

 WILEY

# INTRODUCTION TO SOFT MATTER

Polymers, Colloids, Amphiphiles  
and Liquid Crystals

Ian W. Hamley



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Liquid Crystals

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# Preface

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This book is largely intended to provide an introduction to colloid chemistry, but I have used the term 'soft matter' to indicate a unified subject that includes aspects of liquid crystal and polymer science not found in existing textbooks on colloid chemistry. General textbooks of physical chemistry either do not cover colloid chemistry at all or fail to give it the space it deserves. There is less than a handful of recent books that give a broad coverage of the physical chemistry of soft materials, and these are written at an advanced level. For both these reasons, and also given that existing introductory colloid chemistry texts are mostly getting rather long in the tooth, I felt that a new book in the area offering up-to-date and unified coverage, would be valuable both to students and researchers.

The book has been written primarily for undergraduates taking physical chemistry courses. In Leeds it is a companion book to the final year module 'Physical Chemistry of Condensed Matter'. I hope it will also be of interest to students of physics and materials science taking courses on colloids, polymers, soft condensed matter or complex fluids. It should also serve as a useful introduction and reference for researchers in these areas.

I wish to thank my editors at Wiley for assistance in the production of the book.

IWH

Leeds, 1999

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# 1 Introduction

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## 1.1 INTRODUCTION

Mankind has exploited matter in technology through the ages. For many millenia, we relied on materials like wood or metals that were subject to minimal processing to provide useful objects. It is only within a few minutes of midnight on the proverbial human evolutionary clock that materials have been engineered for ultimate applications based on a deep understanding of molecular properties. Considering substances that have been engineered in a controlled or tailored manner, the nineteenth century was the age of iron and steel. The twentieth century saw the development of new types of engineered materials, especially polymers, which in the form of plastics have, in many applications, usurped many of the traditional 'hard' materials. This is not to forget the emergence of an important class of inorganic material, semiconductors, in the second half of this century. These are, of course, the basis for the second industrial revolution, that of information technology. However, it seems fair to say that many properties of hard matter are now well understood whereas we are still on the learning curve with soft matter. For example, inspired by nature, we are only just beginning to be able to engineer complex structures formed by biopolymers or to exploit nanotechnology to make devices based on self-organization of polymers. In our new millennium it seems safe to predict the continued importance of soft materials, engineered in ways we can as yet only dream of.

The idea of a unified approach to 'soft materials' has only gained ground recently. It is an interdisciplinary subject, taking in aspects of physics, chemistry and materials science, but also of biochemistry or (chemical, mechanical) engineering in specific cases. A consequence of this interdisciplinarity is

that, unfortunately, the subject is not considered in conventional textbooks on physics, physical chemistry or materials science, often being neglected entirely or covered in an inadequate manner. The purpose of this book is to 'fill the gap', by providing an up-to-date introductory summary of the thermodynamics and dynamics of soft materials. In each of the five chapters, the basic physical chemistry is covered first, prior to an outline of applications. The material is presented in a coherent fashion across the book. Equations have been kept to the minimum number that capture important relationships. Derivations are included, where they illustrate thermodynamical or statistical mechanical principles in action. The derivation of the Flory–Huggins theory in Section 2.5.6 or of the thermodynamics of micellar equilibria in Section 4.6.5 are good examples. Soft materials are important in many products, such as detergents, paints, plastics, personal care products, foods, clays, plastics and gels. Such uses of soft materials are exemplified throughout this book.

In this book we consider soft materials under the headings of polymers (Chapter 2), colloids (Chapter 3), amphiphiles (Chapter 4) and liquid crystals (Chapter 5). The distinctions between these systems are often not strong. For example, amphiphiles in solution and some aspects of polymer science are often considered in books on colloid chemistry. However, here we treat them separately since they are technologically important enough to merit detailed consideration on their own. The chapter on liquid crystals is in fact focused on one class of material, thermotropic liquid crystals, where phase transitions are thermally driven. However, a different class of liquid crystal phase is formed in amphiphile solutions, where concentration is also a relevant variable. These are termed lyotropic liquid crystal phases and are discussed in Chapter 4.

