

Practical Business Math Procedures

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BRIEF SEVENTH EDITION



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PRACTICAL BUSINESS MATH PROCEDURES

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PREVIEW OF SPECIAL FEATURES

Before looking at how to succeed in each chapter, let's look at some special features.

- 1. The toll-free, 24-hour hotline. This toll-free number for students allows you to call anytime and get extra help on any of the 22 summary practice tests located at the end of each chapter. As the author, I have recorded messages on how you should solve each problem. Think of this hotline as a pre-exam tune-up. The toll-free number is 1-800-338-9708.
- **2. Group activity: Personal Finance, a Kiplinger Approach.** In each chapter you can debate a business math issue I raise based on a *Kiplinger's Personal Finance* magazine article that is presented. This is great for critical thinking, as well as improving your writing skills.
- **3.** *The Wall Street Journal* newspaper. This newspaper insert helps explain how to read *The Wall Street Journal*, as well as show how business math relates to it. The newspaper is page-referenced to the text and is helpful for those who have never followed stocks, bonds, and mutual funds.
- **4.** Business Math Handbook and Study Guide. This reference guide contains all the tables found in the text. It makes homework, exams, etc. easier to deal with than flipping back and forth through the text. The Handbook also features a built-in study guide that provides self-paced worksheets that review each chapter's vocabulary, theory, and math applications. A set of 10 extra word problems for each chapter is included. Also included is a calculator reference guide with advice on how to use different calculators.
- **5. Blueprint aid boxes.** For the first eight chapters (not in Chapter 4), blueprint aid boxes are available to help you map out a plan to solve a word problem.
- **6.** The Business Math Tutorial. This software is a tutorial that guides you through the entire text. It is highly visual and user friendly.

Excel

- 7. Spreadsheet templates. Excel® templates are available for selected end-of-chapter problems. You can run these templates as is or enter your own data. The templates also include an interest table feature that enables you to input any percentage rate and any terms. The program will then generate table values for you.
- **8.** Business Math Internet Resource Guide. This Guide lists websites covering topics from each chapter, as well as descriptions of what you can expect to find at each site. It is referenced on the Scrapbook page in the text and includes group projects you can work on using the exciting possibilities of the Web.



- **9. New DVD-ROM.** The DVD packaged with the text includes practice quizzes, business math tutorial software links to websites listed in the Business Math Internet Resource Guide, the Excel® templates, PowerPoint, videocases, and videos—which feature tutorials by Jeff Slater of all Learning Unit Practice Quizzes.
- 10. The Slater Business Math website. Visit the site at www.mhhe.com/slater7e and find the Internet Resource Guide with hot links, tutorials, practice quizzes, and other materials useful for the course.

HOW TO READ AND USE THE BOOK

The colors in this text have a purpose. You should read the description below, then look at several pages to see how it works.

Blue: Movement, cancellations, steps to solve, arrows, blueprints

Gold: Formulas and steps

Green: Tables and forms

Red: Key items we are solving for

CHAPTERS

Each chapter is broken down into learning units. Each learning unit covers a key concept or a small group of concepts.

LEARNING OBJECTIVES

At the beginning of each chapter you'll find a list of learning objectives. Each is page referenced.

PRACTICE QUIZZES



At the end of each learning unit is a practice quiz, followed by solutions. These provide you with immediate feedback on your understanding of the unit. These are all solved on the DVD. Check with your instructor for availability.

CHAPTER ORGANIZER

At the end of each chapter is a quick reference guide called the Chapter Organizer. Key points, formulas, and examples are provided. A list of vocabulary terms is also included. All have page references. (A complete glossary is found at the end of the text.) Think of the chapter organizer as your set of notes.

CRITICAL THINKING DISCUSSION QUESTIONS

Factual, as well as thought-provoking, questions appear after the chapter organizer.

PROBLEMS

At the end of each chapter is a complete set of drill and word problems. Check figures for the odd-numbered problems are located in Appendix B.

CHALLENGE PROBLEMS



The last two word problems in each chapter let you "stretch" your business math skills. These are harder and require more effort.

