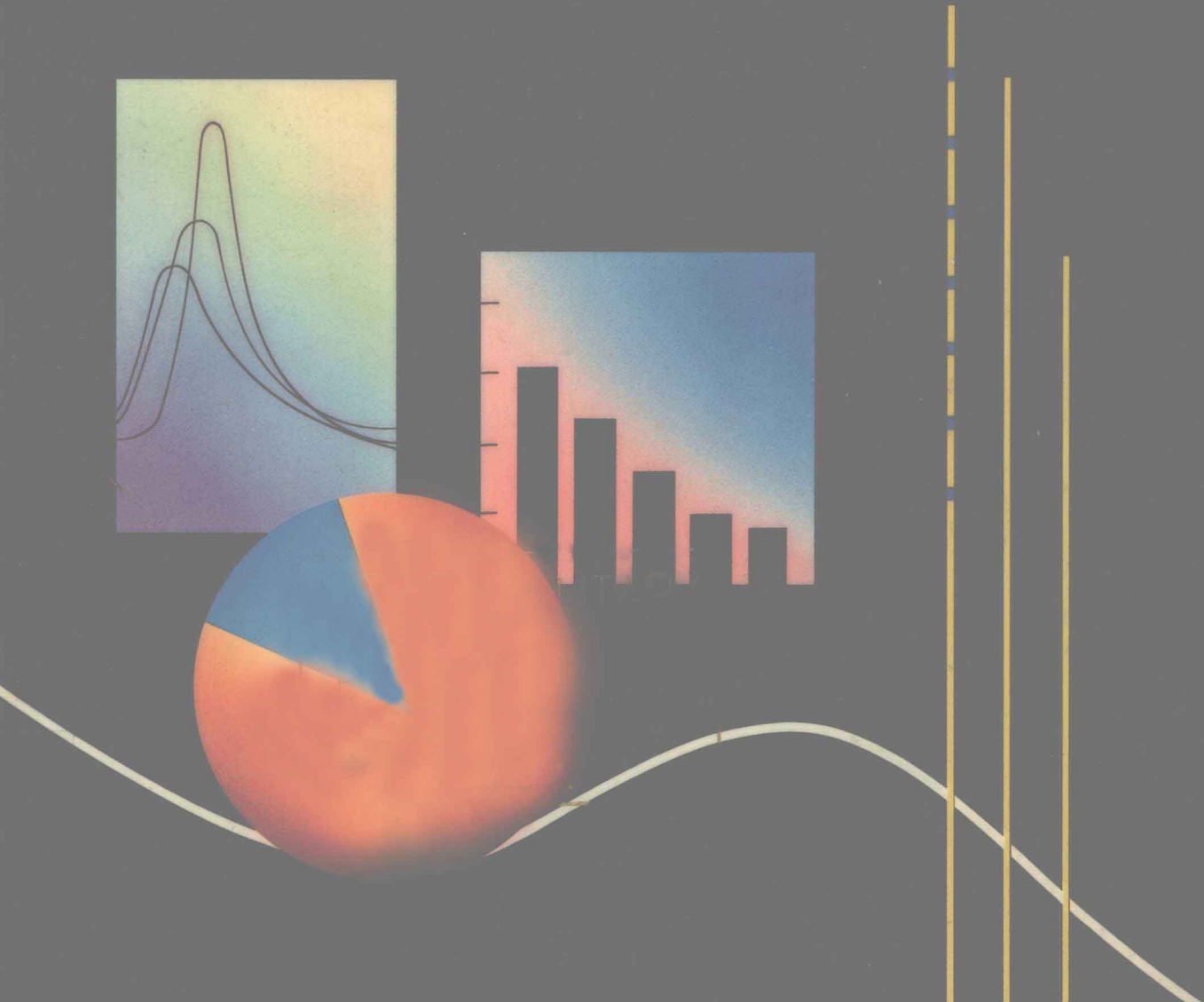
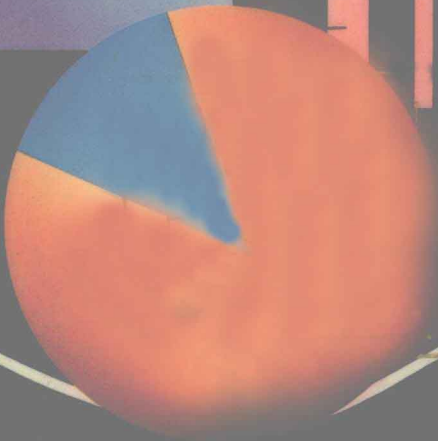
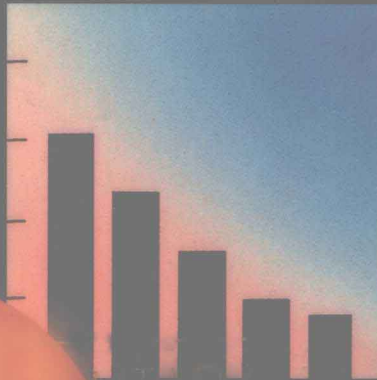
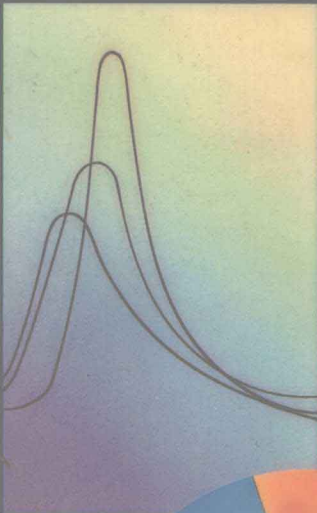


THIRD EDITION

# STATISTICS

A N I N T R O D U C T I O N

MASON LIND MARCHAL



**THIRD EDITION**  
**STATISTICS**  
**A N I N T R O D U C T I O N**  
**MASON LIND MARCHAL**

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*To Anita, Jane, and Andrea*

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## Preface

*Statistics: An Introduction*, Third Edition, is intended for use in an applied introductory statistics course. As in the previous editions, the principles of both descriptive and inferential statistics are discussed and illustrated in situations that are close to most students' own experience. Students with a background limited to basic algebra will be able to complete most of the necessary mathematical calculations.

