



STATISTICS

PRINCIPLES AND METHODS

Fourth Edition

Richard A. Johnson / Gouri K. Bhattacharyya

Statistics

Principles and Methods

FOURTH EDITION

Richard A. Johnson
Gouri K. Bhattacharyya
University of Wisconsin at Madison



John Wiley & Sons, Inc.
New York • Chichester • Weinheim • Brisbane • Toronto • Singapore

ACQUISITION EDITOR
MARKETING MANAGER
PRODUCTION SERVICES MANAGER
SENIOR DESIGNER
ILLUSTRATION EDITOR
PHOTO EDITOR
PRODUCTION MANAGEMENT SERVICES
COVER DESIGN
COVER PHOTO

Debbie Berridge
Julie Z. Lindstrom
Jeanine Furino
Karin Gerdes Kincheloe
Sigmund Malinowski
Jill Tatara
Ingrao Associates
David Levy
Art Wolfe/Tony Stone Images

This book was set in Berling by Progressive Information Technologies and printed and bound by Quebecor USA. The cover was printed by Phoenix Color Corp.

This book is printed on acid-free paper. (∞)

Photo Credits **Chapter 1:** Opener: ©1993 Chromosohm/John Sohm/Photo Researchers. Page 5: Andrew Sacks/Tony Stone Images. Page 6: Mitch Wojnarowicz/The Image Works/**Chapter 2:** Opener: Superstock, Inc. Page 33: Britt Erlanson/The Image Bank. Page 72: ©Datamation/**Chapter 3:** Opener: NASA/Science Photo Library/Photo Researchers/**Chapter 4:** Opener: ©Mark Reinstein/FPG International. Page 136: Calvin and Hobbes ©1990 Universal Press Syndicate. Reprinted with permission. All rights reserved/**Chapter 5:** Opener: ©John Terence Turner/FPG International. Page 210: Superstock, Inc. Page 218: ©Stephen Frisch/Stock Boston. Page 235: Reprinted by permission of United Features Syndicate, Inc. ©1968/**Chapter 6:** Page 283: ©Planet Earth Pictures/FPG International/**Chapter 7:** Opener: ©Bob Daemmrich/PNI/**Chapter 8:** Opener: ©Ron Chapple/FPG International/**Chapter 9:** Opener: ©David R. Frazier/Photo Researchers/**Chapter 10:** Opener: Richard Johnson. Page 443: Elizabeth Crews/Stock Boston/**Chapter 11:** Opener: ©Fred McConnaughey/Photo Researchers. Page 478: By permission of Johnny Hart and Field Enterprises, Inc./**Chapter 12:** Opener: ©David Hall/Photo Researchers/**Chapter 13:** Opener: Richard Johnson/**Chapter 14:** Opener: ©Gary D. Landsman/The Stock Market/**Chapter 15:** Opener: ©Peter Beck/The Stock Market.

Copyright © 2001 John Wiley & Sons, Inc.

All rights reserved.

No part of this publication may be reproduced, stored in a retrieval system or transmitted in any form or by any means, electronic, mechanical, photocopying, recording, scanning, or otherwise, except as permitted under Section 107 or 108 of the 1976 United States Copyright Act, without either the prior written permission of the Publisher or authorization through payment of the appropriate per-copy fee to the Copyright Clearance Center, 222 Rosewood Drive, Danvers, MA 01923, (978) 750-8400, fax (978) 750-4470. Requests to the Publisher for permission should be addressed to the Permissions Department, John Wiley & Sons, Inc., 605 Third Avenue, New York, NY 10158-0012, (212) 850-6011, fax (212) 850-6008, E-Mail: PERMREQ@WILEY.COM. To order books please call 1(800)-225-5945.

Library of Congress Cataloging-in-Publication Data

Johnson, Richard Arnold.

Statistics: principles and methods / Richard A. Johnson, Gouri K. Bhattacharyya. —4th ed.

p. cm

Includes bibliographical references and index.

ISBN 0-471-38897-1 (cloth: alk. paper)

1. Statistics. I. Bhattacharyya, Gouri K, 1940- II. Title.

QA276.12.J38 2000

519.5—dc21

00-039274

Printed in the United States of America

10 9 8 7 6 5 4 3 2

WILEY SERIES IN PROBABILITY AND STATISTICS

ESTABLISHED BY WALTER A. SHEWHART AND SAMUEL S. WILKS

Editors

Vic Barnett, Noel A. C. Cressie, Nicholas I. Fisher, Iain M. Johnstone, J. B. Kadane, David G. Kendall, David W. Scott, Bernard W. Silverman, Adrian F. M. Smith, Jozef L. Teugels, Ralph A. Bradley, Emeritus, J. Stuart Hunter, Emeritus