ADDITIONAL HOMEWORK ASSIGNMENTS BY LEARNING UNIT

At the end of the text in Appendix A is a complete set of drill and word problems arranged by learning unit. These can be used for additional reinforcement. Your instructor may ask you to turn these in. Check figures for the odd-numbered problems are shown in Appendix B. On the inside back cover of the book is a table showing page references for each assignment.

SUMMARY PRACTICE TEST



This is a test before the test. All questions are page referenced back to the topic so you can check your methods. The test is a combination of drill and word problems. Check figures for *all* practice tests are in Appendix B. Remember: There is a toll-free hotline to review these tests at 1-800-338-9708.

BUSINESS MATH SCRAPBOOK

At the end of each chapter you will find actual clippings from *The Wall Street Journal* and various other publications. These articles will give you a chance to use the theory provided in the chapter to apply to the real world. It allows you to put your math skills to work.

CUMULATIVE REVIEWS

At the end of Chapters 3 and 8 are word problems that test your retention of business math concepts and procedures. Check figures for *all* cumulative review problems are in Appendix B.

VIDEO CASES ON DVD



There are three video cases applying business math concepts to real companies such as American President Lines, Washburn Guitars, and Online Banking. Video clips are included on the student DVD. Some background case information and assignment problems incorporating information on the companies are included at the end of Chapters 6, 9, and 11 (pages 161, 240, and 277).

Jeffrey Slater

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COMPANY/APPLICATION(S)

H. J. Heinz-Whole numbers

McDonald's Corp.—General problem solving, Sweatshops, Financial reports, Product liability

Southwest Airlines—Reading, Writing, Whole numbers

United Airlines—Reading, Writing, Whole numbers

American Airlines—Reading, Writing, Whole numbers

Delta—Reading, Writing, Whole numbers, Percent decrease and increase, Pay scales

US Airways—Reading, Writing, Whole numbers

Tootsie Roll Industries—Dissecting word problems

Continental Airlines—Adding and subtracting whole numbers

Ford—Subtracting whole numbers

Hershey—Dissecting word problems

Subway—Whole numbers

M&M Mars—Fractions

Wal-Mart—Types of fractions, Discounts AltaVista—Addition and subtraction of fractions

AMC Theatres—Addition and subtraction of fractions

Lowes Theatres—Addition and subtraction of fractions

Regal Cinemas—Addition and subtraction of fractions

Showcase Cinemas—Addition and subtraction of fractions

United Artists Theatres—Addition and subtraction of fractions

United Air—Adding and subtracting decimals

Carmines, New York—Subtracting decimals

Heaven on Seven, Chicago—Subtracting decimals

Grill 23, Boston — Subtracting decimals Docks, New York—Subtracting decimals

E*Trade—Rounding, Web trading commissions

Ipswich Bank—Banking

Bank One—Trends in banking

Wells Fargo—*Trends in banking* Citigroup—*Trends in banking*

First Union—Trends in banking

Washington Mutual—Trends in banking

Chase—Trends in banking

Fleet Bank—Trends in banking

Visa USA—Banking

UPS—Solving for the unknown

Disney Co.—Solving word problems, Theme parks, Financial reports

Unilever—Solving for the unknown

Procter & Gamble—Solving for the

unknown

Goodyear—Solving for the unknown

Sumitomo Rubber Industries—Solving

for the unknown

Zipcar.com—Kiplinger's

Bank of America—Kiplinger's

Orbitz-Kiplinger's

Expedia—Kiplinger's

Sidestep-Kiplinger's

Travelocity—Kiplinger's, Trade discounts

Bb&T—Kiplinger's

U.S. Small Business—Kiplinger's

Wendy's-Introduction to percents

Coca-Cola Co.—Converting percents to decimals, Solving for the unknown

PepsiCo, Inc.—Converting percents to decimals

Wm. Wrigley Jr., Co.—Percents

American President's Lines-Video case

Jones Apparel Group—Introduction to trade discounts

Nine West-Introduction to trade

discounts

Kodak—Introduction to trade discounts

Federal Express-Freight

CVS—Kiplinger's

Eckerd—Kiplinger's

Walgreens—Kiplinger's

Taco Bell-Discounts

True Value—Introduction to retailing

Bluefly, Inc.-Markup

JCPenney Co.—Markdowns

Sears—Kiplinger's

Family Dollar Store—Kiplinger's

UAL Corp.—Pay scales

Universal Pictures-Work for hire

Washburn Guitars—Video case

AT&T Corp.—Interest introduction

Cisco Systems—Promissory notes

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Treasury Department—Online sales

