

Applied Statistics for Economists

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Preface

Economists have used empirical information to understand economic phenomena for many years. While economic data, and the statistical methods for evaluating it, are increasingly sophisticated, the basic reason for using such evidence remains the same – learning about an economy by systematically measuring economic activity.

The following text presents quantitative methods frequently used by economists to gain such understanding. The methods examined are divided into two categories – descriptive statistics used to measure individual economic variables, and statistical inference used to measure relationships between economic variables and to test hypotheses about them. In addition to demonstrating how to generate a numerical result with each method, the current text applies each method to specific and contemporary economic questions. The text also provides detailed economic interpretations of the statistical results, a feature missing from virtually every current text, and it explains the strengths and limitations associated with each method. The goal is for students to learn to “do” empirical economics as they work through the text.

The text was initially developed as class notes for a course in quantitative methods in economics and grew out of a dissatisfaction with the scope and emphasis in existing textbooks. Many currently available texts, designed for business and economics courses in statistics, focus primarily on business examples, rarely using actual data for economic variables and seldom discussing questions of interest to economists. A second group of texts focuses on econometric analysis, an important statistical tool in economics, but certainly not the only quantitative method useful to economists.

Most contemporary texts also emphasize the mechanics of generating statistical measures, but provide little on the important questions of economic interpretation and economic application of the methods. As a result, students may gain technical knowledge from such an emphasis, but, when it comes to conducting their own economic research, they may not fully understand how the methods can be applied to their own research, nor can they always accurately interpret the statistical results generated. The current text attempts to bridge this gap.

Textbooks for statistical methods in economics have not always been so focused. Several years ago, I found a used copy of Harold W. Guthrie’s *Statistical Methods in Economics* (Richard D. Irwin, Homewood, IL, 1966). Guthrie’s book, like contemporary texts, provided instruction on how to use a wide range of quantitative methods, but it did more than that: it used actual economic data in most examples and, most importantly, it provided economic interpretations of the empirical results generated. The text also emphasized the appropriate, and inappropriate, use of statistics and quantitative methods in economics, another feature sometimes given short shrift in contemporary textbooks.

Guthrie's book inspired the class notes that evolved into the current text. While substantially different, it is my hope that the current text retains the clarity, accessibility, and applicability of Guthrie's text. I also want today's students to better understand, as those who used Guthrie's text surely did, the empirical dimensions of contemporary economic problems and how quantitative methods can increase our understanding of them. Indeed, to put a twist on an old economic adage, theory without measurement can lead us to conclusions that have little basis in reality.

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December 2010

A note on the textbook's focus and scope

This textbook is designed for undergraduate students of economics who have completed an introductory course in statistics. While we review key findings from probability theory, sampling theory, and probability distribution functions in Part III, the purpose is to apply these concepts to hypothesis testing of sample means, correlation analysis, and regression analysis. Students without the prerequisite statistics course may find this discussion too brief and require additional study in basic statistics.

The economic questions raised throughout the text are based on the assumption that students have completed courses in micro- and macroeconomic theory, and that they have acquired some sophistication in applying economic theory to economic issues. Since it is the goal for students to learn these methods so they can conduct empirical analysis, this background is crucial. The text is thus pitched to students in the second half of their undergraduate education in economics.

The text also contains detailed instructions at the end of each chapter for using Microsoft Excel 2007/2010 to apply the quantitative methods described. While those familiar with dedicated statistical software may find Excel's tools less efficient, the widespread use and availability of Excel recommends its use here.

As economists know, economic statistics are governed by detailed definitions that can vary significantly across nations. Thus the text uses data primarily from the United States (reflecting the author's background), although the economic variables measured here are available for most economies. For those unfamiliar with a data series, the text will include information about who collects the data and how the data is constructed. Those wanting additional information can access the agency responsible, where detailed handbooks of methods and other information can be found.

A note on the “Where can I find. . .?” boxes

These boxes, found throughout the text, provide information about several popular locations for online economic data. Online accessibility has greatly facilitated empirical economic analysis, much as the development of computing power and the availability of statistical software has transformed such work.

The growing and widespread availability of economic data necessarily means much more information is available than can be recorded in this book. While each data source is current as of its writing, it is possible that some details, or even the web address itself, may have changed. (Readers are directed to use a search engine if forwarding links are not provided.)

Information is also increasingly available through the agencies that generate the data. It is recommended that students first visit the agency responsible for a particular data series to see if it is available and easily downloadable from that source.

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