Probability and Statistics Section

*ANDERSON • The Statistical Analysis of Time Series
ARNOLD, BALAKRISHNAN, and NAGARAJA • A First Course in Order Statistics
ARNOLD, BALAKRISHNAN, and NAGARAJA • Records
BACCELLI, COHEN, OLSDER, and QUADRAT • Synchronization and Linearity: An Algebra for Discrete Event Systems
BARNETT • Comparative Statistical Inference, *Third Edition*
BASILEVSKY • Statistical Factor Analysis and Related Methods: Theory and Applications
BERNARDO and SMITH • Bayesian Statistical Concepts and Theory
BILLINGSLEY • Convergence of Probability Measures, *Second Edition*
BOROVKOV • Asymptotic Methods in Queuing Theory
BOROVKOV • Ergodicity and Stability of Stochastic Processes
BRANDT, FRANKEN, and LISEK • Stationary Stochastic Models
CAINES • Linear Stochastic Systems
CAIROLI and DALANG • Sequential Stochastic Optimization
CONSTANTINE • Combinatorial Theory and Statistical Design
COOK • Regression Graphics
COVER and THOMAS • Elements of Information Theory
GSÖRGÖ and HORVÁTH • Weighted Approximations in Probability Statistics
GSÖRGÖ and HORVÁTH • Limit Theorems in Change Point Analysis
*DANIEL • Fitting Equations to Data: Computer Analysis of Multifactor Data, *Second Edition*
DETTE and STUDDEN • The Theory of Canonical Moments with Applications in Statistics, Probability, and Analysis
DEY and MUKERJEE • Fractional Factorial Plans
*DOOB • Stochastic Processes
DRYDEN and MARDIA • Statistical Shape Analysis
DUPUIS and ELLIS • A Weak Convergence Approach to the Theory of Large Deviations
ETHIER and KURTZ • Markov Processes: Characterization and Convergence
FELLER • An Introduction to Probability Theory and Its Applications, Volume 1, *Third Edition*, Revised; Volume II, *Second Edition*
FULLER • Introduction to Statistical Time Series, *Second Edition*
FULLER • Measurement Error Models
GHOSH, MUKHOPADHYAY, and SEN • Sequential Estimation
GIFI • Nonlinear Multivariate Analysis
GUTTORP • Statistical Inference for Branching Processes
HALL • Introduction to the Theory of Coverage Processes
HAMPEL • Robust Statistics: The Approach Based on Influence Functions
HANNAN and DEISTLER • The Statistical Theory of Linear Systems
HUBER • Robust Statistics
HUSKOVA, BERAN, and DUPAC • Collected Works of Jaroslav Hajek—with Commentary
IMAN and CONOVER • A Modern Approach to Statistics
JUREK and MASON • Operator-Limit Distributions in Probability Theory
KASS and VOS • Geometrical Foundations of Asymptotic Inference
KAUFMAN and ROUSSEEUW • Finding Groups in Data: An Introduction to Cluster Analysis
KELLY • Probability, Statistics, and Optimization
KENDALL, BARDEN, CARNE, and LE • Shape and Shape Theory
LINDVALL • Lectures on the Coupling Method
McFADDEN • Management of Data in Clinical Trials
MANTON, WOODBURY, and TOLLEY • Statistical Applications Using Fuzzy Sets
MORGENTHAUER and TUKEY • Configural Polysampling: A Route to Practical Robustness
MUIRHEAD • Aspects of Multivariate Statistical Theory
OLIVER and SMITH • Influence Diagrams, Belief Nets and Decision Analysis
*PARZEN • Modern Probability Theory and Its Applications
PRESS • Bayesian Statistics: Principles, Models, and Applications
PUKELSHEIM • Optimal Experimental Design
RAO • Asymptotic Theory of Statistical Inference
RAO • Linear Statistical Inference and Its Applications, *Second Edition*
RAO and SHANBHAG • Choquet-Deny Type Functional Equations with Applications to Stochastic Models

* Now available in a lower priced paperback edition in the Wiley Classics Library.

ROBERTSON, WRIGHT, and DYKSTRA • Order Restricted Statistical Inference
 ROGERS and WILLIAMS • Diffusions, Markov Processes, and Martingales, Volume I: Foundations, *Second Edition*; Volume II: Itô Calculus
 RUBINSTEIN and SHAPIRO • Discrete Event Systems: Sensitivity Analysis and Stochastic Optimization by the Score Function Method
 RUZSA and SZEKELY • Algebraic Probability Theory
 SCHEFFE • The Analysis of Variance
 SEBER • Linear Regression Analysis
 SEBER • Multivariate Observations
 SEBER and WILD • Nonlinear Regression
 SERFLING • Approximation Theorems of Mathematical Statistics
 SHORACK and WELLNER • Empirical Processes with Applications to Statistics
 SMALL and McLEISH • Hilbert Space Methods in Probability and Statistical Inference
 STAPLETON • Linear Statistical Models
 STAUDTE and SHEATHER • Robust Estimation and Testing
 STOYANOV • Counterexamples in Probability
 TANAKA • Time Series Analysis: Nonstationary and Noninvertible Distribution Theory
 THOMPSON and SEBER • Adaptive Sampling
 WELSH • Aspects of Statistical Inference
 WHITTAKER • Graphical Models in Applied Multivariate Statistics
 YANG • The Construction Theory of Denumerable Markov Processes

