

G. Slavcheva  
P. Roussignol  
*Editors*

NANOSCIENCE AND TECHNOLOGY

# Optical Generation and Control of Quantum Coherence in Semiconductor Nanostructures

---



Springer

Gabriela Slavcheva  
Philippe Roussignol  
(Editors)

# Optical Generation and Control of Quantum Coherence in Semiconductor Nanostructures

With 137 Figures



 Springer

*Editors*

Dr. Gabriela Slavcheva  
Imperial College London  
Blackett Laboratory  
Prince Consort Road  
SW7 2AZ London  
United Kingdom  
g.slavcheva@imperial.ac.uk

Professor Philippe Roussignol  
Ecole Normale Supérieure  
Laboratoire Pierre Aigrain  
24, rue Lhomond  
75231 Paris CEDEX 05  
France  
philippe.roussignol@lpa.ens.fr

*Series Editors:*

Professor Dr. Phaedon Avouris  
IBM Research Division  
Nanometer Scale Science & Technology  
Thomas J. Watson Research Center  
P.O. Box 218  
Yorktown Heights, NY 10598, USA

Professor Dr. Bharat Bhushan  
Ohio State University  
Nanotribology Laboratory  
for Information Storage  
and MEMS/NEMS (NLIM)  
Suite 255, Ackerman Road 650  
Columbus, Ohio 43210, USA

Professor Dr. Dieter Bimberg  
TU Berlin, Fakultät Mathematik/  
Naturwissenschaften  
Institut für Festkörperphysik  
Hardenbergstr. 36  
10623 Berlin, Germany

Professor Dr., Dres. h.c. Klaus von Klitzing  
Max-Planck-Institut  
für Festkörperforschung  
Heisenbergstr. 1  
70569 Stuttgart, Germany

Professor Hiroyuki Sakaki  
University of Tokyo  
Institute of Industrial Science  
4-6-1 Komaba, Meguro-ku  
Tokyo 153-8505, Japan

Professor Dr. Roland Wiesendanger  
Institut für Angewandte Physik  
Universität Hamburg  
Jungiusstr. 11  
20355 Hamburg, Germany

NanoScience and Technology    ISSN 1434-4904  
ISBN 978-3-642-12490-7    e-ISBN 978-3-642-12491-4  
DOI 10.1007/978-3-642-12491-4  
Springer Heidelberg Dordrecht London New York

Library of Congress Control Number: 2010929186

© Springer-Verlag Berlin Heidelberg 2010

This work is subject to copyright. All rights are reserved, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, reuse of illustrations, recitation, broadcasting, reproduction on microfilm or in any other way, and storage in data banks. Duplication of this publication or parts thereof is permitted only under the provisions of the German Copyright Law of September 9, 1965, in its current version, and permission for use must always be obtained from Springer. Violations are liable to prosecution under the German Copyright Law.

The use of general descriptive names, registered names, trademarks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

Cover design: eStudio Calamar S.L.

Printed on acid-free paper

Springer is part of Springer Science+Business Media ([www.springer.com](http://www.springer.com))

# NANO SCIENCE AND TECHNOLOGY

---

# NANO SCIENCE AND TECHNOLOGY

---

*Series Editors:*

P. Avouris B. Bhushan D. Bimberg K. von Klitzing H. Sakaki R. Wiesendanger

The series NanoScience and Technology is focused on the fascinating nano-world, mesoscopic physics, analysis with atomic resolution, nano and quantum-effect devices, nano-mechanics and atomic-scale processes. All the basic aspects and technology-oriented developments in this emerging discipline are covered by comprehensive and timely books. The series constitutes a survey of the relevant special topics, which are presented by leading experts in the field. These books will appeal to researchers, engineers, and advanced students.