There are a number of texts that deal with aspects of the subjects covered in this book. General texts in the area include those by Evans and Wennerström, Hunter, Larson and Shaw (see Further Reading at the end of the chapter). Detailed textbooks for background reading on each topic are listed in the Further Reading section that follows each chapter. In



Chapter 2, polymer science is outlined in a particularly concise form, and after the fundamentals are introduced, attention is paid to applications of polymers in the latter part of the chapter. There are quite a number of monographs concerned with colloids. However, many of these are not suitable for use as undergraduate textbooks. Thus, Chapter 3 fulfills a particularly useful function in providing an up-to-date introduction to the essential physical chemistry. Also emphasized are applications of colloids and colloids in everyday life, such as in foods. Chapter 4 summarizes the important aspects underpinning the self-assembly of amphiphiles, i.e. surfactants and lipids. The action of surfactants as detergents is also considered and the importance of lipids in cell membranes is discussed. Chapter 5 is concerned with thermotropic liquid crystals. Recommended texts for background reading on these subjects are listed in the Further Reading sections.

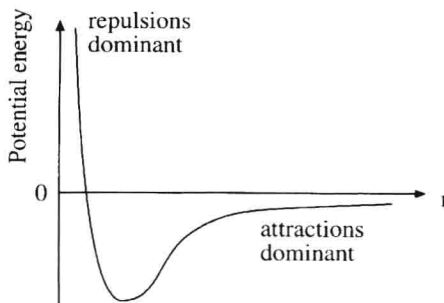
In this chapter, intermolecular forces that are the basis of self-assembly are considered in Section 1.2. Section 1.3 outlines common features of structural ordering in soft materials. Section 1.4 deals similarly with general considerations concerning the dynamics of macromolecules and colloids. Section 1.5 focuses on phase transitions along with theories that describe them, and the associated definition of a suitable order parameter is introduced in Section 1.6. Scaling laws are defined in Section 1.7. Polydispersity in particle size is an important characteristic of soft materials and is described in Section 1.8. Section 1.9 details the primary experimental tools for studying soft matter and Section 1.10 summarizes the essential features of appropriate computer simulation methods.

## 1.2 INTERMOLECULAR INTERACTIONS

The term 'soft' matter originates from macroscopic mechanical properties. We mean here materials such as colloids, surfactants, liquid crystals and polymers in the melt or solution. Many soft materials can be induced to flow under certain

conditions. This weak ordering results from the lack of three-dimensional atomic long-range order found in a crystalline solid. Nevertheless, there is always a degree of local order at least as great as that in a liquid. From the viewpoint of kinetic energy, a crude distinction between 'soft' materials and 'hard' ones can be made on the basis that the molecular kinetic energy for the former is close to  $k_B T$ , whereas for the latter it is much less than  $k_B T$  (when the temperature is near ambient). Here we consider the intermolecular forces responsible for the ordering of soft materials. Our purpose is not to provide a detailed description of these forces, since this is dealt with in many physical chemistry textbooks (for example Atkins, 1998). Here we briefly outline the essential results, especially in the context of self-assembly in soft matter, which is the subject of this book.

The forces between molecules are a balance of repulsive interactions at short distances and attractive interactions that predominate over larger length-scales. This is illustrated by the curve of potential energy as a function of intermolecular separation in Fig. 1.1. We will now consider the origin of the repulsive and attractive forces. Then we consider Coulombic forces since ions are present in solution in many colloid and surfactant systems, and in this case interactions between charged species predominate.



**Figure 1.1** Typical curve of potential energy versus separation of two molecules or atoms. At short distances, repulsive interactions predominate, whilst attractive forces act over a longer range

Repulsive interactions are important when molecules are close to each other. They result from the overlap of electrons when atoms approach one another. As molecules move very close to each other the potential energy rises steeply, due partly to repulsive interactions between electrons, but also due to forces with a quantum mechanical origin in the Pauli exclusion principle. Repulsive interactions effectively correspond to steric or excluded volume interactions. Because a molecule cannot come into contact with other molecules, it effectively excludes volume to these other molecules. The simplest model for an excluded volume interaction is the hard sphere model. The hard sphere model has direct application to one class of soft materials, namely sterically stabilized colloidal dispersions. These are described in Section 3.14. It is also used as a reference system for modelling the behaviour of simple fluids. The hard sphere potential,  $V(r)$ , has a particularly simple form:

$$V(r) = \begin{cases} \infty & \text{for } r \leq d \\ 0 & \text{for } r > d \end{cases} \quad (1.1)$$

where  $d$  is the diameter of the hard sphere. The ordering of hard spheres depends only on their volume fraction. The phase diagram has been obtained by computer simulations and experiments on sterically stabilized colloid particles, as discussed in Section 3.14.