Applied Probability and Statistics Section

ABRAHAM and LEDOLTER • Statistical Methods for Forecasting
 AGRESTI • Analysis of Ordinal Categorical Data
 AGRESTI • Categorical Data Analysis
 ANDERSON, AUQUIER, HAUCK, OAKES, VANDAELE, and WEISBERG • Statistical Methods for Comparative Studies
 ARMITAGE and DAVID (editors) • Advances in Biometry
 *ARTHANARI and DODGE • Mathematical Programming in Statistics
 ASMUSSEN • Applied Probability and Queues
 *BAILEY • The Elements of Stochastic Processes with Applications to the Natural Sciences
 BARNETT and LEWIS • Outliers in Statistical Data, *Third Edition*
 BARTHOLOMEW, FORBES, and McLEAN • Statistical Techniques for Manpower Planning, *Second Edition*
 BASU and RIGDON • Statistical Methods for the Reliability of Repairable Systems
 BATES and WATTS • Nonlinear Regression Analysis and Its Applications
 BECHHOFFER, SANTNER, and GOLDSMAN • Design and Analysis of Experiments for Statistical Selection, Screening, and Multiple Comparisons
 BELSLEY • Conditioning Diagnostics: Collinearity and Weak Data in Regression
 BELSLEY, KUH, and WELSCH • Regression Diagnostics: Identifying Influential Data and Sources of Collinearity
 BHAT • Elements of Applied Stochastic Processes, *Second Edition*
 BHATTACHARYA and WAYMIRE • Stochastic Processes with Applications
 BIRKES and DODGE • Alternative Methods of Regression
 BLISCHKE and MURTHY • Reliability: Modeling, Prediction, and Optimization
 BLOOMFIELD • Fourier Analysis of Time Series: An Introduction, *Second Edition*
 BOLLEN • Structural Equations with Latent Variables
 BOULEAU • Numerical Methods for Stochastic Processes
 BOX • Bayesian Inference in Statistical Analysis
 BOX and DRAPER • Empirical Model-Building and Response Surfaces
 *BOX and DRAPER • Evolutionary Operation: A Statistical Method for Process Improvement
 BUCKLEW • Large Deviation Techniques in Decision, Simulation, and Estimation
 BUNKE and BUNKE • Nonlinear Regression, Functional Relations and Robust Methods: Statistical Methods of Model Building
 CHATTERJEE and HADI • Sensitivity Analysis in Linear Regression
 CHERNICK • Bootstrap Methods: A Practitioner's Guide
 CHILÈS and DELFINER • Geostatistics: Modeling Spatial Uncertainty
 CHOW and LIU • Design and Analysis of Clinical Trials: Concepts and Methodologies
 CLARKE and DISNEY • Probability and Random Processes: A First Course with Applications, *Second Edition*
 *COCHRAN and COX • Experimental Designs, *Second Edition*
 CONOVER • Practical Nonparametric Statistics, *Second Edition*
 CORNELL • Experiments with Mixtures, Designs, Models, and the Analysis of Mixture Data, *Second Edition*
 *COX • Planning of Experiments
 CRESSIE • Statistics for Spatial Data, *Revised Edition*
 DANIEL • Applications of Statistics to Industrial Experimentation
 DANIEL • Biostatistics: A Foundation for Analysis in the Health Sciences, *Sixth Edition*
 DAVID • Order Statistics, *Second Edition*

* Now available in a lower priced paperback edition in the Wiley Classics Library.

Preface

THE NATURE OF THE BOOK

Statistics—the subject of data analysis and data-based reasoning—is playing an increasingly vital role in virtually all professions. Some familiarity with this subject is now an essential component of any college education. Yet, pressures to accommodate a growing list of academic requirements often necessitate that this exposure be brief. Keeping these conditions in mind, we have written this book to provide students with a first exposure to the powerful ideas of modern statistics. It presents the key statistical concepts and the most commonly applied methods of statistical analysis. Moreover, to keep it accessible to freshmen and sophomores from a wide range of disciplines, we have avoided mathematical derivations. They usually pose a stumbling block to learning the essentials in a short period of time.

This book is intended for students who do not have a strong background in mathematics but seek to learn the basic ideas of statistics and their application in a variety of practical settings. The core material of this book is common to almost all first courses in statistics and is designed to be covered well within a one-semester course in introductory statistics for freshmen–seniors. It is supplemented with some additional special-topics chapters.