Please view available titles in *NanoScience and Technology* on series homepage  
<http://www.springer.com/series/3705/>

*To Marta and Metodi Slavchev*

# Preface

The fundamental concept of quantum coherence plays a central role in quantum physics, cutting across disciplines of quantum optics, atomic and condensed matter physics. Quantum coherence represents a universal property of the quantum systems that applies both to light and matter thereby tying together materials and phenomena. Moreover, the optical coherence can be transferred to the medium through the light-matter interactions. Since the early days of quantum mechanics there has been a desire to control dynamics of quantum systems. The generation and control of quantum coherence in matter by optical means, in particular, represents a viable way to achieve this longstanding goal and semiconductor nanostructures are the most promising candidates for controllable quantum systems. Optical generation and control of coherent light-matter states in semiconductor quantum nanostructures is precisely the scope of the present book.

Recently, there has been a great deal of interest in the subject of quantum coherence. We are currently witnessing parallel growth of activities in different physical systems that are all built around the central concept of manipulation of quantum coherence. The burgeoning activities in solid-state systems, and semiconductors in particular, have been strongly driven by the unprecedented control of coherence that previously has been demonstrated in quantum optics of atoms and molecules, and is now taking advantage of the remarkable advances in semiconductor fabrication technologies.

A recent impetus to exploit the coherent quantum phenomena comes from the emergence of the quantum information paradigm. The scientific effort in this field is focussed on how to exploit the properties of the quantum systems to perform computations. The issues in computation theory are fascinating and recent progress has generated a great deal of excitement. Furthermore, in recent years, a new paradigm focussed on the exploitation of the previously largely ignored spin degree of freedom, has emerged. Spin offers the opportunity to store and manipulate phase coherence over much larger length and time scales than is typically possible in charged-based devices. In this respect, the idea of encoding the quantum information in the spin degree of freedom has been particularly promising and extensively investigated. Furthermore, spin can be accessed through the orbital properties of the electron in

solid state, which in turn can be efficiently manipulated by light according to angular momentum conservation laws, through the optical orientation mechanism. An all-optical implementation of quantum coherent spin control in semiconductor nanostructures, is of particular interest since it takes full advantage of the cutting edge ultrafast laser technologies and enables the implementation of ultrafast schemes for quantum computation.

Although quantum information is undoubtedly a worthy and useful goal in its own right, many more conventional and near-term problems ranging from novel lasers to spintronics are all bound up with issues in coherence. Historically, the quest for the demonstration of fundamental coherent quantum-optical effects in semiconductor systems that have been initially observed in atomic systems has proved to be very successful and has enormous potential for applications. For instance, the idea of achieving Bose-Einstein condensation in solid state at elevated temperatures originates from the cold atom field and was proposed more than 40 years ago. The recent experimental discovery of the room-temperature polariton lasing and the superfluid properties of exciton-polaritons in semiconductor microcavities have opened up new and exciting opportunities for tangible applications of the quantum coherent phenomena of the Bose-Einstein condensation and superfluidity. On the other hand, the exploitation of coherent optical effects, such as electromagnetically-induced transparency and coherent population trapping in semiconductor systems opens up pathways to freeze light in future devices and to build an inversionless laser. This is yet another demonstration of a fruitful transfer of ideas built around the concept of coherence from cold atoms field to the solid state. Although the atomic and semiconductor physical systems are very different, from conceptual and theoretical point of view there are many cognate issues between atomic coherence and the coherence of relatively simple many-body systems such as excitons or exciton-polaritons in semiconductors. The study of these more controllable systems is extremely helpful to interpret and guide work on complex materials with their innumerable confounding issues.

The main focus of this book is the study of the optical manipulation of the coherence in excitonic, polaritonic, and spin systems as model systems for complex coherent semiconductor dynamics, towards the goal of achieving quantum coherence control in the solid-state. The book is intended for graduate students, postdocs and active researchers in the fields of semiconductor quantum optics, nonlinear and coherent ultrafast optical spectroscopies, quantum information processing and quantum computation, semiconductor spintronics, and for physicists and engineers, who want to become familiar with recent experimental and theoretical advances in this frontier research field.