The hard sphere model is based on the excluded volume of spherical particles. An excluded volume theory has been developed to account for the orientational ordering of liquid crystal molecules, assuming them to be hard rods. This is the Onsager theory and its variants, outlined in Section 5.5.2. Excluded volume interactions influence the conformation of polymer chains. The conformation of an ideal chain is described by a random walk. However, in this case the chain can cross itself, i.e. it has no excluded volume. Under certain circumstances a polymer chain can behave as if this was the case (see Section 2.3.2). However, it is more usual for excluded volume interactions to lead to a self-avoiding walk,

which produces a more extended conformation than that of a random walk (Section 2.3.2).

Because there are no attractive interactions in the potential, the hard sphere model does not describe the forces between molecules very well. More realistic potentials include an attractive contribution, which usually varies as  $-1/r^6$  (as discussed shortly) as well as a repulsive term. The latter is chosen to vary as  $1/r^n$ , with  $n > 6$ , to ensure that repulsions dominate at short distances,  $n = 12$  often being assumed. This combination of attractive and repulsive terms defines the Lennard–Jones (12,6) potential:

$$V(r) = 4\varepsilon \left[ \left( \frac{r_0}{r} \right)^{12} - \left( \frac{r_0}{r} \right)^6 \right] \quad (1.2)$$

Here  $\varepsilon$  is the depth of the potential energy minimum and  $2^{1/6}r_0$  is the intermolecular separation corresponding to this minimum. This potential has a form similar to that shown in Fig. 1.1. It is often used as a starting point for modelling intermolecular interactions, for example it can be chosen as the intermolecular potential in computer simulations (see Section 1.10). It is not completely realistic, though, because for example it is known that the  $1/r^{12}$  form is not a good representation of the repulsive potential. An exponential form  $\exp(-r/r_0)$  is better because it reproduces the exponential decay of atomic orbitals at large distances, and hence the overlap which is responsible for repulsions.

Attractive interactions in uncharged molecules result from van der Waals forces, which arise from interactions between dipoles. A molecule has a dipole moment if it contains two opposite charges of magnitude  $q$ , separated by some distance  $\mathbf{r}$ . Such a molecule is said to be polar. The dipole moment is then defined by  $\boldsymbol{\mu} = q\mathbf{r}$ . Dipole moments of small molecules are usually about 1 debye (D), where  $1 \text{ D} = 3.336 \times 10^{-30} \text{ C m}$ . Some molecules, such as  $\text{H}_2\text{O}$ , possess a permanent dipole moment due to charge separation resulting from the electronegativity of the oxygen atom. Dipolar molecules can also induce dipole moments in other molecules producing dipole-induced dipole forces. The potential energy between two

dipoles can be calculated by summing up the Coulomb potential energy between each of the four charges. Recall that the Coulomb potential energy is given by

$$V(r) = \frac{q_1 q_2}{4\pi\epsilon_0 r} \quad (1.3)$$

where  $r$  is the distance between charges  $q_1$  and  $q_2$  and  $\epsilon_0$  is the vacuum permittivity.

Considering two parallel dipoles, the potential can be shown to vary as  $1/r^3$ . However, if the dipoles are freely rotating, the potential varies as  $1/r^6$ . Further details of the derivations of these functional forms are provided by Atkins (1998). Here we have only discussed the dependence of the potential on  $r$ ; all prefactors are omitted. This type of relationship is an example of a scaling law, discussed in more detail in Section 1.7.

