

Encyclopedia

of
Fluid Mechanics

VOLUME 7

Rheology and
Non-Newtonian
Flows

52.7073
EJ.6

Encyclopedia of Fluid Mechanics

VOLUME 7

Rheology and Non-Newtonian Flows

N. P. Cheremisinoff, Editor

in collaboration with

R. Agarwal
J. Berlamont
B. H. Bersted
A. F. Borghesani
M. J. Brekner
J. F. Céspedes B.
R. P. Chhabra
J. T. Chung
Y. Cohen
R. Darby
D. DeKee
J. F. Dijkman
A. Duduković
K. Funatsu
E. R. Harrell

S. I. Harris
C. K. Kiang
T. Kajiwaru
D. K. Kalyon
W. Kozicki
A. K. Kulshreshtha
C. Kureta
P. J. R. Leblond
M. F. Letelier S.
G. H. Michler
N. Nakajima
A. Nakayama
K. Ogawa
V. O. Popadić
M. B. Powley

P. W. Savenije
A. Schneider
J. R. Scholtens
H. Sebastian
V. Shenoy
J. Stastna
K. Takahashi
P. N. Tandon
M. N. Tekić
C. Tiu
P. H. T. Uhlherr
G. Verreet
K. C. Wilson

Encyclopedia of Fluid Mechanics

VOLUME 7

Rheology and Non-Newtonian Flows

Library of Congress Cataloging-in-Publication Data

(Revised for vol. 7)

Encyclopedia of fluid mechanics.

Includes bibliographies and indexes.

Contents: v. 1. Flow phenomena and measurement—
v. 2. Dynamics of single-fluid flows and mixing—[etc.]
— v. 7. Rheology and non-Newtonian flow.

1. Fluid mechanics—Dictionaries. I. Cheremisinoff,
Nicholas P.

TA357.E53 1986 620.1'06 85-9742

Series ISBN 0-87201-492 4

Copyright © 1988 by Gulf Publishing Company, Houston,
Texas. All rights reserved. Printed in the United States of America. This book, or parts thereof, may not be reproduced in any
form without permission of the publisher.

ISBN 0-87201-540-8

CONTRIBUTORS TO THIS VOLUME

- R. Agarwal, Department of Mathematics, Harcourt Butler Technological Institute, Kanpur, India.
- J. Berlamont, Laboratorium Voor Hydraulica, Katholieke Universiteit te Leuven, Heverlee, Belgium.
- B. H. Bersted, Amoco Chemicals Company, Naperville, Illinois, USA.
- A. F. Borghesani, Dipartimento di Fisica "G. Galilei" Università di Padova and G.N.S.M./C.I.S.M., Padova, Italy.
- M.-J. Brekner, Research and Development Informationstechnik-Division, Hoechst AG, Kalle Wiesbaden, Federal Republic of Germany.
- J. F. Céspedes B., Department of Mechanical Engineering, University of Santiago, Chile, Casilla 10233, Santiago, Chile.
- N. P. Cheremisinoff, Exxon Chemical Company, Linden, New Jersey, USA.
- R. P. Chhabra, Department of Chemical Engineering, Indian Institute of Technology, Kanpur, India.
- J. T. Chung, Haake Buchler Instruments, Inc., Saddle Brook, New Jersey, USA.
- Y. Cohen, Department of Chemical Engineering, University of California, Los Angeles, California, USA.
- R. Darby, Department of Chemical Engineering, Texas A&M University, College Station, Texas, USA.
- D. DeKee, Department of Chemical Engineering, University of Windsor, Windsor, Ontario, Canada.
- J. F. Dijkman, Philips Research Laboratories, Eindhoven, The Netherlands.
- A. Duduković, Institute for Petrochemistry, Gas, Oil and Chemical Engineering, Faculty of Technology, University of Novi Sad, Novi Sad, Yugoslavia.
- K. Funatsu, Department of Chemical Engineering, Kyushu University, Fukuoka, Japan.
- E. R. Harrell, BF Goodrich Company, Technical Center, Avon Lake, Ohio, USA.
- S. L. Harris, Department of Chemical Engineering, Clarkson University, Potsdam, New York, USA.
- C. R. Huang, Department of Chemical Engineering, Chemistry & Environmental Science, New Jersey Institute of Technology, Newark, New Jersey, USA.
- T. Kajiwara, Department of Chemical Engineering, Kyushu University, Fukuoka, Japan.
- D. M. Kalyon, Department of Chemistry and Chemical Engineering, Stevens Institute of Technology, Castle Point, Hoboken, New Jersey, USA.
- W. Kozicki, Department of Chemical Engineering, University of Ottawa, Ottawa, Ontario, Canada.