Xerox—Lines of credit

Home Depot-Loans, Kiplinger's

Conseco-Introduction to compounding

Upromise—Rebates, Kiplinger's

Hewitt Associates—Kiplinger's, 401K

American Express-Tax payment, Online

security

Debt. Solutions—Settling debt,

Kiplinger's

Europay–MasterCard—Smart Card
Saturn Corp—Video case
Fannie Mae—Jumbo mortgage
Freddie Mac—Jumbo mortgage
Eloan—Mortgage
Lendingtree.com—Mortgages
Homespace.com—Mortgages
DIC Entertainment Holdings—Financial reports
Golden Books Family Entertainment—Financial reports
Rent-Way Inc.—Financial reports

Rent-Way Inc.—Financial reports
Kimberly-Clark—Income statement,
Inventory control

Motorola—*Trend analysis*GemStar–T.V. Guide International— *Business models, Kiplinger's*Show Boats International—*Floating condominium*

Land Rover-Depreciation

Campbell Soup Co.—Inventory
Amazon.com—Perpetual inventory
Circuit City—Inventory strategy
America Online—Tax on Internet
MCI World.com—Tax on Internet
Time Warner—Tax on Internet
Gateway—Tax on Internet
Bed Bath & Beyond—Profit margins
GE Financial—Nursing home care
Savings Bank Life—Level premium
Insurance (Massachusetts)—Level
premium
Royal Caribbean Cruises, Ltd.—

Earnings per share
Land O' Lakes—Buyout
Purina Mills Inc.—Buyout
Krispy Kreme—Stock price
Charles Schwab—Web trading

commissions, Tax on Internet

Fidelity Investments—Web trading commissions

TD Waterhouse—Web trading commissions

Ameritrade—Web trading commissions
DLG Direct—Web trading commissions
Datek Online—Web trading commissions
National Discount Brokers—Web trading commissions

Federal Signal Corporation—Video case BMW—Median age Internal Revenue Service—E-filing Ford Motor—India car market Toys "R" Us—New marketing strategy, Kiplinger's

Kiplinger's Personal Finance—Group projects

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CONTENTS

Kiplinger's Personal Finance Magazine Subscription Form 1 Whole Numbers: How to Dissect and Solve Word Problems 3 CHAPTER 1 LU 1-1 Reading, Writing, and Rounding Whole Numbers 5 LU 1-2 Adding and Subtracting Whole Numbers 9 LU 1-3 Multiplying and Dividing Whole Numbers 13 Fractions CHAPTER 2 33 LU 2-1 Types of Fractions and Conversion Procedures 34 LU 2-2 Addition and Subtraction of Fractions 39 LU 2-3 Multiplication and Division of Fractions 45 Decimals 63 CHAPTER 3 LU 3-1 Rounding Decimals; Fraction and Decimal Conversions LU 3-2 Adding, Subtracting, Multiplying, and Dividing Decimals 69 Cumulative Review: A Word Problem Approach—Chapters 1-3 86 Banking 89 CHAPTER 4 LU 4-1 The Checking Account; Credit Card Transactions 90 LU 4-2 Bank Statement and Reconciliation Process; Trends in Online Banking 95 Solving for the Unknown: A How-to Approach CHAPTER 5 for Solving Equations LU 5-1 Solving Equations for the Unknown 115 LU 5-2 Solving Word Problems for the Unknown 119 Percents and Their Applications 133 CHAPTER 6 LU 6-1 Conversions 134 LU 6-2 Application of Percents—Portion Formula 138 Video Case: American President Lines 161 Discounts: Trade and Cash 163 CHAPTER 7 LU 7-1 Trade Discounts—Single and Chain (Includes Discussion of Freight) 164 LU 7-2 Cash Discounts, Credit Terms, and Partial Payments 172 Markups and Markdowns; Insight into Perishables 193 CHAPTER 8 LU 8-1 Markups Based on Cost (100%) 195 LU 8-2 Markups Based on Selling Price (100%) 199 LU 8-3 Markdowns and Perishables 204 Cumulative Review: A Word Problem Approach—Chapters 6-8 218