ORIENTATION

The topics treated in this text are, by and large, the ones typically covered in an introductory statistics course. They span three major areas: (i) descriptive statistics, which deals with summarization and description of data; (ii) ideas of probability and an understanding of the manner in which sample-to-sample variation influences our conclusions; and (iii) a collection of statistical methods for analyzing the types of data that are of common occurrence. However, it is the treatment of these topics that makes the text distinctive. By means of good motivation, sound explanations, and an abundance of illustrations given in a real-world context, it emphasizes more than just a superficial understanding.

Each concept or technique is motivated by first setting out its goal and indicating its scope by an illustration of its application. The subsequent discussion is not only limited to showing how a method works but includes an explanation of the why. Even without recourse to mathematics, we are able to make the reader aware of possible pitfalls in the statistical analysis. Students can gain a proper appreciation of statistics only when they are provided with a careful explanation of the underlying logic. Without this understanding, a learning of elementary statistics is bound to be rote and transient.

When describing the various methods of statistical analysis, the reader is continually reminded that the validity of a statistical inference is contingent upon certain model assumptions. Misleading conclusions may result when these assumptions are violated. We feel that the teaching of statistics, even at an introductory level, should not be limited to the prescription of methods. Students should be encouraged to develop a critical attitude in applying the methods and to be cautious when interpreting the results. This attitude is especially important in the study of relationship among variables, which is perhaps the most widely used (and also abused) area of statistics. In addition to discussing inference procedures in this context, we have particularly stressed critical examination of the model assumptions and careful interpretation of the conclusions.

SPECIAL FEATURES

1. Crucial elements are boxed to highlight important concepts and methods. These boxes provide an ongoing summary of the important items essential for learning statistics. At the end of each chapter, all of its **key ideas and formulas** are summarized.
2. A rich collection of examples and exercises is included. These are drawn from a large variety of **real-life settings**. In fact, many data sets stem from genuine experiments, surveys, or reports.
3. Exercises are provided at the end of **each major section**. These provide the reader with the opportunity to practice the ideas just learned. Occasionally, they supplement some points raised in the text. A larger collection of exercises appears at the **end of a chapter**. The starred problems are relatively difficult and suited to the more mathematically competent student.
4. **Statistics in Context** sections, in four of the beginning chapters, each describe an important statistical application where a statistical approach to understanding variation is vital. These extended examples reveal, early on in the course, the value of understanding the subject of statistics.
5. ***P*-values** are emphasized in examples concerning tests of hypotheses. Graphs giving the relevant normal or *t*-density curve, rejection region, and *P*-value are presented.

6. **Regression analysis** is a primary statistical technique so we provide a more thorough coverage of the topic than is usual at this level. The basics of regression are introduced in Chapter 11, whereas Chapter 12 stretches the discussion to several issues of practical importance. These include methods of **model checking**, handling nonlinear relations, and multiple regression analysis. Complex formulas and calculations are judiciously replaced by computer output so the main ideas can be learned and appreciated with a minimum of stress.
7. **Computer Aided Statistical Analyses** use software packages that can remove much of the drudgery of hand calculation and plotting. They allow students to work with larger data sets where patterns are more pronounced and make complicated calculations. Besides discussion of some computer output in the text, computer exercises are included in all chapters where relevant.
8. **Convenient Electronic Data Bank** at the end of the book contains a substantial collection of data. These data sets, together with numerous others throughout the book, allow for considerable flexibility in the choice between concept-orientated and applications-orientated exercises. The Data Bank and the other larger data sets are available on floppy disk.
9. **Technical Appendix A** presents a few statistical facts of a mathematical nature. These are separated from the main text so that they can be left out if the instructor so desires.

ABOUT THIS FOURTH EDITION

The fourth edition of *STATISTICS—Principles and Methods* maintains the objectives and level of presentation of the earlier editions. The goals are the developing (i) of an understanding of the reasonings by which findings from sample data can be extended to general conclusions and (ii) a familiarity with some basic statistical methods. There are numerous data sets and computer outputs which give an appreciation of the role of the computer in modern data analysis.

Throughout, we have endeavored to give clear and concise explanations of the concepts and important statistical terminology and methods. Discussion of the statistical methods includes an explanation of their underlying assumptions and the dangers of ignoring them. Real-life settings are used to motivate the statistical ideas and well organized discussions proceed to cover statistical methods with heavy emphasis on examples. The fourth edition enhances these special features. More particularly, the major improvements are:

More Emphasis on Understanding Data. We have expanded the first chapter by including an extended discussion of population and sample with more examples to tie to student experiences. New material on using a random digit table to select a sample enables students to appreciate the importance of properly selecting a sample from a population.

New exercises are abundant. Nearly a third of the exercises are new or modified. All exercises are now numbered sequentially within a chapter. For instance, 8.73 refers to the 73rd problem in Chapter 8.

Titles are added to each example to clarify their purpose and emphasize the main point.

