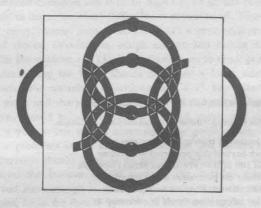
## Solving Problems in Analytical Chemistry Brewer

## Solving Problems in Analytical Chemistry



## Stephen Brewer

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Solving Problems in Analytical Chemistry

### Preface

A knowledge of analytical chemistry is important to students of many different disciplines. Thus in a typical class there will not only be students majoring in chemistry and chemical engineering but also those who are studying soil science, poultry science, dietetics, medical technology, and biology. Often, the biggest difficulty that these students, chemistry majors included, encounter is that of doing the necessary calculations in laboratory and classroom work.

The purpose of this book is to give students a readable, detailed, and useful guide to the calculations required in a beginning analytical chemistry course. Some knowledge of algebra and graphing is assumed, but no knowledge of calculus is required. Moreover, no calculus is introduced, although many topics in algebra and graphing are reviewed.

Generally, the best way to learn how to solve problems in any discipline is to work through detailed examples and then to try to solve similar problems, whose solutions are available in instances where difficulty is encountered. Thus I divided each section of almost every chapter into three parts: (1) a presentation with some descriptive material of typical calculations, which are worked out in detail; (2) a number of problems for the student; and (3) detailed solutions to those problems.

The student using the book should first buy a hand calculator, preferably one featuring scientific notation, logarithms, and a y<sup>x</sup> key. Next he or she should get plenty of paper and sharp pencils. Each one of the calculations in the first part of a given section should be worked out with pencil, paper, and calculator. (Marking the text with a yellow pen almost never does any good.) Then the student should do each of the problems at the end of the section. An earnest attempt of at least five minutes' duration should be made on any given problem. If no progress is made after this attempt, the student should turn to the detailed solutions that follow the problems and learn enough at least to get a start. Once the student has worked all of the problems, he or she should try to work them once again, to determine whether the knowledge just acquired has been retained. Finally, two or more people can usually secure a quiet classroom with a blackboard and quiz each other on the problems. The process requires time, it is true, but these detailed examples and solutions should make learning how to calculate a less fearsome task.

This book may be assigned as a supplementary text by an instructor, or it may, in combination with a detailed laboratory manual, be used as the lecture text for a course. I have followed the latter course of action, perhaps because calculations are very heavily stressed in my own lectures. There are many correct ways to teach analytical chemistry, and therefore each instructor in the discipline should make his or her own choice.

In this book, I cover the calculations most frequently encountered in most beginning analytical chemistry courses. There are six chapters in the book: Chapter 1 on basic material, covering basic graphing, statistics, and stoichiometry; Chapter 2 on acid-

base chemistry, in which solutions by approximation methods are stressed, and in which polyprotic acids with closely spaced dissociation constants are given their just due; Chapter 3 on solubility control, with approximation methods and a stress on complexation and acid dissolution; Chapter 4 on spectrophotometry, which includes, after basic analytical material, calculations of physical constants; Chapter 5 on potentiometry, ranging from simple cells through titrations, to physical constants and activities to ion-selective electrodes; and Chapter 6 on separations, beginning with separatory funnel extractions, going through multistage (Craig) separations, to liquid-liquid chromatography, through gas chromatography to sorption chromatography.

It would be best if the chapters were taken in the order just listed. However, it is possible to study each of the first five chapters independently. The sixth chapter, that on separations, does require knowledge of topics covered in Chapters 1, 2, and 4.

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## Acknowledgments

I acknowledge first the generous contribution of Professor John Walters, of the Department of Chemistry at the University of Wisconsin-Madison. Professor Walters was my mentor during my graduate school days at Madison, and thus made a great contribution to the shaping of this book, although neither of us had such a project in mind at that time. In later years, Professor Walters wrote a set of highly detailed notes, which he then distributed to his classes in analytical chemistry. He very kindly sent me sets of these massive notes and urged me to use his material freely, which I was pleased to do.

In 1974, Professor Walters and I decided, together with Gary Carlson of Wiley, that the notes should be used as the basis for a textbook. The textbook was to emphasize problem solving for analytical chemistry, and was to contain vast numbers of solved problems.

Time went by quickly. In 1976, Professor Walters, as busy as a chemist could possibly be, generously offered me, for use in this book, any of the material contained in his notes and problem sets. The material represents a labor of several years on his part and represents an intense dedication to making complicated matters accessible to the beginning student in analytical chemistry. Indeed, the material is a symbol of his dedication to students.