CHAPTER 9	Payroll	221							
	LU 9-1	Calculating Various Types of Employees' Gross Pay 222							
	LU 9-2	Computing Payroll Deductions for Employees' Pay; Employers' Responsibilities 226							
	Video Cas	e: Washburn Guitars 240							
CHAPTER 10	Simple Interest 243								
	LU 10-1	Calculation of Simple Interest and Maturity Value 244							
	LU 10-2	Finding Unknown in Simple Interest Formula 246							
	LU 10-3	U.S. Rule—Making Partial Note Payments before Due Date 249							
CHAPTER 11	Promissory Notes, Simple Discount Notes, and the Discount Process 263								
	LU 11-1	Structure of Promissory Notes; the Simple Discount Note 264							
	LU 11-2	Discounting an Interest-Bearing Note before Maturity 267							
	Video Case: Online Banking 277								
CHAPTER 12	Compound Interest and Present Value 279								
	LU 12-1	Compound Interest (Future Value)—The Big Picture 280							
	LU 12-2	Present Value—The Big Picture 286							
	Appendix A Additional Homework Assignments by Learning Unit A								
	Appendix B Check Figures B-1								
	Appendix	C Glossary C							
	Index IN								

Practical Business Math Procedures

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Case of Not Enough Ketchup for Meatloaf Squeezes H.J. Heinz

Company Agrees to Overfill Products in California, Pay \$180,000 After Investigation

Staff Reporter of THE WALL STREET JOURNAL By CHRISTINA BINKLEY LOS ANGELES - H.J. Heinz Co. has some catching up to do after two California district attended in the catching and the catching are two california districts attended in the catching are catching and the catching are catching and catching are catching are catching and catching are catc some catching up to do after two Califor-ma district attorneys found it had been underfilling millions of ketchup bottles sold in this bastion of consumer protec-tion

Caught red-handed after a four-year investigation, the Pittsburgh-based ketchup wesuganon, the riusturgh-based ketchap manufacturer agreed yesterday to make up for shorting its customers by overfilling up for shorting his customers by overhing its 18- to 64-ounce bottles in California. So for the next year, California ketchup buyers can anticipate getting a tiny freebie—a ers can anticipate getting a tiny freebie—a little less air and about one extra ounce of little less air and about one extra ounce in the ketchup in a bottle of Heinz. "We're going to return about 10 million ounces to the to return about 10 million. That is expected of the Los Angeles district attorney head of the Los Angeles district. That is exconsumer-protection division. consumer-protection division. That is expected to cost Heinz about \$650,000.

Whole Numbers; How to Dissect and Solve Word Problems

LEARNING UNIT OBJECTIVES

LU 1-1: Reading, Writing, and Rounding Whole Numbers

- Use place values to read and write numeric and verbal whole numbers (p. 5).
- Round whole numbers to the indicated position (pp. 6-7).
- Use blueprint aid for dissecting and solving a word problem (p. 7).

LU 1-2: Adding and Subtracting Whole Numbers

- Add whole numbers; check and estimate addition computations (pp. 9-10).
- Subtract whole numbers; check and estimate subtraction computations (pp. 11-12).

LU 1-3: Multiplying and Dividing Whole Numbers

- Multiply whole numbers; check and estimate multiplication computations (pp. 13–14).
- Divide whole numbers; check and estimate division computations (pp. 15-16).

People of all ages make personal business decisions based on the answers to number questions. Numbers also determine most of the business decisions of companies. For example, click on your computer and go to the website of a company such as eBay and note the importance of numbers in the company's business decision-making process.

The following *Wall Street Journal* clipping illustrates how McDonald's fast-food chain plans to increase its profit numbers by changing its business strategy.

Will Big Mac Find New Sizzle In Shoes, Videos?

By JENNIFER ORDONEZ
Staff Reporter of The Wall Street Journal

McDonald's Corp. wants to supersize its brand name.

