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# **HEAT AND THERMODYNAMICS**

**An Intermediate Textbook**

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**Sixth Edition**

**Mark W. Zemansky, Ph.D.**

**Richard H. Dittman, Ph.D.**

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An Intermediate Textbook

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Sixth Edition

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## **HEAT AND THERMODYNAMICS**

### **INTERNATIONAL STUDENT EDITION**

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# PREFACE

Early textbooks on "heat" devoted many chapters to discussions of thermometry, calorimetry, and heat engines, included many experimental details, and ended with one or two chapters in which an attempt was made to construct a deductive theory, known as "thermodynamics." In these two divisions only the large-scale characteristics of matter were considered, so that both divisions were strictly "macroscopic." In later years, when molecular theory was better understood, the subject matter of statistical mechanics and of kinetic theory was included in the field. Since these two subjects are microscopic in point of view, a more general term was needed to include the four divisions: heat, thermodynamics, statistical mechanics, and kinetic theory. The term most widely used today for this purpose is "thermal physics." Of course, there is no hard and fast rule concerning the relative weights of each of the divisions of thermal physics. Some authors regard statistical mechanics and kinetic theory of primary importance, with heat and thermodynamics a somewhat necessary evil. Others, feeling guilty about their worship of statistical mechanics, hide behind the misnomer "statistical thermodynamics," which seems to refer to a subject that is both microscopic and macroscopic at the same time.

In the present volume, thermodynamics constitutes about 50 percent, heat about 37 percent, statistical mechanics about 10 percent, and kinetic theory about 3 percent. The main reason for this distribution is the deep conviction on the part of the authors that the fundamental foundation of the subject is thermodynamics, which is well within the abilities of undergraduate students. At the sophomore or junior level students have sufficient physical and mathematical sophistication to prepare them for thermodynamic arguments and proofs, whereas they are not quite ready for the subtleties of ergodic theory or of Gibbsian ensembles. Only the simplest treatment of weakly interacting particles is given and applied to an ideal gas, an electron gas, blackbody radiation, a vibrating lattice, and a paramagnetic-ion subsystem in a crystal. This sixth edition contains about the same amount of engineering, chemistry, and experimental detail as its

predecessor, but the subjects of superfluidity and superconductivity have been deleted, on the ground that their treatment is no longer exclusively thermodynamic.

The two main features of this sixth edition are: (1) the almost complete use of SI units in all parts of the subject, with the exception of a few topics in chemical thermodynamics; and (2) the subdivision of the book into two almost-equal sections, the first part being devoted to fundamental concepts, designed to be the core of an introductory course in thermodynamics, and the second part, starting with a chapter on elementary statistical mechanics, designed to enable the teacher to choose those applications which require the use of thermodynamics and statistical mechanics, such as specific heats of solids, cryogenics, nuclear paramagnetism, and negative temperatures, to name a few. Part 2 also contains such topics as chemical equilibrium, ideal-gas reactions, phase theory, the third law, fuel cells, thermocouples, blackbody radiation, and negative Kelvin temperatures.

The authors would like to express their appreciation of the expertise, understanding, and kindness displayed by the McGraw-Hill staff in the preparation of this book—particularly Marian Provenzano and Scott Amerman. The endpapers contain eighteen pictures of world-famous pioneers in thermodynamics and statistical mechanics. The authors are very grateful to Professor Peter T. Landsberg of Southampton University and to Joan Warnow of the American Institute of Physics for supplying us with these pictures.

Mark W. Zemansky  
Richard H. Dittman

# NOTATION

## CAPITAL ITALIC

- A** Area; paramagnetic heat-capacity constant
- B** Second virial coefficient; Brillouin function
- C** Heat capacity; critical point
- D** Debye function; electric displacement
- E** Electric intensity; energy
- F** Helmholtz function
- G** Gibbs function
- H** Enthalpy
- I** Current; nuclear quantum number
- J** Electronic quantum number
- K** Thermal conductivity; equilibrium constant
- L** Length; latent heat; coupling coefficients
- M** Magnetization; mass
- N** Number of molecules
- P** Pressure
- Q** Heat