Most molecules are non-polar. It is evident, however, that there must be attractive van der Waals interactions between such molecules in order that condensed phases, such as those exhibited by liquid hydrogen or argon at low temperature, can exist. Molecules without a permanent dipole moment can possess an instantaneous dipole moment due to fluctuations in the atomic electron distribution. These fluctuating dipoles can induce dipoles which create a transient electric field that can polarize nearby molecules, leading to an induced dipole. Such induced dipole–induced dipole forces create dispersion interactions, also known as London interactions. It is again found that the potential varies as  $1/r^6$ . In other words, for both freely rotating dipole–dipole and induced dipole–induced dipole interactions, the attractive potential takes the form

$$V(r) = -\frac{C}{r^6} \quad (1.4)$$

although the term  $C$  is different for the two types of interaction (further details are provided by Atkins, 1998, for example). This explains why the attractive contribution to the total potential is often taken to have the  $1/r^6$  form, as in the Lennard–Jones (12,6) potential (Eq. 1.2) for example.

Coulombic forces dominate other interactions in systems containing ions. This is because the Coulombic potential energy falls off much more slowly (as  $1/r$ , Eq. 1.1) than any dipole–dipole interaction. A typical Coulombic potential energy is  $\sim 250 \text{ kJ mol}^{-1}$ , whereas a van der Waals energy is about  $1 \text{ kJ mol}^{-1}$  or less.

An important distinction can be made between materials in which the structure comes from intermolecular ordering and those for which it is produced by the ordering of molecular aggregates. Many soft materials, such as colloids and micellar amphiphiles, belong to the latter class. A necessary condition for the formation of such aggregates is the existence of at least two components in the system. Often the second component is water and then *hydrogen bonding* interactions are important. In fact, hydrogen bonding is predominantly a type of dipole–dipole interaction, although there may also be some covalent character. For amphiphiles in solution, the *hydrophobic effect* drives the formation of micelles. The hydrophobic effect originates in the local structuring of water, which consists of a tetrahedral arrangement of hydrogen-bonded molecules. When an insoluble species such as a hydrocarbon is added to the water, this structure has to accommodate itself around each molecule, which produces a reduction in entropy. This is known as the hydrophobic effect. This structuring effect is reduced when the molecules assemble into micelles. The hydrophobic effect is discussed further in Section 4.6.5. We note here that since the hydrophobic effect has its origin in the entropy associated with local hydrogen bonding of water molecules, it ultimately depends on dipole–dipole forces.

Even in systems where structure results from molecular self-assembly into aggregates, it is forces between molecules that drive the self-assembly process, although these can be between molecules of different types. In one-component systems such as thermotropic liquid crystals, ordering can only result from forces between molecules of the same type. It is difficult to make a quantitative statement about the precise form of the potential for any soft material, other than observ-

ing that it will be some combination of repulsive short-ranged contributions and attractive long-range contributions.

### 1.3 STRUCTURAL ORGANIZATION

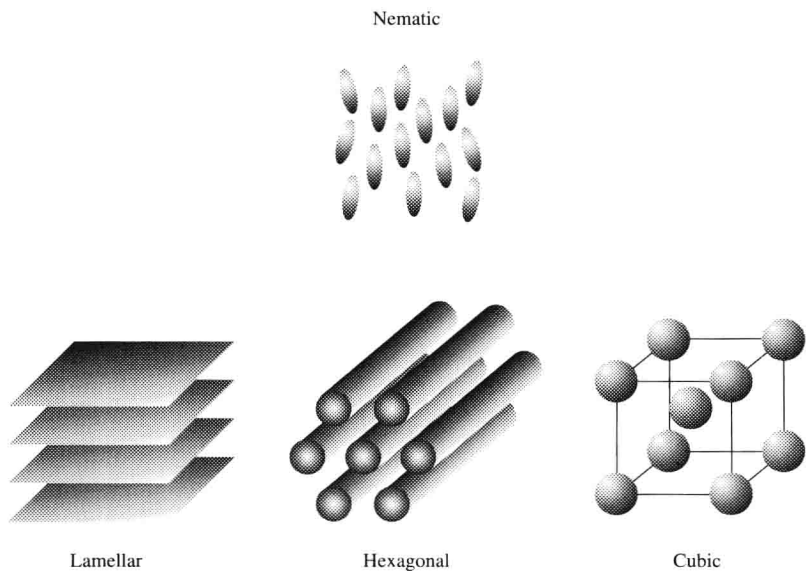
There are both common and distinct features in the ordering of different types of soft material. The most important feature in common is that the ordering is generally intermediate between that of a crystalline solid and that of a liquid. This lack of crystalline order leads to the 'soft' mechanical response of the materials. There may, however, be partial translational and/or orientational order of molecules due to the formation of a mesophase by a thermotropic liquid crystal or an amphiphile in water. Polymer melts and solutions are also classified as 'soft materials', although there is no long-range translational or orientational order. However, these phases are distinguished from conventional liquids due to their high viscosity and/or viscoelasticity. The lack of long-range translational order can be expressed in another way: soft material structures are characterized by numerous defects, for example lattice dislocations or disclinations in liquid crystals (discontinuities in orientational order, Section 5.4.1). These defects have a profound effect on flow behaviour.