Led by a new brand-extension executive, the burger giant is quietly developing or expanding several lines of McDonald's-brand consumer goods. Already, German consumers are buying McDonald's-brand ketchup, and for some time American parents have been picking up McKids clothing and shoes at Wal-Mart stores. Under consideration now are McDonald's-brand snacks and other packaged goods, as well as a line of McDonald's books and videos.

"A few years from now, people will say, 'I remember when McDonald's was a restaurant," says Peter Oakes, a restaurant analyst for Merrill Lynch Global Securities who has caught wind of the strategy and is preparing a report on it. "Why not do something more than just sponsor Saturday morning cartoons?"

McDonald's has yet to announce the strategy, whose initial thrust will likely be overseas. But a



Jack Greenberg

year ago it created a new executive position—vice president for corporate strategy—to explore ways of extending the McDonald's brand. Mats Lederhausen, who holds the title, reports directly to Chief Executive Jack Greenberg.

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Companies often follow a general problem-solving procedure to arrive at a change in company policy. Using McDonald's as an example, the following steps illustrate this procedure:

Step 1.	State the problem(s).	The restaurant business is very competitive. A new strategy is needed that broadens the scope of sales and results in a continued increase in profits.
Step 2.	Decide on the best method(s) to solve the problem(s).	Create new products (ketchup; McKids clothing and shoes) with McDonald's brand name.
Step 3.	Does the solution make sense?	Test market new products overseas (ketchup). Sell McKids clothing and shoes at Wal-Mart.
Step 4.	Evaluate results.	All test markets will be evaluated before worldwide distribution begins.

Have you seen the new H. L. Heinz Company's green ketchup? McDonald's-brand ketchup was introduced in Germany to compete with the Heinz ketchup—the No. 1 seller of ketchup in Germany. How well is McDonald's-brand ketchup performing in the Heinz market? As you may expect, a spokesman for Heinz answers, "Not very well, consumers tell us ours is better." The driving force behind McDonald's desire to add new products such as ketchup to its brand name is higher profit numbers.

Your study of numbers begins with a review of basic computation skills that focuses on speed and accuracy. You may think, "But I can use my calculator." Even if your instructor allows you to use a calculator, you still must know the basic computation skills. You need these skills to know what to calculate, how to interpret your calculations, how to make estimates to recognize errors you made in using your calculator, and how to make

Learning Unit 1–1 5

calculations when you do not have a calculator. (How to use a calculator is explained in the *Business Math Handbook* and on the Slater website.)

The United States' numbering system is the **decimal system** or *base 10 system*. Your calculator gives the 10 single-digit numbers of the decimal system—0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. The center of the decimal system is the **decimal point**. When you have a number with a decimal point, the numbers to the left of the decimal point are **whole numbers** and the numbers to the right of the decimal point are decimal numbers (discussed in Chapter 3). When you have a number *without* a decimal, the number is a whole number and the decimal is assumed to be after the number.

This chapter discusses reading, writing, and rounding whole numbers; adding and subtracting whole numbers; and multiplying and dividing whole numbers.

LEARNING UNIT 1-1 READING, WRITING, AND ROUNDING WHOLE NUMBERS

	nes, ranked by Internet re	volido.
AIRLINE	1999	2000*
Southwest	\$877,000,000	\$1,280,000,000
United	505,000,000	1,190,000,000
American	416,000,000	1,060,000,000
Delta	671,000,000	1,040,000,000
US Airways	450,000,000	800,000,000

We often use whole numbers in business calculations. For example, look at *The Wall Street Journal* clipping "Click and Soar." Note that in 2000 the Internet revenue of Southwest airline increased to \$1,280,000,000. From the information in this unit, you will learn that you can read this numeric whole number as one billion, two hundred eighty million. Now let's begin our study of whole numbers.

*Estimated.

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Reading and Writing Numeric and Verbal Whole Numbers

The decimal system is a *place-value system* based on the powers of 10. Any whole number can be written with the 10 digits of the decimal system because the position, or placement, of the digits in a number gives the value of the digits.