- A. K. Kulshreshtha, Department of Mathematics, Harcourt Butler Technological Institute, Kanpur, India.
- C. Kuroda, Research Laboratory of Resources Utilization, Tokyo Institute of Technology, Yokohama, Japan.
- P. J. R. Leblans, DSM Research, Geleen, The Netherlands.
- M. F. Letelier S., Department of Mechanical Engineering, University of Santiago, Casilla, Santiago, Chile.
- G. H. Michler, Wissenschaftliches Forschungs- und Koordinierungszentrum im Kombinat VEB Chemische Werke Buna, Schkopau and Institut für Festkörperphysik und Elektronenmikroskopie der Akademie der Wissenschaften der DDR, German Democratic Republic.
- N. Nakajima, Polymer Engineering Center, University of Akron, Akron, Ohio, USA.
- A. Nakayama, Department of Energy and Mechanical Engineering, Shizuoka University, Hamamatsu, Japan.
- K. Ogawa, Department of Chemical Engineering, Tokyo Institute of Technology, Tokyo, Japan.
- V. O. Popadić, Faculty of Technology, University of Novi Sad, Novi Sad, Yugoslavia.
- M. B. Powley, Department of Chemical Engineering, University of Windsor, Windsor, Ontario, Canada.
- E. P. W. Savenije, Philips Research Laboratories, Eindhoven, The Netherlands.
- H. A. Schneider, Institute of Macromolecular Chemistry, Albert-Ludwigs University of Freiburg, Federal Republic of Germany.
- B. J. R. Scholtens, DSM Research, Geleen, The Netherlands.
- D. H. Sebastian, Department of Chemical Engineering and Polymer Processing Institute, Stevens Institute of Technology, Castle Point, Hoboken, New Jersey, USA.
- A. V. Shenoy, Department of Materials Science and Engineering, University of Florida, Gainesville, Florida, USA.
- J. Stastna, Department of Chemical Engineering, University of Windsor, Windsor, Ontario, Canada.
- K. Takahashi, Department of Chemical Engineering, Yamagata University, Yonezawa, Japan.
- P. N. Tandon, Department of Mathematics, Harcourt Butler Technological Institute, Kanpur, India.
- M. N. Tekić, Faculty of Technology, University of Novi Sad, Novi Sad, Yugoslavia.
- C. Tiu, Department of Chemical Engineering, Monash University, Clayton, Victoria Australia.
- P. H. T. Uhlherr, Department of Chemical Engineering, Monash University, Clayton, Victoria, Australia.
- G. Verreet, Laboratorium Voor Hydraulica, Katholieke Universiteit te Leuven, Heverlee, Belgium.
- K. C. Wilson, Department of Civil Engineering, Queen's University at Kingston, Ontario, Canada.

ABOUT THE EDITOR

Nicholas P. Cheremisinoff heads the product development group in the Polymers Technology Division of Exxon Chemical Company. Dr. Cheremisinoff has extensive experience and research interests in multiphase and rheologically complex flows. He received his B.S., M.S., and Ph.D. degrees in chemical engineering from Clarkson College of Technology, and he is a member of a number of professional societies including Tau Beta Pi and Sigma Xi.

in memory

A final acknowledgment belongs to my beloved mother, Louise, whose efforts in no small way contributed to this entire series. Beyond the typing services provided for many of the contributors and meticulous effort of volume indexing, she was and still remains the Editor's major source of inspiration.

PREFACE

This volume of the Encyclopedia is devoted to the subjects of rheology and flow dynamics of non-Newtonian fluids. Although related topics are treated in previous volumes, prior subject coverage was specific to the generic flow topics of those volumes. This work attempts to provide a unified treatment of practical rheology and industrial handling/processing of rheologically complex fluids.