Another feature common to the ordering of soft materials is the periodicity of the structures formed, typically in the range 1–1000 nm, which corresponds to 'nanoscale' ordering. Another term often employed is 'mesoscopic' ordering. This originates because the length-scale of the structures is intermediate between the microscopic (atomic) and macroscopic scales.

The number of symmetry groups of possible mesophases is restricted. Many types of soft material form structures of the same symmetry, although the molecular ordering may differ. The nematic phase (Section 5.5.2) possesses no long-range translational order, i.e. the molecular order is locally liquid-like. However, there is long-range orientational order

(Fig. 1.2). Nematic phases are formed by particles ranging from small organic molecules ( $\sim 2\text{--}3$  nm long), such as those used in liquid crystal displays, up to long macromolecules, such as rod-like tobacco mosaic virus ( $\sim 300$  nm long).

The simplest structure with translational order is a one-dimensional layered structure (Fig. 1.2). In thermotropic liquid crystals, there are a number of such smectic phases formed by molecules in a weakly layered arrangement (Section 5.2.2). Amphiphiles also form smectic phases, but they are usually



**Figure 1.2** Examples of ordering in soft materials. A nematic liquid crystal has no long-range translational order, but the molecules (here shown as ellipses) are orientationally ordered. The lamellar phase has one-dimensional translational order, the hexagonal phase two-dimensional translational order and cubic phases three-dimensional orientational order. The layers in the lamellar phase can be formed from molecules (smectic phase) or amphiphilic bilayers. A hexagonal structure can be formed by disc-like molecules (then being termed columnar phase) or rod-like micelles. The cubic phase shown here is formed by spherical micelles. Bicontinuous cubic structures are also found (see Fig. 4.25d)



called lamellar phases. Here, amphiphile bilayers alternate with layers of solvent (Section 4.10.2). Smectic layered structures are also found in clays, i.e. mineral-based colloidal dispersions.

Phases with two-dimensional translational order are found for both thermotropic and lyotropic liquid crystals, being termed columnar phases for thermotropic liquid crystals and hexagonal phases for lyotropic materials (Fig. 1.2). There is only partial orientational and translational order of molecules within these aggregates. This lower level of molecular order produces a 'softer' structure than for hexagonal phases formed by simple molecules or atoms. The hexagonal micellar phase formed by amphiphiles in solution is much softer than graphite, the structure of which is based on a hexagonal arrangement of covalently bonded atoms. The forces between molecules within rod-like micelles and those between amphiphilic molecules and solvent molecules are both much weaker than those involved in covalent bonding and the structure is much less tightly held together. In addition, the van der Waals forces act over a longer range, so that the structural periodicity is much larger. Hexagonal phases are also formed in concentrated solutions of biological macromolecules such as DNA.

Structures with three-dimensional translational order include micellar cubic phases (Fig. 1.2) and bicontinuous cubic phases. These are distinguished topologically (Section 4.9). Micelles are discrete, closed objects within a matrix of solvent. In bicontinuous structures, space is divided into two continuous labyrinths. For lyotropic liquid crystal phases, cocontinuous water channels are divided from each other by a surfactant membrane in one type of bicontinuous structure (in the other, the positions of water and surfactant are reversed). These cubic phases are, on symmetry grounds, crystalline solids. However, unlike atomic or molecular crystals, they are built from supermolecular aggregates, i.e. micelles or surfactant membranes. Thus, as for hexagonal structures, these phases are softer than their atomic/molecular analogues, which are held together by shorter-range forces. Structures with one-, two- and three-dimensional order are also formed