To determine the value of each digit in a number, we use a place-value chart (Figure 1.1) that divides numbers into named groups of three digits, with each group separated by a comma. To separate a number into groups, you begin with the last digit in the number and insert commas every three digits, moving from right to left. This divides the number into the named groups (units, thousands, millions, billions, trillions) shown in the place-value chart. Within each group, you have a ones, tens, and hundreds place.

In Figure 1.1, the numeric number 1,605,743,891,412 illustrates place values. When you study the place-value chart, you can see that the value of each place in the chart is 10 times the value of the place to the right. We can illustrate this by analyzing the last four digits in the number 1,605,743,891,412:

$$1,412 = (1 \times 1,000) + (4 \times 100) + (1 \times 10) + (2 \times 1)$$

So we can also say that in the number 745, the "7" means seven hundred (700); in the number 75, the "7" means 7 tens (70).

To read and write a numeric number in verbal form, you begin at the left and read each group of three digits as if it were alone, adding the group name at the end (except the last units group and groups of all zeros). Using the place-value chart in Figure 1.1, the

FIGURE 1.1
Whole number place-value chart

Whole Number Groups

	rillio	ns			Billio	ns		/	Milli	ons	/	/TI	nous	ands			Unit	s	
Hundred trillions	Ten trillions	Trillions	Comma	Hundred billions	Ten billions	Billions	Comma	Hundred millions	Ten millions	Millions	Comma	Hundred thousands	Ten thousands	Thousands	Comma	Hundreds	Tens	Ones	Decimal Point
74.5		1	1	6	0	5		7	4	3	3	8	9	1		4	1	2	1.0

Rounding Whole

Numbers

number 1,605,743,891,412 is read as one trillion, six hundred five billion, seven hundred forty-three million, eight hundred ninety-one thousand, four hundred twelve. You do not read zeros. They fill vacant spaces as placeholders so that you can correctly state the number values. Also, the numbers twenty-one to ninety-nine must have a hyphen. And most important, when you read or write whole numbers in verbal form, do not use the word *and*. In the decimal system, *and* indicates the decimal, which we discuss in Chapter 3.

By reversing the above process of changing a numeric number to a verbal number, you can use the place-value chart to change a verbal number to a numeric number. Remember that you must keep track of the place value of each digit. The place values of the digits in a number determine its total value.

Many of the whole numbers you read and hear are rounded numbers. Government statistics are usually rounded numbers. The financial reports of companies also use rounded numbers. All rounded numbers are *approximate* numbers. The more rounding you do, the more you approximate the number.

Rounded whole numbers are used for many reasons. With rounded whole numbers you can quickly estimate arithmetic results, check actual computations, report numbers that change quickly such as population numbers, and make numbers easier to read and remember.

Numbers can be rounded to any identified digit place value, including the first digit of a number (rounding all the way). To round whole numbers, use the following three steps:

Rounding Whole Numbers

- **Step 1.** Identify the place value of the digit you want to round.
- **Step 2.** If the digit to the right of the identified digit in Step 1 is 5 or more, increase the identified digit by 1 (round up). If the digit to the right is less than 5, do not change the identified digit.
- Step 3. Change all digits to the right of the rounded identified digit to zeros.

EXAMPLE 1 Round 9,362 to the nearest hundred.

Step 1. 9,362 The digit 3 is in the hundreds place value.

Step 2. The digit to the right of 3 is 5 or more (6). Thus, 3, the identified digit in Step 1, is now rounded to 4. You change the identified digit only if the digit to the right is 5 or more.

9,462

Step 3. 9,400 Change digits 6 and 2 to zeros, since these digits are to the right of 4, the rounded number.



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By rounding 9,362 to the nearest hundred, you can see that 9,362 is closer to 9,400 than to 9,300.

We can use *The Wall Street Journal* clipping "McDonald's Restaurants in Selected Cities" to illustrate rounding to the nearest hundred. Note that the number of restaurants in Chicago is 440 and in Sao Paulo, 182. Round these numbers to the nearest hundred as shown above and you can say, "Chicago has 400 McDonald's restaurants; Sao Paulo has 200 restaurants." Numbers rounded to the nearest hundred can either be relatively less than the actual number, as in the Chicago restaurants, or a little more than the actual number, as in the Sao Paulo restaurants. Next we show you how to round to the nearest thousand.