Professor Walters' influence is found particularly in the section on stoichiometry and in the chapters on acids, solubility, spectrophotometry, and potentiometry. I have taken much that appears in these parts of this book directly from his notes. In the chapters on acids and solubility, his approach using approximations and  $\alpha$ -and  $\beta$ -functions is closely followed. (Professor Walters has told me that Professor H. L. Laitinen, then at the University of Illinois, introduced him to the  $\alpha$ - and  $\beta$ -functions) I should like, then, gratefully to acknowledge my debt to Professor Walters, without whose efforts, dedication, and generosity this book would not have appeared.

Professors J. Schrag and J. Wright, also of the Department of Chemistry at Madison, have made considerable contributions both to Professor Walters' notes and to this book. Professor D. Coleman, of Wayne State University, read the typescript and offered valuable suggestions.

Assistance in computer programming was given by Dr. A. Scheeline, then of the University of Wisconsin, who helped me write a program executed at the Madison Academic Computer Center. Also, B. Finzel, of Eastern Michigan's Chemistry Department, and R. Frownfelter, of University Computing at Eastern Michigan, made a plotting program produce the desired graphs with Eastern Michigan's instructional computer system.

Several patient and able typists helped me to prepare the typescript. They are Ms. P. Quinn, Ms. J. Wright, Ms. L. Mundt, Ms. J. Haynie, Ms. L. Myers, and Ms. C. Bashawaty.

Gary Carlson, Chemistry Editor at Wiley, gave me much help and coordinated the work of three other analytical chemists who reviewed the typescript. Nina R. West, production supervisor, gave her best efforts to the sometimes trying task of getting the book from manuscript to printed pages.

Finally, there were my student helpers—about 200 of them both at Madison and at Ypsilanti. From two of them, Vicki McGuffin and Kena Helkaa, I borrowed quires of data. Others read preliminary editions of the book, and eagerly sought and reported errors. Patrick Harrington helped proofread the galleys. (With this company of diligent proofreaders, I hope that errors are few but would be grateful to anyone who discovers and informs me of errors.)

My colleagues in the Chemistry Department at Eastern Michigan and the Eastern Michigan University administration gave me a sabbatical leave for the writing. The chemistry faculty at Madison very kindly furnished me working facilities during that leave and invited me to teach a summer session and spring term, doing everything to make me feel welcome.

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## Contents

#### Chapter One

## **Basic Material**

1.1	USEFUL STATISTICS		
	1.2	Significant Figures	2
357.3	1.3	Accuracy and Precision	5
	1.4	Errors	10
	1.5	Mathematical Description of Random Error Distributions	10
	1.6	Comparison of Two Means	.19
	1.7	Rejection of a Discordant Datum	23
	1.8	Graphing	25
	1.9	Problems	30
	1.10	Detailed Solutions to Problems	35
1.11	STOICHIOMETRY		
	1.12	Simple Gravimetric Calculations	51
	1.13	Indirect Analyses	56
	1.14	Solutions and Coupled Chemical Reactions	58
	1.15	Problems	73
	1.16	Detailed Solutions to Problems	76

#### Chapter Two

## **Acid-Base Chemistry**

2.1	GEN	ERAL DISCUSSION	93
2.2	STRO	ONG ACIDS AND BASES	97
	2.3	Strong Acids	97
	2.4.	Strong Bases	101
	2.5	Problems	104
	2.6	Detailed Solutions to Problems	105
2.7	WEA	K MONOPROTIC ACIDS	109
	2.8	Weak Acids Alone in Solution	109
-	2.9	Buffers of Weak Monoprotic Acids	112
	2.10	The Anions of Weak Acids Alone	117
	2.11	Distribution Functions	119
	2.12	Problems	121
	2.13	Detailed Solutions to Problems	123
2.14	WEA	K POLYPROTIC ACIDS	130
	2.15	Distribution Functions	131
	2.16	Solutions of Weak Polyprotic Acids in Water	135
	2.17	Buffers of Weak Polyprotic Acids	139
	2.18	The Unprotonated Anions of Weak Acids	147
	2.19	Ampholytes	149
	2.20	Problems	153
	2.21	Detailed Solutions to Problems	154
2.22	THE	TITRATION OF WEAK ACIDS	168
	2.23	Titration of Weak Monoprotic Acids with	
		Strong Bases	168
	2,24	Titration of Weak, Well-Behaved Polyprotic Acids with Strong Bases	172
	2.25	Titration of Any Polyprotic Acids (Well- or	172
	2.43	III-Behaved) with Strong Bases	179
	2.26	Problems	184
	2.27	Detailed Solutions to Problems	188
2.28	WFA	K BASES	199
2.20	2.29		199
	2.30	Buffers of Weak Monoacidic Bases	201
	2.31	The Protonated Cations of Weak Bases	203
	2.32	The Titration of Weak Bases by Strong Acids	205
	2.33	Problems	207
	2.34	Detailed Solutions to Problems	208
	and a real of	E THE STATE OF THE	200

