.1.2	Analysis	116
4.1.3	Simulation	117
4.1.4	Experimentation	118
4.2	Permanent Magnet Synchronous Drive Systems	119
4.2.1	Modeling	120
4.2.2	Analysis	122
4.2.3	Simulation	125
4.2.4	Experimentation	127
4.3	Synchronous Reluctance Drive Systems	129
4.3.1	Modeling	130
4.3.2	Analysis	133
4.3.3	Simulation	136
4.3.4	Experimentation	139
	References	143
<b>5</b>	<b>Chaos in Switched Reluctance Drive Systems</b>	<b>145</b>
5.1	Voltage-Controlled Switched Reluctance Drive System	146
5.1.1	Modeling	146
5.1.2	Analysis	149
5.1.3	Simulation	151
5.1.4	Experimentation	153
5.2	Current-Controlled Switched Reluctance Drive System	155
5.2.1	Modeling	155
5.2.2	Analysis	157
5.2.3	Simulation	159
5.2.4	Phenomena	163
	References	166

**PART III CONTROL OF CHAOS IN ELECTRIC DRIVE SYSTEMS**

<b>6 Stabilization of Chaos in Electric Drive Systems</b>	<b>171</b>
6.1 Stabilization of Chaos in DC Drive System	171
6.1.1 Modeling	171
6.1.2 Analysis	175
6.1.3 Simulation	178
6.1.4 Experimentation	179
6.2 Stabilization of Chaos in AC Drive System	181
6.2.1 Nonlinear Feedback Control	182
6.2.2 Backstepping Control	183
6.2.3 Dynamic Surface Control	186
6.2.4 Sliding Mode Control	189
References	192
<b>7 Stimulation of Chaos in Electric Drive Systems</b>	<b>193</b>
7.1 Control-Oriented Chaoization	193
7.1.1 Time-Delay Feedback Control of PMDC Drive System	193
7.1.2 Time-Delay Feedback Control of PM Synchronous Drive System	199
7.1.3 Proportional Time-Delay Control of PMDC Drive System	201
7.1.4 Chaotic Signal Reference Control of PMDC Drive System	204
7.2 Design-Oriented Chaoization	207
7.2.1 Doubly Salient PM Drive System	209
7.2.2 Shaded-Pole Induction Drive System	219
References	231

**PART IV APPLICATION OF CHAOS IN ELECTRIC DRIVE SYSTEMS**

<b>8 Application of Chaos Stabilization</b>	<b>235</b>
8.1 Chaos Stabilization in Automotive Wiper Systems	235
8.1.1 Modeling	236
8.1.2 Analysis	238
8.1.3 Stabilization	240
8.2 Chaos Stabilization in Centrifugal Governor Systems	246
8.2.1 Modeling	247
8.2.2 Analysis	248
8.2.3 Stabilization	248
8.3 Chaos Stabilization in Rate Gyro Systems	250
8.3.1 Modeling	251
8.3.2 Analysis	253
8.3.3 Stabilization	253
References	255
<b>9 Application of Chaotic Modulation</b>	<b>257</b>
9.1 Overview of PWM Schemes	257
9.1.1 Voltage-Controlled PWM Schemes	257
9.1.2 Current-Controlled PWM Schemes	260
9.2 Noise and Vibration	261

9.3	Chaotic PWM	263
9.3.1	Chaotic Sinusoidal PWM	265
9.3.2	Chaotic Space Vector PWM	269
9.4	Chaotic PWM Inverter Drive Systems	271
9.4.1	Open-Loop Control Operation	272
9.4.2	Closed-Loop Vector Control Operation	273
	References	280
<b>10</b>	<b>Application of Chaotic Motion</b>	<b>283</b>
10.1	Chaotic Compaction	283
10.1.1	Compactor System	285
10.1.2	Chaotic Compaction Control	286
10.1.3	Compaction Simulation	287
10.1.4	Compaction Experimentation	290
10.2	Chaotic Mixing	292
10.2.1	Mixer System	293
10.2.2	Chaotic Mixing Control	294
10.2.3	Chaotic Mixing Simulation	295
10.2.4	Chaotic Mixing Experimentation	298
10.3	Chaotic Washing	301
10.3.1	Chaotic Clothes-Washer	302
10.3.2	Chaotic Dishwasher	304
10.4	Chaotic HVAC	306
10.5	Chaotic Grinding	309
	References	312
	<b>Index</b>	<b>315</b>

# **Part One**

## **Introduction**



# 1

## Overview of Chaos

This chapter gives an overview of chaos, including the definition of chaos, the development of chaology, and the research of chaos. In particular, the research and development of chaos in the field of electrical engineering – with an emphasis on electric drive systems – are discussed in detail.

### 1.1 What is Chaos?

The etymology of the word “chaos” is a Greek word “ $\chi\alpha\omicron\varsigma$ ” (Nagashima and Baba, 1999) which means “the nether abyss, or infinite darkness,” and was personified as “the most ancient of the gods.” Namely, the god Chaos was the foundation of all creation. From this god arose Gaea (god of the earth), Tartarus (god of the underworld) and Eros (the god of love). Eros drew Chaos and Gaea together so that they could produce descendants, the first born of whom was Uranus (the god of the sky). This also resulted in the creation of the elder gods known as Titans. The interaction of these gods resulted in the creation of other gods, including such well-known figures as Aphrodite, Hades, Poseidon, and Zeus.

There is a Chinese myth of chaos (Liu, 1998), taken from one of the ancient Chinese classics *Chuang-Tzu*: “The god of the Southern Sea was called *Shu* (Change), the god of the Northern Sea was called *Hu* (Suddenness), and the god of the Central was called *Hun-tun* (Chaos). *Shu* and *Hu* often came together for a meeting in the Central, and *Hun-tun* treated them generously. *Shu* and *Hu* determined to repay his kindness, and said, ‘Mankind has seven holes for seeing, hearing, eating and breathing; but *Hun-tun* has none of them; let us bore the holes for him!’ So, every day they bored one hole in his head. On the seventh day, *Hun-tun* died.” This myth not only indicates the disorder-like or random-like behavior of chaos, but also implies that chaos is the natural state of the world and should not be disrupted by a sudden change.

There are many myths relating to the god of chaos in different cradles of civilization, such as Greece, China, Egypt, and India, but in the modern world chaos is no longer a god. In 1997, its meaning in the *Oxford English Dictionary Online* was updated as “Behavior of a system which is governed by deterministic laws but is so unpredictable as to appear random, owing to its extreme sensitivity to changes in parameters or its dependence on a large number of independent variables; a state characterized by such behavior” (Simpson, 2004).

The general perception on chaos is equivalent to disorder or even random. It should be noted that chaos is not exactly disordered, and its random-like behavior is governed by a rule – mathematically,