The book provides a selection of review articles written by leading scientists, focusing on various aspects of optically-induced quantum coherence in semiconductor nanostructures. The latest research findings, interpretation and ideas in this rapidly developing field are discussed in four parts: (i) Carrier dynamics in quantum dots; (ii) Optically-induced spin coherence in quantum dots; (iii) Novel systems for coherent spin manipulation, and (iv) Coherent light-matter states in semiconductor microcavities.

Finally, we would like to thank the authors for their enthusiastic response, dedication and full support of the book project until its successful completion. We wish to express our gratitude to R. Murray, E. Clarke, P. Spencer, M. Taylor and E. Harbord for fruitful discussions, providing assistance and valuable feedback on the manuscript. In addition, we are very much indebted to Angela Lahee of Springer-Verlag whose continuous guidance and help during the course of the project were invaluable. Special thanks are due to our families for their encouragement, appreciation and continuous support.

London, United Kingdom  
Paris, France

*G. Slavcheva*  
*Ph. Roussignol*  
January, 2010

# List of Contributors

**Vollrath Martin Axt**

Theoretische Physik III, Universität Bayreuth, 95440 Bayreuth, Germany.

e-mail: [Martin.Axt@uni-bayreuth.de](mailto:Martin.Axt@uni-bayreuth.de)

**Gérald Bastard**

Laboratoire Pierre Aigrain, Ecole Normale Supérieure and CNRS, 24 rue Lhomond  
F-75005 Paris, France.

e-mail: [gerald.bastard@lpa.ens.fr](mailto:gerald.bastard@lpa.ens.fr)

**Manfred Bayer**

Experimentelle Physik 2, Technische Universität Dortmund, D-44221 Dortmund,  
Germany.

e-mail: [manfred.bayer@tu-dortmund.de](mailto:manfred.bayer@tu-dortmund.de)

**Guillaume Cassabois**

Ecole Normale Supérieure, Laboratoire Pierre Aigrain, 24 rue Lhomond 75231  
Paris Cedex 5, France.

e-mail: [guillaume.cassabois@lpa.ens.fr](mailto:guillaume.cassabois@lpa.ens.fr)

**Edmund Clarke**

Blackett Laboratory, Imperial College London,  
Prince Consort Road,

London SW7 2AZ, United Kingdom.

e-mail: [edmund.clarke@imperial.ac.uk](mailto:edmund.clarke@imperial.ac.uk)

**Sophia E. Economou**

US Naval Research Lab, Washington DC 20375, USA.

e-mail: [economou@bloch.nrl.navy.mil](mailto:economou@bloch.nrl.navy.mil)

**Robson Ferreira**

Laboratoire Pierre Aigrain, Ecole Normale Supérieure and CNRS, 24 rue Lhomond  
F-75005 Paris, France.

e-mail: robson.ferreira@lpa.ens.fr

**Thomas Grange**

Walter Schottky Institut, Technische Universität München,  
85748 Garching, Germany.

e-mail: Thomas.Grange@wsi.tum.de

**Alex Greilich**

Experimentelle Physik 2, Technische Universität Dortmund, D-44221 Dortmund,  
Germany.

e-mail: agreilich@gmail.com

**Michał Grochol**

Institut für theoretische Physik, Universität Erlangen-Nürnberg, Germany.

e-mail: michal.grochol@physik.uni-erlangen.de

**Edmund Harbord**

Blackett Laboratory, Imperial College London,  
Prince Consort Road,  
London SW7 2AZ, United Kingdom.

e-mail: edmund.harbord@gmail.com

**Jonathan Keeling**

Cavendish Laboratory, University of Cambridge, United Kingdom.

e-mail: jmk2@cam.ac.uk

**Eric M. Kessler**

Max-Planck-Institut für Quantenoptik Garching, Germany.