Non-Newtonian behavior is encountered in an overwhelming number of situations throughout nature and in commercial operations. Examples where such behavior occurs are industrial waste flows; process slurry operations; the manufacture of dies, inks, pigments, and paints; polymer and plastics synthesis and fabrication; preparation of cosmetics and health care products; food processing; and even biological phenomena such as blood flow and coagulation. In fact, nature, along with mankind's capitalization of nature in industry, offers many more examples of rheologically complex materials than those described by rigorous Newtonian mechanics. Despite this over-abundance of encounters, our theoretical foundations and process design methodology are largely empirical, and often drawn by analogy from specific fluid studies.

The present work attempts to provide a unified treatment of the subjects starting from an advanced entry level. Fundamental concepts and properties of viscous flow behavior are presented in Volumes 1, 2, 5, and 6 of this series. This volume provides only an overview of basic principles and directs detailed attention to state-of-the-art topics in handling/processing viscous materials. The work is organized into three sections. Section I contains twelve chapters aimed at phenomenological description and establishing theoretical development of non-Newtonian flow behavior. Discussions and modeling of flow regimes in symmetric and non-symmetric flow systems are discussed. The relations between viscous behavior and transport properties are presented. Section II contains five chapters addressing the topics of slippage and drag phenomena. These behaviors are major properties but are often least understood in practical process operations. The final section contains eighteen chapters on characterization, behavior, and processing of polymers and elastomeric materials. Polymer technology is perhaps the most advanced in terms of our understanding of viscous flow properties, and although principles discussed evolved from the study of these materials, concepts and design methodology are general. There are three main themes in this section, namely (1) the relationships between the molecular structure of the fluid and its deformation properties, (2) industrial handling operations, including design methodology, and (3) techniques for assessing and predicting the behavior of viscous materials in industrial processing equipment.

This work represents the efforts of 44 researchers/practitioners from around the world. In addition, it reflects the opinions of scores of colleagues who provided invaluable suggestions and critiques. Deepest gratitude is extended to the contributors and to Gulf Publishing Company whose efforts are presented herein.

Nicholas P. Cheremisinoff

ENCYCLOPEDIA OF FLUID MECHANICS

VOLUME 1: FLOW PHENOMENA AND MEASUREMENT

Transport Properties and Flow Instability
Flow Dynamics and Frictional Behavior
Flow and Turbulence Measurement

VOLUME 2: DYNAMICS OF SINGLE-FLUID FLOWS AND MIXING

Channel and Free Surface Flows
Mixing Phenomena and Practices
Fluid Transport Equipment

VOLUME 3: GAS-LIQUID FLOWS

Properties of Dispersed and Atomized Flows
Flow Regimes, Hold-Up, and Pressure Drop
Reactors and Industrial Applications

VOLUME 4: SOLIDS AND GAS-SOLIDS FLOWS

Properties of Particulates and Powders
Particle-Gas Flows
Fluidization and Industrial Applications
Particulate Capture and Classification

VOLUME 5: SLURRY FLOW TECHNOLOGY

Slurry and Suspension Flow Properties
Unit Operations of Slurry Flows

VOLUME 6: COMPLEX FLOW PHENOMENA AND MODELING

Transport Phenomena and Hydrodynamics of Complex Flows
Transport Phenomena in the Environment
Advanced Modeling Techniques for Complex Flows

VOLUME 7: RHEOLOGY AND NON-NEWTONIAN FLOWS

Flow Dynamics and Transport Phenomena
Slippage and Drag Phenomena
Polymer Rheology and Processing

VOLUME 8: AERODYNAMICS AND COMPRESSIBLE FLOWS

Turbulence Phenomena and Modeling
Selected Engineering Problems

VOLUME 9: POLYMER FLOW ENGINEERING

**VOLUME 10: SUBSURFACE AND GROUNDWATER FLOW
PHENOMENA**

VOLUME 11: GAS DYNAMICS AND PLASMA FLOWS

VOLUME 12: ADVANCED NUMERICAL FLOW MODELING

CONTENTS

CONTRIBUTORS TO THIS VOLUME	ix
<i>(For a note about the editor, please see page xi)</i>	