New figures show P -values and rejection regions for hypotheses testing examples that involve the normal or student's t distribution.

New statistics in context sections, or small case studies, give students an early exposure to the power of statistical tools. Chapter 2 contains an application of statistics in the context of quality monitoring. This example provides strong motivation for learning more about the subject of statistics.

Another section, in Chapter 7, concerns a problem a flower importer faces because of a fluctuating exchange rate. We show how to obtain a model for changes in the U.S.–Canadian exchange rate.

More Data Based Exercises. Some of the new exercises are keyed to the new data based examples given an extended discussion. The Data Bank now includes a data set on wolves and one on malt extraction which are connected to new exercises. As with all the data sets in the Data Bank, many additional techniques can be applied beyond those specifically detailed in any exercise. Overall, there are a large number of new or updated exercises.

ORGANIZATION

This book is organized into fifteen chapters, an optional technical appendix (Appendix A), and a collection of tables (Appendix B). Although designed for a one-semester or a two-quarter course, it is enriched with ample additional material to allow the instructor some choices of topics. Beyond Chapter 1, which sets the theme of statistics, and distinguishes population and sample, the subject matter could be classified as follows:

Topic	Chapter
Descriptive study of data	2, 3
Probability and distributions	4, 5, 6
Sampling variability	7
Core ideas and methods of statistical inference	8, 9, 10
Special topics of statistical inference	11, 12, 13, 14, 15

We regard Chapters 1 to 10 as constituting the core material of an introductory statistics course, with the exception of the starred sections in Chapter 6.

Although this material is just about enough for a one-semester course, many instructors may wish to eliminate some sections in order to cover the basics of regression analysis in Chapter 11. This is most conveniently done by initially skipping Chapter 3 and then taking up only those portions that are linked to Chapter 11. Also, instead of a thorough coverage of probability that is provided in Chapter 4, the later sections of that chapter may receive a lighter coverage.

ACKNOWLEDGMENTS

We thank Minitab (State College, Pa.) and the SAS Institute (Cary, N.C.) for permission to include commands and output from their software packages. A special thanks to K. T. Wu and Kam Tsui for many helpful suggestions and comments. We also thank all those who have contributed the data sets which enrich the presentation and all those who reviewed this and previous editions. The help of Erik Johnson, Li-fei Huang, and Wenqing Lu, with this edition, is greatly acknowledged.