e-mail: eric.kessler@mpq.mpg.de

**Tilmann Kuhn**

Institut für Festkörpertheorie, Westfälische Wilhelms-Universität Münster,  
Wilhelm-Klemm-Str. 10, 48149 Münster, Germany.

e-mail: Tilmann.Kuhn@uni-muenster.de

**Le Si Dang**

Equipe Mixte, Institut Néel, CEA-CNRS-Université Joseph Fourier, 25 rue des Martyrs, F-38042 Grenoble, France.

e-mail: lesidang@grenoble.cnrs.fr

**Peter Littlewood**

Cavendish Laboratory, University of Cambridge, United Kingdom.

e-mail: pb121@cam.ac.uk

**Ray Murray**

Blackett Laboratory, Imperial College London,  
Prince Consort Road,  
London SW7 2AZ, United Kingdom.

e-mail: r.murray@imperial.ac.uk

**Carlo Piermarocchi**

Department of Physics and Astronomy, Michigan State University, East Lansing,  
Michigan 48824, USA.

e-mail: piermaro@msu.edu

**Stefano Portolan**

CEA/CNRS/UJF Joint Team "Nanophysics and Semiconductors" Institut Néel,  
CNRS BP 166, 25 rue des Martyrs, 38042 Grenoble Cedex 9, France

e-mail: stefano.portolan@grenoble.cnrs.fr

**Thomas L. Reinecke**

US Naval Research Lab, Washington DC 20375, USA.

e-mail: reinecke@nrl.navy.mil

**Doris E. Reiter**

Institut für Festkörpertheorie, Westfälische Wilhelms-Universität Münster,  
Wilhelm-Klemm-Str. 10, 48149 Münster, Germany.

e-mail: Doris.Reiter@uni-muenster.de

**Maxime Richard**

Equipe Mixte, Institut Néel, CEA-CNRS-Université Joseph Fourier, 25 rue des  
Martyrs, F-38042 Grenoble, France.

e-mail: maxime.richard@grenoble.cnrs.fr

**Philippe Roussignol**

Laboratoire Pierre Aigrain, Ecole Normale Supérieure and CNRS, 24 rue Lhomond,  
75231 Paris Cedex 5, France.

e-mail: philippe.roussignol@lpa.ens.fr

**Salvatore Savasta**

Dipartimento di Fisica della Materia e Ingegneria Elettronica,  
Università di Messina, Salita Sperone 31, I-98166 Messina, Italy  
e-mail: Salvatore.Savasta@unime.it

**Gabriela Slavcheva**

Blackett Laboratory, Imperial College  
London, Prince Consort Road,  
London SW7 2AZ, United Kingdom.  
e-mail: g.slavcheva@imperial.ac.uk

**Marzena H. Szymańska**

Department of Physics, University of Warwick, United Kingdom.  
e-mail: M.H.Szymanska@warwick.ac.uk

**Michiel Wouters**

ITP, Ecole Polytechnique Fédérale de Lausanne (EPFL), Station 3, 1015 Lausanne,  
Switzerland.  
e-mail: michiel.wouters@epfl.ch

**Dmitri R. Yakovlev**

Experimentelle Physik 2, Technische Universität Dortmund, D-44221 Dortmund,  
Germany.  
e-mail: dmitri.yakovlev@tu-dortmund.de

# Contents

<b>1</b>	<b>Introduction</b>	1
	Gabriela Slavcheva and Philippe Roussignol	
<b>Part I Carrier dynamics in quantum dots</b>		
<b>2</b>	<b>Decoherence of intraband transitions in InAs quantum dots</b>	9
	Thomas Grange, Robson Ferreira and Gérald Bastard	
2.1	Introduction	9
2.2	Electronic states of self-organized quantum dots	10
2.3	Magneto-polaron states in charged QDs	12
2.4	Anharmonic decay of polaron states	14
2.5	Time resolved studies of pure dephasing in QDs	16
2.6	Conclusion	22
	References	23
<b>3</b>	<b>Spectral diffusion dephasing and motional narrowing in single semiconductor quantum dots</b>	25
	Guillaume Cassabois	
3.1	Introduction	25
3.2	Theory	26
3.2.1	Random telegraph noise	27
3.2.2	Gaussian stochastic noise	28
3.3	Experiments	29
3.3.1	Unconventional motional narrowing	30
3.3.2	Voltage-controlled conventional motional narrowing	32
3.4	Conclusion	34
	References	35