#### Chapter Three

## The Control of Solubility

H TO S					
3.1	INTRODUCTION	218			
	3.2 The Common Ion Effect	222			
	3.3 Differential Solubility	224			
	3.4 Problems	226			
	3.5 Detailed Solutions to Problems	228			
3.6	COMPLEX FORMATION WITH A LIGAND	236			
	3.7 Problems	240			
to to ca	3.8 Detailed Solutions to Problems	240			
3.9	FORMATION OF A WEAK ACID WITH				
	THE ANION OF THE PRECIPITATE	242			
	3.10 Problems	247			
	3.11 Detailed Solutions to Problems	247			
	Absorption Spectro- photometry				
4.1	BASIC RELATIONSHIPS AND				
	INSTRUMENTATION	254			
	4.2 A Derivation of Beer's Law	256			
	4.3 A Simple Spectrophotometric Instrument	262			
	4.4 Problems	264			
	4.5 Detailed Solutions to Problems	265			
4.6	SOME APPLICATIONS OF ABSORPTION				
×	SPECTROPHOTOMETRY	269			
	4.7 Simple Applications	269			
	4.8 Finding the Wavelength of				
	Maximum Absorption	270			
	4.9 Plotting the Beer's Law Graph	271			
	4.10 Finding the Concentration of				
	an Unknown	272			
	4.11 Error	273			
		1 122			

Contents / XIII

		4.12 Chemical errors	274		
		4.13 Errors of monochromation	274		
		4.14 Error resulting from	076		
	115	uncertainty in readout	275		
	4.15	Simultaneous Analysis of Two or More Components	276		
	4.16	Spectrophotometric Titrations	285		
	4.17	Spectrophotometric Determination of			
		Physical Constants	287		
		4.18 Metal-Ligand Complexes	289		
		4.19 The mole-ratio method	289		
		4.20 The method of continuous			
		variations	294		
		4.21 The slope-ratio method	299		
	4.00	4.22 K <sub>a</sub> -Values for Indicator Dyes Problems	304		
	4.23	Detailed Solutions to Problems	310 319		
	4.24	Detailed Solutions to Problems	313		
	Chap	ter Five			
	Do	tentiometry			
	ro	tentionetry			
	INITO	ODUCTION	220		
1	INIK	ODUCTION	338		
2	BASIC CONSIDERATIONS				
	5.3	Problems	349		
	5.4	Detailed Solutions to Problems	350		
31.	DOTE	NELONISTENS TITE ATIONS	255		
5		ENTIOMETRIC TITRATIONS	355		
	5.6	Prediction of Curve Shapes	355		
	5.7 5.8	Endpoint Detection Problems	373		
	5.9	Detailed Solutions to Problems	374		
			314		
0		SICAL CONSTANTS AND			
	ACTI	VITIES	381		
	5.11	Physical Constants	381		
	5.12	Activities and Activity Coefficients	385		
1	5.13	Problems	393		
	5.14	Detailed Solutions to Problems	394		
5	ION-SELECTIVE ELECTRODES				
D In	5.16	Problems	401		
	5.17	Detailed Solutions to Problems	412		

5.

5.1

5.1

#### Chapter Six

## Separations Not Involving Precipitation

6.1	INTE	RODUCTION				
6.2	IMMISCIBLE LIQUID PHASES USING					
	SEPA	RATO	RY FUNNELS	414		
	6.3	Proble	ems	426		
	6.4	Detail	ed Solutions to Problems	430		
6.5	MULTISTAGE LIQUID-LIQUID					
	EXTRACTIONS					
	6.6	Proble	ems	447		
	6.7	Detail	ed Solutions to Problems	449		
6.8	LIQU	LIQUID-LIQUID CHROMATOGRAPHY				
	(LLC	)		454		
	6.9		nuous Countercurrent Extraction			
		Metho	ods	455		
	6.10	Real L	iquid-Liquid Chromatography (LLC)	455		
		6.11	Classical Column Chromatography	455		
		6.12		458		
		6.13	Thin-Layer Chromatography (TLC)	460		
		6.14	High-Performance Liquid-Liquid Chromatography (HPLC)	462		
	6.15	A Ref	lection	466		
5.16	GAS-LIQUID CHROMATOGRAPHY (GLC)					
	6.17		n Apparatus for Gas-Liquid			
		Chromatography				
	6.18	Some	471			
		6.19	Calculating the Number of Theoretical Plates on a Column			
			and the HETP for a Column	472		
		6.20	Calculation of the Number of Theoretical Plates Required for Resolution of Two Sample			
		C 21	Component Peaks	474		
		6.21	Determination of the Optimum Flow Rate	476		