This book is appropriate for use in any survey course in statistics. The material is organized so that it provides the greatest possible flexibility of use. Illustrations and exercises are drawn from disciplines as varied as sociology, education, business, sports, demography, meteorology, politics, and mathematics. Considerable latitude has been built into the organization of chapter topics so that the text can be adapted for use in a one-semester or one-quarter course or a two-quarter course. A one-semester course, for example, might include Chapters 1–10, 13, and 14. Time permitting, Chapters 11 and 16 would be logical additions.

• • • • •

## SPECIAL FEATURES

*Statistics: An Introduction*, Third Edition, has a number of special features that will motivate and assist students as they progress through the material:

- Each chapter begins with a set of *learning objectives*—what the student should be able to do upon completion of the chapter. These objectives act as advance organizers and motivators.
- At the beginning of each chapter, the important concepts that were presented in the preceding chapter are reviewed in a brief *introduction* that explains how these earlier concepts are linked to the present chapter. Then, a chapter overview introduces the new chapter's topics.
- The discussion of each concept is followed by a realistic *problem and solution*.

- Throughout the chapter are interspersed a number of *Self-Reviews*, each one closely patterned after the chapter problems that precede it. The Self-Reviews help students monitor their progress, and they provide students with constant reinforcement. Answers and methods of solution for Self-Reviews are given at the end of the chapter.
- Many interesting, real-world *Exercises* are incorporated within and at the end of each chapter. Answers and methods of solution for all even-numbered exercises are given at the back of the book.
- Every important *new term and formula* is defined and has been placed in a box for easy reference.
- Each chapter includes a *Summary*.
- End-of-chapter *Achievement Tests* help students evaluate their comprehension of the material covered. Answers and methods of solution are given at the back of the book.
- A *Unit Review* is included after each of six major groups of chapters. Each includes a brief review, key concepts, key terms, key symbols, review problems, and a section called “Using Statistics,” in which a situation is presented for which statistics can provide a solution, followed by a discussion of the situation and its resolution.
- Each chapter contains an interesting, challenging *Case*.
- A *Glossary* is included at the back of the book.
- The normal distribution and Student’s  $t$  distribution are printed on the front and back endpapers for easy reference.
- Simple *flowcharts* are presented throughout the textbook to help students choose the appropriate formula or test statistic.

The Third Edition also includes

- a large number of new chapter exercises;
- extensive use of statistical software in problem solving, especially in the multiple correlation and regression chapters;
- blue computer shapes next to selected exercises to indicate that statistical software is strongly recommended to solve these problems. Black computer shapes indicate that the use of statistical software is recommended, but not absolutely necessary;
- the concept of the  $p$ -value introduced in hypothesis testing;
- “drill” problems, scattered through the chapters, that allow the student to concentrate on the basic calculations;
- in Chapters 4 and 6, Chebyshev’s Theorem for interpreting the standard deviation;
- in the Multiple Regression chapter, emphasis on the interpretation of computer software output, which includes a global test to determine the significance of a set of regression coefficients. This chapter also includes a test of significance for individual regression coefficients.

## . . . . . **ANCILLARY MATERIALS**

A complete ancillary package accompanies the Third Edition.

The comprehensive *Study Guide* is organized much like the textbook. Each chapter includes objectives, problems and solutions, exercises, a summary, and assignments on perforated pages that can be removed and graded by the instructor. Ample space is provided for computations.

An *Instructor's/Solutions Manual* contains the solutions to all chapter exercises, Unit Review exercises, and Cases in the textbook and to the assignments in the Study Guide. In addition, it includes lecture materials and in-class lecture problems (plus solutions to these problems), prepared in a larger typeface so that they can easily be used as transparency masters.

An *EasyStat Guide* is available for the Third Edition. This guide, prepared by Toni M. Somers of Wayne State University, is a user-friendly program for any IBM-PC system. *EasyStat* is a computer program that works within the framework of a spreadsheet and includes a data set for 1,000 urban families, from which students can select random samples for carrying out exercises.

An all-new *Testbook* is available, organized by chapter with each chapter containing true-false, multiple choice, problem, and essay questions. The questions in a chapter may be used as a test over the entire chapter, selected questions may be chosen and given in class as a "pop" quiz, the entire chapter test may be assigned to be completed outside of class, or questions from several chapters may be combined to form a unit test, a midterm, or a final examination. The answers to the questions appear at the end of each chapter of the Testbook. The Testbook is also available computerized, in IBM, Macintosh, and Apple II formats.

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**ROBERT D. MASON**  
**DOUGLAS A. LIND**  
**WILLIAM G. MARCHAL**



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