## LOWERCASE ITALIC

- a** A dimension;  $g\mu_B\mu_0\mathcal{H}/kT$
- b** A dimension; a constant
- c** Molar heat capacity; speed of light
- d** Differential sign
- e** Napierian logarithm base; electronic charge
- f** Molar Helmholtz function; variance
- g** Molar Gibbs function; Landé  $g$  factor; degree of degeneracy
- h** Molar enthalpy; Planck's constant
- i** Vapor-pressure constant
- j** Valence
- k** Boltzmann's constant
- l** Latent heat per kilogram or per mole
- m** Mass of a molecule or electron
- n** Number of moles; quantum number
- p** Partial pressure; momentum
- q** Heat per mole

$R$	Universal gas constant; electric resistance; radius	$r$	Radius; number of individual reactions
$S$	Entropy	$s$	Molar entropy
$T$	Kelvin temperature	$t$	Celsius temperature; empirical temperature
$U$	Internal energy	$u$	Molar energy; radiant-energy density
$V$	Volume	$v$	Molar volume
$W$	Work	$w$	Speed of a wave or a molecule
$X$	Generalized displacement	$x$	Space coordinate; mole fraction
$Y$	Generalized force; Young's modulus	$y$	Space coordinate; fraction
$Z$	Electric charge; partition function; compressibility factor	$z$	Space coordinate

## SCRIPT CAPITALS

$\mathcal{B}$	Magnetic induction
$\mathcal{E}$	Electromotive force
$\mathcal{F}$	Tension; force
$\mathcal{H}$	Magnetic intensity
$\mathcal{M}$	Molar mass or molecular weight
$\mathcal{R}$	Radiant exitance
$\mathcal{S}$	Surface tension

## ROMAN SYMBOLS FOR UNITS

m	meter
kg	kilogram
s	second
atm	atmosphere
A	ampere
A/m	ampere turn per meter
C	coulomb
Hz	hertz (cps)
J	joule
N	newton
Pa	Pascal
T	tesla
V	volt
W	watt

## SPECIAL SYMBOLS

$N_A$	Avogadro's number
$d$	Inexact differential
$N_F$	Faraday's constant
$T^*$	Magnetic temperature
$C_C$	Curie constant

## GREEK LETTERS

$\alpha$	Linear expansivity; critical-point exponent
$\beta$	Volume expansivity; $1/kT$ ; critical-point exponent
$\gamma$	Ratio of heat capacities; electronic term in heat capacity; critical-point exponent
$\Omega$	Thermodynamic probability; solid angle
$\delta$	Energy of a magnetic ion; critical-point exponent
$\Delta$	Finite difference
$\epsilon$	Degree of reaction; molecular energy; reduced temperature difference; Seebeck coefficient
$\eta$	Efficiency



$\theta$	Ideal-gas temperature; angle	$\pi$	Peltier coefficient
$\Theta$	Debye temperature	$\rho$	Density (mass per unit volume)
$\kappa$	Compressibility	$\sigma$	Thomson coefficient; Stefan-Boltzmann constant; function for isentropic surface
$\lambda$	Wavelength; Lagrange multiplier; integrating factor	$\tau$	Time; period
$\mu$	Joule-Kelvin coefficient; molecular magnetic moment; chemical potential	$\phi$	Angle; function of temperature
$\mu_0$	permeability of vacuum	$\varphi$	Number of phases
$\nu$	Molecular density; frequency; stoichiometric coefficient	$\omega$	Coefficient of performance; angular speed
$\Pi$	Polarization	$\chi$	Magnetic susceptibility



James F. Joule  
1818-1890



Hermann L. F. von Helmholtz  
1811-1894



Robert Peltier  
1814-1881



William Thomson  
1824-1907



Gustav Kirchhoff  
1824-1887



Lord Kelvin  
1824-1907





*Robert Boyle*  
1627-1691



*Benjamin Thompson Count  
Rumford* 1753-1814



*Nicolas Léonard  
Sadi Carnot* 1796-1832



*James P. Joule*  
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*Albert Einstein  
1879-1955*



*Peter Debye  
1884-1966*



*Francis E. Simon  
1893-1956*

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PART  
**ONE**

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FUNDAMENTAL CONCEPTS