Richard A. Johnson
Gouri K. Bhattacharyya

*DEGROOT, FIENBERG, and KADANE • Statistics and the Law
 DODGE • Alternative Methods of Regression
 DOWDY and WEARDEN • Statistics for Research, *Second Edition*
 DUNN and CLARK • Applied Statistics: Analysis of Variance and Regression, *Second Edition*
 *ELANDT-JOHNSON and JOHNSON • Survival Models and Data Analysis
 EVANS, PEACOCK, and HASTINGS • Statistical Distributions, *Second Edition*
 *FLEISS • The Design and Analysis of Clinical Experiments
 FLEISS • Statistical Methods for Rates and Proportions, *Second Edition*
 FLEMING and HARRINGTON • Counting Processes and Survival Analysis
 GALLANT • Nonlinear Statistical Models
 GLASSERMAN and YAO • Monotone Structure in Discrete-Event Systems
 GNANADESIKAN • Methods for Statistical Data Analysis of Multivariate Observations, *Second Edition*
 GOLDSTEIN and LEWIS • Assessment: Problems, Development, and Statistical Issues
 GREENWOOD and NIKULIN • A Guide to Chi-Squared Testing
 *HAHN • Statistical Models in Engineering
 HAHN and MEEKER • Statistical Intervals: A Guide for Practitioners
 HAND • Construction and Assessment of Classification Rules
 HAND • Discrimination and Classification
 HEIBERGER • Computation for the Analysis of Designed Experiments
 HEDAYAT and SINHA • Design and Inference in Finite Population Sampling
 HINKELMAN and KEMPTHORNE • Design and Analysis of Experiments, Volume I: Introduction to Experimental Design
 HOAGLIN, MOSTELLER, and TUKEY • Exploratory Approach to Analysis of Variance
 HOAGLIN, MOSTELLER, and TUKEY • Exploring Data Tables, Trends and Shapes
 HOAGLIN, MOSTELLER, and TUKEY • Understanding Robust and Exploratory Data Analysis
 HOCHBERG and TAMHANE • Multiple Comparison Procedures
 HOCKING • Methods and Applications of Linear Models: Regression and the Analysis of Variables
 HOGG and KLUGMAN • Loss Distributions
 HOSMER and LEMESHOW • Applied Logistic Regression
 HØYLAND and RAUSAND • System Reliability Theory: Models and Statistical Methods
 HUBERTY • Applied Discriminant Analysis
 JACKSON • A User's Guide to Principle Components
 JOHN • Statistical Methods in Engineering and Quality Assurance
 JOHNSON • Multivariate Statistical Simulation
 JOHNSON and KOTZ • Distributions in Statistics
 Continuous Multivariate Distributions
 JOHNSON, KOTZ, and BALAKRISHNAN • Continuous Univariate Distributions, Volume 1, *Second Edition*
 JOHNSON, KOTZ, and BALAKRISHNAN • Continuous Univariate Distributions, Volume 2, *Second Edition*
 JOHNSON, KOTZ, and BALAKRISHNAN • Discrete Multivariate Distributions
 JOHNSON, KOTZ, and KEMP • Univariate Discrete Distributions, *Second Edition*
 JUREČKOVÁ and SEN • Robust Statistical Procedures: Asymptotics and Interrelations
 KADANE • Bayesian Methods and Ethics in a Clinical Trial Design
 KADANE and SCHUM • A Probabilistic Analysis of the Sacco and Vanzetti Evidence
 KALBFLEISCH and PRENTICE • The Statistical Analysis of Failure Time Data
 KELLY • Reversability and Stochastic Networks
 KHURI, MATHEW, and SINHA • Statistical Tests for Mixed Linear Models
 KLUGMAN, PANJER, and WILLMOT • Loss Models: From Data to Decisions
 KLUGMAN, PANJER, and WILLMOT • Solutions Manual to Accompany Loss Models: From Data to Decisions
 KOVALENKO, KUZNETZOV, and PEGG • Mathematical Theory of Reliability of Time-Dependent Systems with Practical Applications
 LACHIN • Biostatistical Methods: The Assessment of Relative Risks
 LAD • Operational Subjective Statistical Methods: A Mathematical, Philosophical, and Historical Introduction
 LANGE, RYAN, BILLARD, BRILLINGER, CONQUEST, and GREENHOUSE • Case Studies in Biometry
 LAWLESS • Statistical Models and Methods for Lifetime Data
 LEE • Statistical Methods for Survival Data Analysis, *Second Edition*
 LEPAGE and BILLARD • Exploring the Limits of Bootstrap
 LINHART and ZUCCHINI • Model Selection
 LITTLE and RUBIN • Statistical Analysis with Missing Data
 LLOYD • The Statistical Analysis of Categorical Data
 MAGNUS and NEUDECKER • Matrix Differential Calculus with Applications in Statistics and Econometrics, *Revised Edition*
 MALLER and ZHOU • Survival Analysis with Long Term Survivors
 MANN, SCHAFFER, and SINGPURWALLA • Methods for Statistical Analysis of Reliability and Life Data
 McLACHLAN and KRISHNAN • The EM Algorithm and Extensions
 McLACHLAN • Discriminant Analysis and Statistical Pattern Recognition
 McNEIL • Epidemiological Research Methods

* Now available in a lower priced paperback edition in the Wiley Classics Library.

Applied Probability and Statistics (Continued)

MEEKER and ESCOBAR • Statistical Methods for Reliability Data
*MILLER • Survival Analysis, *Second Edition*
MONTGOMERY and PECK • Introduction to Linear Regression Analysis, *Second Edition*
MYERS and MONTGOMERY • Response Surface Methodology: Process and Product in Optimization Using Designed Experiments
NELSON • Accelerated Testing, Statistical Models, Test Plans, and Data Analyses
NELSON • Applied Life Data Analysis
OCHI • Applied Probability and Stochastic Processes in Engineering and Physical Sciences
OKABE, BOOTS, and SUGIHARA • Spatial Tesselations: Concepts and Applications of Voronoi Diagrams
PANKRATZ • Forecasting with Dynamic Regression Models
PANKRATZ • Forecasting with Univariate Box-Jenkins Models: Concepts and Cases
PIANTADOSI • Clinical Trials: A Methodologic Perspective
PORT • Theoretical Probability for Applications
PUTERMAN • Markov Decision Processes: Discrete Stochastic Dynamic Programming
RACHEV • Probability Metrics and the Stability of Stochastic Models
RÉNYI • A Diary on Information Theory
RIPLEY • Spatial Statistics
RIPLEY • Stochastic Simulation
ROLSKI, SCHMIDLI, SCHMIDT, and TEUGELS • Stochastic Processes for Insurance and Finance
ROUSSEEUW and LEROY • Robust Regression and Outlier Detection
RUBIN • Multiple Imputation for Nonresponse in Surveys
RUBINSTEIN • Simulation and the Monte Carlo Method
RUBINSTEIN and MELAMED • Modern Simulation and Modeling
RYAN • Statistical Methods for Quality Improvement, *Second Edition*
SCHUSS • Theory and Applications of Stochastic Differential Equations
SCOTT • Multivariate Density Estimation: Theory, Practice, and Visualization
*SEARLE • Linear Models
SEARLE • Linear Models for Unbalanced Data
SEARLE, CASELLA, and McCULLOCH • Variance Components
SENNOTT • Stochastic Dynamic Programming and the Control of Queueing Systems
STOYAN, KENDALL, and MECKE • Stochastic Geometry and Its Applications, *Second Edition*
STOYAN and STOYAN • Fractals, Random Shapes and Point Fields: Methods of Geometrical Statistics
THOMPSON • Empirical Model Building
THOMPSON • Sampling
THOMPSON • Simulation: A Modeler's Approach
TIJMS • Stochastic Modeling and Analysis: A Computational Approach
TIJMS • Stochastic Models: An Algorithmic Approach
TITTERINGTON, SMITH, and MAKOV • Statistical Analysis of Finite Mixture Distributions
UPTON and FINGLETON • Spatial Data Analysis by Example, Volume I: Point Pattern and Quantitative Data
UPTON and FINGLETON • Spatial Data Analysis by Example, Volume II: Categorical and Directional Data
VAN RIJCKEVORSEL and DE LEEUW • Component and Correspondence Analysis
VIDAKOVIC • Statistical Modeling by Wavelets
WEISBERG • Applied Linear Regression, *Second Edition*
WESTFALL and YOUNG • Resampling-Based Multiple Testing: Examples and Methods for p -Value Adjustment
WHITTLE • Systems in Stochastic Equilibrium
WOODING • Planning Pharmaceutical Clinical Trials: Basic Statistical Principles
WOOLSON • Statistical Methods for the Analysis of Biomedical Data
*ZELLNER • An Introduction to Bayesian Inference in Econometrics