PREFACE	xii
---------------	-----

SECTION I: FLOW DYNAMICS AND TRANSPORT PHENOMENA

1. Characterization of Thixotropic Fluids	3
<i>C. R. Huang</i>	
2. Laminar and Turbulent Pipe Flows of Non-Newtonian Fluids .	19
<i>R. Darby</i>	
3. Laminar Unsteady Flow of Elementary Non-Newtonian Fluids in Long Pipes	55
<i>M. F. Letelier S. and J. F. Céspedes B.</i>	
4. Non-Newtonian Flow Behavior of Coal-Fuel Oil Suspensions .	89
<i>A. F. Borghesani</i>	
5. Rheology and Non-Newtonian Behavior of Sea and Estuarine Mud	135
<i>G. Verreet and J. Berlamont</i>	
6. Velocity and Velocity Gradient in Turbulent Viscoelastic Pipe Flow	151
<i>C. Kuroda and K. Ogawa</i>	
7. The Flow of Newtonian and Non-Newtonian Liquids through Annular Converging Regions	173
<i>J. F. Dijksman and E. P. W. Savenije</i>	
8. Parametric Modeling of Flow Geometries in Non-Newtonian Flows	199
<i>W. Kozicki and C. Tiu</i>	

9. Hydrodynamics of Bubbles and Drops in Rheologically Complex Liquids 253
R. P. Chhabra
10. Natural Convection Heat Transfer to Viscoelastic Fluids 287
A. V. Shenoy
11. Integral Methods for Forced Convection Heat Transfer in Power-Law Non-Newtonian Fluids 305
A. Nakayama
12. Analogies Between Momentum, Heat and Mass Transfer in Dilute Polymer Solutions 341
A. Duduković

SECTION II: SLIPPAGE AND DRAG PHENOMENA

13. Stress Measurement of Viscoelastic Fluids by Flow Birefringence Technique and Slip Phenomena of Polymer Melts 359
K. Funatsu and T. Kajiwara
14. Apparent Slip Flow of Polymer Solutions 407
Y. Cohen
15. Rheological Study of Laminar-Turbulent Transition in Drag-Reducing Polymeric Solutions 459
P. N. Tandon, A. K. Kulshreshtha, and R. Agarwal
16. Turbulent Flow Velocity Profiles in Drag-Reducing Fluids ... 479
A. V. Shenoy
17. Mechanisms of Drag Reduction in Turbulent Non-Newtonian Pipeline Flow 505
K. C. Wilson

SECTION III: POLYMER RHEOLOGY AND PROCESSING

18. Determination of Morphology and Mechanical Microprocesses in Polymers 527
G. H. Michler

19. Constitutive Analysis of the Nonlinear Viscoelastic Properties in Simple Extension of Polymeric Fluids and Networks: A Comparison	555
<i>P. J. R. Leblans and B. J. R. Scholtens</i>	
20. Modeling Complex Viscosity as a Response Function	581
<i>J. Stastna, D. DeKee, and M. B. Powley</i>	
21. Static Equilibrium and Motion of Spheres in Viscoplastic Liquids	611
<i>R. P. Chhabra and P. H. T. Uhlherr</i>	
22. Effects of Long Chain Branching on Polymer Rheology	635
<i>B. H. Bersted</i>	
23. Rheology of Highly Filled Polymer Melt Systems	667
<i>A. V. Shenoy</i>	
24. Analyzing Steady-State Flow of Elastomers	703
<i>N. Nakajima and E. R. Harrell</i>	
25. Temperature Dependence of Local Flow in Polymers	725
<i>M.-J. Brekner and H. A. Schneider</i>	
26. Principles of Polymer Mixing and Extrusion	761
<i>N. P. Cheremisinoff</i>	
27. Mixing of Non-Newtonian Liquids with Helical Ribbon Impellers	867
<i>K. Takahashi</i>	
28. Mixing in Continuous Processors	887
<i>D. M. Kalyon</i>	
29. Computer Modeling and Analysis of Extrusion Operations ..	927
<i>D. H. Sebastian</i>	
30. Control of Single Screw Extrusion	953
<i>S. L. Harris</i>	
31. Practical Applications of Rheology to Polymer Processing ...	961
<i>A. V. Shenoy</i>	