**Part II Optically-induced spin coherence in quantum dots**

<b>4 Carrier spin dynamics in self-assembled quantum dots</b> . . . . .	39
Edmund Clarke, Edmund Harbord and Ray Murray	
4.1 Introduction . . . . .	40
4.2 Growth and optical properties of In(Ga)As/GaAs QDs . . . . .	41
4.3 Spin generation and detection . . . . .	46
4.4 Spin relaxation and dephasing mechanisms in QDs . . . . .	48
4.5 Outlook . . . . .	54
References . . . . .	55
<b>5 Optically induced spin rotations in quantum dots</b> . . . . .	63
Sophia E. Economou and Thomas L. Reinecke	
5.1 Introduction . . . . .	63
5.2 Useful concepts . . . . .	65
5.2.1 Spin state as vector on Bloch sphere . . . . .	65
5.2.2 Composite rotations . . . . .	65
5.3 rf control of spin in quantum dots . . . . .	66
5.4 Optical control of spin in quantum dots . . . . .	67
5.4.1 Energy levels and selection rules . . . . .	68
5.4.2 Optical spin rotations . . . . .	69
5.5 Optical spin rotation proposals . . . . .	71
5.5.1 Optical Stark effect based rotation . . . . .	71
5.5.2 Adiabatic approaches to spin rotation . . . . .	71
5.5.3 Hyperbolic secant based rotations . . . . .	72
5.6 Outlook . . . . .	79
Appendix . . . . .	79
5.6.1 Fidelity . . . . .	79
5.6.2 Coherent Population Trapping . . . . .	80
References . . . . .	82
<b>6 Ensemble spin coherence of singly charged InGaAs quantum dots</b> . .	85
Alex Greilich, Dmitri R. Yakovlev and Manfred Bayer	
6.1 Introduction . . . . .	85
6.2 Experimental technique . . . . .	88
6.3 Exciton fine structure . . . . .	91
6.3.1 Fine structure of heavy-hole exciton . . . . .	91
6.3.2 Linear dichroism in longitudinal magnetic field . . . . .	93
6.3.3 Circular dichroism in transverse magnetic field . . . . .	94
6.3.4 Spectral dependence of the electron g-factor . . . . .	95
6.3.5 Anisotropy of electron g-factor in quantum dot plane . .	96
6.4 Generation of spin coherence . . . . .	97
6.5 Mode-locking of spin coherence . . . . .	100
6.5.1 Spin coherence time of an individual electron . . . . .	101
6.5.2 Mechanism of spin synchronization . . . . .	102
6.5.3 Tailoring of ensemble spin precession . . . . .	104

6.5.4	Temperature dependence of electron spin coherence time	108
6.6	Nuclei induced frequency focusing	109
6.7	Collective single-mode precession	115
6.8	Ultrafast optical spin rotation	119
6.9	Conclusions	125
	References	125