Texts and References Section

AGRESTI • An Introduction to Categorical Data Analysis
ANDERSON • An Introduction to Multivariate Statistical Analysis, *Second Edition*
ANDERSON and LOYNES • The Teaching of Practical Statistics
ARMITAGE and COLTON • Encyclopedia of Biostatistics: Volumes 1 to 6 with Index
BARTOSZYNSKI and NIEWIADOMSKA-BUGAJ • Probability and Statistical Inference
BENDAT and PIERSON • Random Data: Analysis and Measurement Procedures, *Third Edition*
BERRY, CHALONER, and GEWEKE • Bayesian Analysis in Statistics and Econometrics: Essays in Honor of Arnold Zellner
BHATTACHARYA and JOHNSON • Statistical Concepts and Methods
BILLINGSLEY • Probability and Measure, *Second Edition*
BOX • R. A. Fisher, the Life of a Scientist
BOX, HUNTER, and HUNTER • Statistics for Experimenters: An Introduction to Design, Data Analysis, and Model Building

* Now available in a lower priced paperback edition in the Wiley Classics Library.

Contents

1 INTRODUCTION 1

- 1 What Is Statistics? 3
- 2 Statistics in Our Everyday Life 3
- 3 Statistics in Aid of Scientific Inquiry 5
- 4 Two Basic Concepts—Population and Sample 8
- 5 The Purposeful Collection of Data 14
- 6 Statistics in Context 15
- 7 Objectives of Statistics 17
- 8 Review Exercises 18

2 ORGANIZATION AND DESCRIPTION OF DATA 23

- 1 Introduction 25
- 2 Main Types of Data 25
- 3 Describing Data by Tables and Graphs 26
- 4 Measures of Center 45
- 5 Measures of Variation 55
- 6 Checking the Stability of the Observations over Time 67
- 7 More on Graphics 71
- 8 Statistics in Context 73
- 9 Review Exercises 77

3 DESCRIPTIVE STUDY OF BIVARIATE DATA 89

- 1 Introduction 91
- 2 Summarization of Bivariate Categorical Data 91
- 3 A Designed Experiment for Making a Comparison 98
- 4 Scatter Diagram of Bivariate Measurement Data 100
- 5 The Correlation Coefficient—A Measure of Linear Relation 103
- 6 Prediction of One Variable from Another (Linear Regression) 116
- 7 Review Exercises 121

4 PROBABILITY 129

- 1 Introduction 131
- 2 Probability of an Event 132
- 3 Methods of Assigning Probability 139
- 4 Event Relations and Two Laws of Probability 147
- 5 Conditional Probability and Independence 159
- 6 Random Sampling from a Finite Population 173
- 7 Review Exercises 182

5 PROBABILITY DISTRIBUTIONS 191

- 1 Introduction 193
- 2 Random Variables 193
- 3 Probability Distribution of a Discrete Random Variable 197
- 4 Expectation (Mean) and Standard Deviation of a Probability Distribution 207
- 5 Successes and Failures—Bernoulli Trials 217
- 6 The Binomial Distribution 223
- 7 The Binomial Distribution in Context 235
- 8 Review Exercises 239