		6.22	Qualitative Analysis		482
		6.23	Quantitative Analysis		486
	6.24	Probler	ns		493
	6.25	Detaile	d Solutions to Problems		495
6.26	SEPA	RATIO	NS BY SORPTION		
	CHR	CHROMATOGRAPHY			
	6.27	Probler	ns HOUGOSTHE 13		- 511
	6.28	Detaile	d Solutions to Problems		516
APPE	NDIX.	FOUR-P	LACE LOGARITHMS O	F	
	NUM	BERS	T THE PERSON NAMED IN		525
INDE	X				531

# chapter 1 Basic Material

#### ■ 1.1 USEFUL STATISTICS ■

In 1954, a charming little volume entitled *How to Lie with Statistics* appeared.\* The author's purpose was to educate the literate public in all the statistical ruses that could be used to influence them to buy a particular product or vote for a particular office seeker. The members of the author's high school debating team eagerly sought the book out. The purpose of *our* discussion of statistical matters is not chiefly to protect students from purveyors of snake oil, but to aid them in interpreting and evaluating their own and others' data. A rudimentary knowledge of statistics, intelligently applied, can give fairly satisfactory answers to such questions as:

- 4 1. How many figures in an answer are significant (have meaning)?
- 2. What do the terms accuracy and precision mean, and how do they differ?
- 3. What are some measures of accuracy and precision?
- H 4. What sorts of errors plague results?
- д 5. How may one mathematically describe distributions of random errors?
- m 6. Can it be determined whether two averages are significantly different from each other?
- # 7. Can a result that looks bad, or deviant, be cast out?

<sup>\*</sup> Darrell Huff, How to Lie with Statistics, Norton, New York, 1954.

8. How can one draw the best straight line through points that ought to (but do not quite) line up?

#### 1.2 Significant Figures

Let us address the first question. Modern-day computing techniques and pocketsized calculators make it likely that workers will retain a great many more significant figures than they really should.

#### **EXAMPLE:**

Multiply

$$(1.236) \cdot (4.859)$$

on a pocket calculator.

$$(1.236) \cdot (4.859) = 6.005724$$

The multiplier and multiplicand each contain four digits. The product, displayed on the dial of a calculator, contains 7. If numbers are simply being multiplied together, this is all right, but what happens when each number is part of a measurement? Is the area of a square 1.236 in. by 4.859 in. exactly 6.005724 in.<sup>2</sup>? Can one start with four-figure numbers, and finish with a seven-figure number, all of whose digits are significant? Of course not! The following rules will help the student avoid at least the sillier mistakes in manipulation.

RULE 1 / Retain no digits beyond the first uncertain one.

#### **EXAMPLE:**

On a balance, you might read a mass as 21.4238 grams. This number means, in practice,  $21.4238 \pm 0.0002$  grams because  $\pm 0.0002$  grams is the uncertainty stated by the manufacturer. The last figure, 8, is uncertain.

You should not guess one more figure. In a number such as 21.42387 grams, guessed on the same balance, the 7 would be meaningless.

RULE 2 / Rounding off. The residue is the digit to be dropped. If the residue > 5, increase the digit to the left of the residue by 1.

If the residue < 5, do not change the digit to the left of the residue.

If the residue = 5, and the digit to the left of the residue is even, do not change the digit to the left of the residue. If

the digit to left of residue is odd, increase the digit to the left of the residue by 1.

RULE 3 / In addition or subtraction, one may safely retain only as many digits to the right of the decimal as there are in addend or subtrahend with the smallest number of digits to the right of the decimal point.

#### **EXAMPLE:**

48.7 2.941 33.13 84.771 → 84.8

RULE 4 / In multiplication and division, the relative uncertainty in the product or quotient must be the same as the relative uncertainty in the factor with the lowest number of significant figures. In simple terms, this means roughly that the number of significant figures in the answer may not exceed the number of significant figures in the factor with the lowest number of significant figures.

#### **EXAMPLES:**

 $(1.0923)(2.07) = 2.261061 \rightarrow 2.26$ three significant figures also three significant figures  $(1.0923)(207) = 226.1061 \rightarrow 226$ 

#### CAUTION:

What is the average of these four replicates done on one chloride sample?