### Part III Novel systems for coherent spin manipulation

<b>7</b>	<b>Optically controlled spin dynamics in a magnetically doped quantum dot</b>	131
	Doris E. Reiter, Tilmann Kuhn and Vollrath M. Axt	
7.1	Introduction	132
7.2	Model System of a single dot doped with a single Mn atom	133
7.3	Spin flip in the heavy hole exciton system using $\pi$ and $2\pi$ pulses	136
7.4	Switching into all Mn spin states	140
7.4.1	Switching into spin eigenstates	140
7.4.2	Measurement by pump probe spectroscopy	143
7.4.3	Switching into superposition states	145
7.5	Magnetic field in Voigt configuration	146
7.6	Conclusions	149
	References	149
<b>8</b>	<b>Coherent magneto-optical activity in a single carbon nanotube</b>	151
	Gabriela Slavcheva and Philippe Roussignol	
8.1	Introduction	152
8.2	Problem Formulation	154
8.2.1	Dielectric response function of an isolated SWCNT	157
8.2.2	Optical dipole matrix element for circularly polarised light	158
8.3	Theoretical framework for the natural optical activity	159
8.4	Simulation results for the natural optical activity	163
8.5	Magneto-optical activity of a chiral SWCNT in an axial magnetic field	171
8.5.1	Theoretical model of the nonlinear Faraday rotation in an axial magnetic field	172
8.5.2	Simulation results for Faraday rotation	176
8.6	Conclusions	178
	References	179
<b>9</b>	<b>Exciton and spin coherence in quantum dot lattices</b>	181
	Michał Grochol, Eric M. Kessler, and Carlo Piermarocchi	
9.1	Introduction	182
9.2	Theory	183
9.2.1	Neutral quantum dot lattice	183
9.2.2	Charged quantum dot lattice	191

9.2.3	Neutral quantum dots in lattice of optical cavities . . . . .	194
9.3	Results and discussion . . . . .	199
9.3.1	Neutral quantum dot lattice . . . . .	199
9.3.2	Charged quantum dot lattice . . . . .	203
9.3.3	Neutral quantum dots in lattice of cavities . . . . .	205
9.4	Conclusions . . . . .	210
	References . . . . .	210

## Part IV Coherent light-matter states in semiconductor microcavities

<b>10</b>	<b>Quantum optics with interacting polaritons</b> . . . . .	215
	Stefano Portolan and Salvatore Savasta	
10.1	Introduction . . . . .	216
10.2	Electronic excitation in semiconductor . . . . .	217
10.3	Linear and nonlinear dynamics . . . . .	222
10.4	Entangled photon pairs from the optical decay of biexcitons . . . . .	229
10.5	The picture of interacting polaritons . . . . .	231
10.6	Noise and environment: Quantum Langevin approach . . . . .	234
10.7	Quantum complementarity of cavity polaritons . . . . .	243
10.8	Coherent Trapping . . . . .	248
10.9	Spin-entangled cavity polaritons . . . . .	250
10.10	Emergence of entanglement out of a noisy environment: The case of microcavity polaritons . . . . .	251
10.10.1	Coherent and incoherent polariton dynamics . . . . .	252
10.10.2	Results . . . . .	256
10.11	Outlook . . . . .	260
	References . . . . .	260
<b>11</b>	<b>Spontaneous coherence within a gas of exciton-polaritons in Telluride microcavities</b> . . . . .	265
	Maxime Richard, Michiel Wouters and Le Si Dang	
11.1	Introduction . . . . .	266
11.2	Formation and steady state of a polariton gas . . . . .	267
11.3	Momentum distribution, polariton thermalization . . . . .	269
11.4	Similarities and differences between polariton condensation, polariton lasing and conventional photon lasing . . . . .	270
11.5	Spatial properties . . . . .	272
11.5.1	Gross-Pitaevskii equation . . . . .	272
11.5.2	Small size condensate . . . . .	274
11.5.3	Polariton condensate in disordered environment . . . . .	275
11.6	Vortices in polariton condensates . . . . .	278
11.6.1	Quantized vortices . . . . .	279
11.6.2	Half-quantized vortices . . . . .	282
11.7	Correlations within a degenerate polaritons gas . . . . .	283
11.7.1	Spatial first order correlations . . . . .	283
11.7.2	Number fluctuations in a polariton condensate . . . . .	285