6 THE NORMAL DISTRIBUTION 249

- 1 Probability Model for a Continuous Random Variable 251
- 2 The Normal Distribution—Its General Features 258
- 3 The Standard Normal Distribution 261
- 4 Probability Calculations with Normal Distributions 268
- 5 The Normal Approximation to the Binomial 273
- *6 Checking the Plausibility of a Normal Model 279
- *7 Transforming Observations to Attain Near Normality 282
- 8 Review Exercises 286

7 VARIATION IN REPEATED SAMPLES — SAMPLING DISTRIBUTIONS 291

- 1 Introduction 293
- 2 The Sampling Distribution of a Statistic 294
- 3 Distribution of the Sample Mean and the Central Limit Theorem 301
- 4 Statistics in Context 313
- 5 Review Exercises 317

8 DRAWING INFERENCES FROM LARGE SAMPLES 321

- 1 Introduction 323
- 2 Point Estimation of a Population Mean 325
- 3 Confidence Interval for a Population Mean 331
- 4 Testing Hypotheses about a Population Mean 341
- 5 Inferences about a Population Proportion 356
- 6 Review Exercises 369

9 SMALL-SAMPLE INFERENCES FOR NORMAL POPULATIONS 377

- 1 Introduction 379
- 2 Student's t Distribution 379
- 3 Inferences about μ —Small Sample Size 384
- 4 Relationship between Tests and Confidence Intervals 394
- 5 Inferences About the Standard Deviation σ
(The Chi-Square Distribution) 397
- 6 Robustness of Inference Procedures 403
- 7 Review Exercises 406

10 COMPARING TWO TREATMENTS 411

- 1 Introduction 413
- 2 Independent Random Samples from Two Populations 417
- 3 Randomization and Its Role in Inference 439
- 4 Matched Pair Comparisons 441
- 5 Choosing Between Independent Samples and a Matched Pair Sample 453
- 6 Comparing Two Population Proportions 454
- 7 Review Exercises 466

11 REGRESSION ANALYSIS—I (Simple Linear Regression) 475

- 1 Introduction 477
- 2 Regression with a Single Predictor 479
- 3 A Straight-Line Regression Model 482
- 4 The Method of Least Squares 484

- 5 The Sampling Variability of the Least Squares Estimators—
Tools for Inference 492
- 6 Important Inference Problems 494
- 7 The Strength of a Linear Relation 508
- 8 Remarks About the Straight Line Model Assumptions 512
- 9 Review Exercises 515

12 REGRESSION ANALYSIS—II **521**

Multiple Linear Regression and Other Topics

- 1 Introduction 523
- 2 Nonlinear Relations and Linearizing Transformations 523
- 3 Multiple Linear Regression 529
- 4 Residual Plots to Check the Adequacy of a Statistical
Model 540
- 5 Review Exercises 544

13 ANALYSIS OF CATEGORICAL DATA **549**

- 1 Introduction 551
- 2 Pearson's χ^2 Test for Goodness of Fit 554
- 3 Contingency Table with One Margin Fixed
(Test of Homogeneity) 559
- 4 Contingency Table with Neither Margin Fixed
(Test of Independence) 570
- 5 Review Exercises 579

14 ANALYSIS OF VARIANCE (ANOVA) **585**

- 1 Introduction 587
- 2 Comparison of Several Treatments—The Completely
Randomized Design 587
- 3 Population Model and Inferences for a Completely Randomized
Design 596
- 4 Simultaneous Confidence Intervals 600
- 5 Graphical Diagnostics and Displays to Supplement
ANOVA 604
- 6 Randomized Block Experiments for Comparing
 k Treatments 606
- 7 Review Exercises 616

15	NONPARAMETRIC INFERENCE	623
	1 Introduction 625	
	2 The Wilcoxon Rank-Sum Test for Comparing Two Treatments 625	
	3 Matched Pair Comparisons 637	
	4 Measure of Correlation Based on Ranks 647	
	5 Concluding Remarks 651	
	6 Review Exercises 652	
APPENDIX A1	SUMMATION NOTATION	655
APPENDIX A2	RULES FOR COUNTING	660
APPENDIX A3	EXPECTATION AND STANDARD DEVIATION—PROPERTIES	663
APPENDIX A4	THE EXPECTED VALUE AND STANDARD DEVIATION OF \bar{X}	668
APPENDIX B	TABLES	670
	Table 1 Random Digits 670	
	Table 2 Cumulative Binomial Probabilities 673	
	Table 3 Standard Normal Probabilities 680	
	Table 4 Percentage Points of t Distributions 682	
	Table 5 Percentage Points of χ^2 Distributions 683	
	Table 6 Percentage Points of $F(\nu_1, \nu_2)$ Distributions 684	
	Table 7 Selected Tail Probabilities for the Null Distribution of Wilcoxon's Rank-Sum Statistic 686	
	Table 8 Selected Tail Probabilities for the Null Distribution of Wilcoxon's Signed-Rank Statistic 691	
DATA BANK		693
ANSWERS TO SELECTED ODD-NUMBERED EXERCISES		706
INDEX		720