32. Rheological Characterization and Processability Testing	991
<i>N. P. Cheremisinoff</i>	
33. Fundamentals of Polymer Materials	1061
<i>J. T. Chung</i>	
34. Torque Rheometer Technology and Instrumentation	1081
<i>J. T. Chung</i>	
35. Coating Using Pseudoplastic Liquids	1141
<i>M. N. Tekić and V. O. Popadić</i>	
INDEX	1165

SECTION I

FLOW DYNAMICS AND TRANSPORT PHENOMENA

CONTENTS

CHAPTER 1.	CHARACTERIZATION OF THIXOTROPIC FLUIDS,	3
CHAPTER 2.	LAMINAR AND TURBULENT PIPE FLOWS OF NON-NEWTONIAN FLUIDS,	19
CHAPTER 3.	LAMINAR UNSTEADY FLOW OF ELEMENTARY NON-NEWTONIAN FLUIDS IN LONG PIPES,	55
CHAPTER 4.	NON-NEWTONIAN FLOW BEHAVIOR OF COAL-FUEL OIL SUSPENSIONS,	89
CHAPTER 5.	RHEOLOGY AND NON-NEWTONIAN BEHAVIOR OF SEA AND ESTUARINE MUD,	135
CHAPTER 6.	VELOCITY AND VELOCITY GRADIENT IN TURBULENT VISCOELASTIC PIPE FLOW,	151
CHAPTER 7.	THE FLOW OF NEWTONIAN AND NON-NEWTONIAN LIQUIDS THROUGH ANNULAR CONVERGING REGIONS,	173
CHAPTER 8.	PARAMETRIC MODELING OF FLOW GEOMETRIES IN NON-NEWTONIAN FLOWS,	199
CHAPTER 9.	HYDRODYNAMICS OF BUBBLES AND DROPS IN RHEOLOGICALLY COMPLEX LIQUIDS,	253
CHAPTER 10.	NATURAL CONVECTION HEAT TRANSFER TO VISCOELASTIC FLUIDS,	287
CHAPTER 11.	INTEGRAL METHODS FOR FORCED CONVECTION HEAT TRANSFER IN POWER-LAW NON-NEWTONIAN FLUIDS,	305
CHAPTER 12.	ANALOGIES BETWEEN MOMENTUM, HEAT AND MASS TRANSFER IN DILUTE POLYMER SOLUTIONS,	341

CHAPTER 1

CHARACTERIZATION OF THIXOTROPIC FLUIDS

Ching-Rong Huang

Department of Chemical Engineering, Chemistry & Environmental Science
New Jersey Institute of Technology
Newark, New Jersey, USA

CONTENTS

INTRODUCTION, 3

- Rheological Classification of Fluid Behavior, 3
- History of Thixotropy, 4
- Experimental Measurements of Thixotropy, 4
- Currently Accepted Definition of Thixotropy, 5

QUANTITATIVE CHARACTERIZATION OF THIXOTROPY, 5

- Phenomenological Approach, 5
- Theoretical Approach, 7

THIXOTROPIC FLUIDS, 13

- Organic Suspensions, 13
- Inorganic Suspensions, 13
- Oils, 13
- Coal-Water Slurries, 14
- Foodstuffs, 14
- Whole Blood, 14

CONCLUSION, 15

NOTATION, 15

REFERENCES, 16

INTRODUCTION

Rheological Classification of Fluid Behavior

Rheology is the science of deformation and flow of materials in response to stress. A rheological equation describes or relates stress or deformation to flow variables of materials such as strain, shear rate, and time. Fluids can be conveniently classified based on their rheological properties as follows [1, 2]: (a) Newtonian fluids follow the simplest rheological equation of Newton's law of viscosity, the stress being proportional to the shear rate. The flow curve (shear stress vs. shear rate) shows a linear relationship and passes through the origin. (b) Time-independent non-Newtonian fluid exhibits a non-linear relationship between the shear stress and the shear rate, or its flow curve exhibits a yield stress (not passing through the origin), provided its viscosity is not time dependent. Time-independent non-Newtonian fluids have attracted more attention by rheologists than others. More than fifteen rheological equations or models have been proposed to represent the time-independent relation as summarized by Skelland [2]. These equations employ two to five parameters to describe the pseudoplastic (shear thinning) or the dilatant (shear thickening) properties of time-independent non-Newtonian fluids with or without a yield stress. (c) Time-dependent non-

4 Flow Dynamics and Transport Phenomena

Newtonian fluids display time-dependent behavior in the flow curve in addition to the shear-rate dependency. Therefore, the viscosity of time-dependent non-Newtonian fluids is a function of both the shear rate and the time of shearing. They are usually subdivided into two groups, thixotropic fluids and rheopectic fluids. The former are shear-thickening time-dependent fluids. (i) Viscoelastic fluids possess the viscous property of a liquid and the elastic property of a solid. Thus the rheological properties of viscoelastic fluids are inadequately described by relationships between the shear stress and the shear rate unless the elastic properties of the stress and the strain are included. The simplest rheological equation for viscoelastic fluid is the Maxwell model, which includes two rheological parameters—the viscosity and the rigidity modulus. Various theories of viscoelasticity have resulted in many differential or integral constitutive equations relating the shear stress with shear rate, strain, and time.

History of Thixotropy

“Thixotropy” was introduced by Freundlich in 1928 [3]. He and his co-workers observed that many colloidal solutions show a decreased resistance to flow upon being stirred or shaken and revert to their original resistance after being allowed to stand still [4]. He suggested that this phenomenon was due to the structural change of the colloidal particles—a reversible, isothermal gel-sol transition through mechanical disturbance. This reversible, isothermal, viscosity decrease phenomenon was called thixotropy.

The term “thixotropy” has been in continuous use to the present time by many investigators. However, Freundlich’s original definition was not uniformly adhered to. It was sometimes interpreted as pseudoplastic or shear-thinning property without considering the time-dependent behavior. Others used it to represent the non-linear viscoelasticity of fluids, failing to recognize the inelastic property of thixotropic fluids.

Experimental Measurements of Thixotropy

The qualitative detection of thixotropy can be achieved experimentally. Capillary viscometers are not suitable for the study of shear rate and time dependencies of viscosity of thixotropic fluids due to the varying shear rate in the flowing system. Both cone-and-plate type and Couette-type viscometers are commonly used. Common proposed experiments are as follows:

The hysteresis loop. Shear stress is monitored in response to shear-rate variation. The shear rate is linearly increased from zero to a maximum value and then decreased from this maximum value to zero. This experiment, originally employed by Green and Weltman [5], generates a hysteresis loop on the flow curve. The hysteresis loop has been used ever since as one of the characteristic curves for the identification of a thixotropic fluid. This experiment is modified into three other experiments: (a) A multiple hysteresis loop is obtained from the continuation of cycles of the shear-rate increase and decrease [6]. The progressive breakdown of gel-structure of the fluid induced by shear can be observed by the gradual reduction of the area enclosed in hysteresis loops. The enclosed area eventually becomes zero and the flow curve of the fluid behaves as a pseudoplastic fluid. (b) A multiple hysteresis is measured with a finite period of pause between cycles. The pause between cycles will establish the necessary rest time required by the fluid to regain its gel-sol equilibrium condition. (c) Another modified hysteresis loop is obtained. When the shear-rate half cycle reaches the maximum value, it is held at this rate for a period of time before returning to zero.

The stress-decay curve. The time-dependent effect on shear stress at constant shear rate is measured, until a steady-state shear stress is reached. This experiment, first designed by Pryce-Jones with a Couette viscometer, demonstrates the time-dependency of viscosity of various thixotropic fluids [7]. This experimentally observed curve is referred to as the stress-decay curve or the torque-decay curve, and is another characteristic curve of thixotropic fluid. This experiment with a step function of shear rate can be replaced by an alternate experiment with a multiple-step function of shear rates from high to low values. It results in a series of stress-decay curves while shear rates