JOHN I. GRIFFIN

STATISTICS

METHODS AND APPLICATIONS

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Methods and Applications

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Preface

In 1869 Adolphe Quetelet, who merged the methods of political economy, mathematics, and government statistics into one powerful tool for investigating social phenomena, which we now call statistics, drew up a list of 180 different definitions of the term statistics. Even today, statisticians define the area of their professional interest and competence in different ways. The very extent of statistics makes it difficult to define. It is both a science and an art. It is a vital branch of scientific method. It is widely used in most sciences, business, government, and ordinary life. The early statisticians, who calculated the probabilities associated with games of chance and who developed the theory of errors of observation, could not visualize the extent to which statistical methods would become an indispensable part of the intellectual equipment of an educated man.

This text is designed to accomplish two major purposes, which complement each other. Within the established curriculums of American colleges and universities, formal training in statistics for most students is limited to one course, consisting of one or two semesters. The burden imposed upon the instructor in such a course is heavy, indeed. He has the responsibility not only of instruction in specific techniques but more particularly of conveying to the student a sense of the exciting new developments in statistics and the contributions which the science of statistics can make to the student's life as scientist, business manager, government administrator, and, not least of all, as citizen. This text seeks to show the student that statistics is a rapidly growing subject, fast developing a philosophy and body of techniques as far removed from the endless masses of descriptive statistics, "Die Tabellen Statistik," as the flintlock is from the I.C.B.M. The text provides the student with a body of specific techniques he can apply immediately to problems which he encounters in his college courses and which will be relevant to his subsequent life experience.

This text is divided into twenty chapters and seven appendixes, and provides sufficient material for a one-year course in statistics. The emphasis is general so that students majoring in business, economics, or any of the social sciences will find the illustrative material familiar. This is not a text in business statistics or economic statistics but in statistics. The distinction is an important one, since the objective of this text is to introduce the student to statistics rather than to particular subjectmatter problems. The illustrative data, however, are real data taken from sources reflecting research in fields of direct subject-matter interest to the students. Thus, not only are techniques illustrated but also something is learned about the types of

data with which statisticians are concerned. In this manner, methods and applications are learned at the same time.

The twenty chapters of this text are so arranged that the major aspects of modern statistics are presented in a logical sequence, and the chapters should be studied in sequence. A one-semester course should provide sufficient time to cover about fourteen of the chapters, omitting all of Chapters 9, 12, 15, 16, 19, and 20. Depending upon the particular interests of the students, a choice may be made between the chapters dealing with Sampling Methods in Auditing, Statistical Quality Control in Production and Management, and Statistical Methods in Forecasting and Market Research. In all chapters the level of mathematical sophistication is such as to make a professional mathematician quite unhappy, but it is assumed, realistically I believe, that not much mathematical competence beyond secondary school algebra can be taken for granted. It is important that the student does not become self-conscious about mathematical formulas and realizes that mathematical notation is merely a shorthand and not an end in itself. Occupational specialization in the statistical field, as elsewhere, results in a distinction between those who are able to develop path-breaking new theories and those who are competent in the understanding and application of the existing body of scientific knowledge. This book is not addressed to those in the first category. Its objectives are much more modest.

Several features of this text may be pointed out, which should facilitate effective use by students. The chapters are divided into numbered sections, and cross references to material throughout the book are always made by reference to the section number. The statistical tables in Appendix F are keyed to the sections in which the proper use of the particular table is discussed and illustrated. Throughout the chapters boldface type has been employed to call attention to a new term, which is defined at that point in the book. Thus, a student may review the essential technical vocabulary by noting the terms in bold face. In each chapter a number of signals—have been inserted. These signals indicate that the student should turn to the self-reviewing workbook which is now available for use with this text. This separately available workbook not only performs the usual functions of a workbook but is also a self-instruction tool prepared on the basis of the new techniques of programmed learning. A kit of ten transparent slides, suitable for use on an overhead projector, has been prepared from the illustrations in this text, and instructors interested in this type of visual instruction should communicate with the publisher.

The frequent references to the great names in the history of statistical science are designed to give the student some acquaintance with the "founding fathers." It seems to me that the teaching of a concept can be made more effective if the student associates the concept with the scientist who developed it. On the new frontiers of the science, such as decision theory, my approach has been essentially conservative. That is, the newer methods of analysis are not presented as in conflict with the principles underlying the traditional theory of Neyman and Pearson. In a sense all statistics is concerned with decision making and not just special applications. The precise position to be occupied by some of the newer work in decision theory in the

entire body of general statistical methods is not completely clear at this time. The best preparation for further intensive work in decision theory in its applications to management and public policy is, in my opinion, a good understanding of accepted theory and practice as developed in the post Karl Pearsonian period.

The sources of data, tables, and concepts are given in the text and in the acknowledgments. If I have inadvertently adopted material without specific recognition of its source, I can only plead that every author of an introductory text-book is in debt to all his predecessors. My greatest obligation is to my students, who, during the past two decades, have challenged my ability to show them the power and excitement of modern statistics. For those to whom statistics has appealed as a professional career, I hope that the foundation has proven sound and that, in like fashion, many readers of this text will rapidly outgrow this book.

J. I. G.

New York, N. Y. January, 1962

Acknowledgments

In the preparation of a general text in statistics intended for an introductory course for students with no special training in mathematics, it is necessary to draw upon many illustrations of the application of statistical methods made by government agencies and business firms. The generosity with which permission has been granted to reproduce illustrative material is acknowledged with gratitude. The many examples drawn from federal government documents are indicated by the source note identifying the department of issue. The individual statisticians in the several agencies have been most kind in providing materials. The general obligation of the author to the specialists in the field of statistics, as well as to previous writers of text-books, is suggested, although not capable of detailed specification, by the list of references in Appendix E, which lists those books and articles that have been of major importance in shaping the author's approach to the subject of statistics.

Specific obligations for permission to reproduce materials are due to the Sanborn Map Company for the map which is used as the endpaper at the front of this book. Professor Herbert Arkin has given permission to reproduce certain new tables which he has prepared; these are Appendix Tables F-2, F-3, F-15, F-16, and F-17. Mr. Steve A. Demakopoulos, of the Remington Rand Division of Sperry Rand Corporation, ran on a UNIVAC the time series problem used in Chapter 18. Other machine companies that generously provided material are the International Business Machines Corporation, Royal McBee Corporation, and the Monroe Calculating Machine Company, Inc. Professor E. S. Pearson kindly granted permission to reproduce certain tables from Biometrika Tables for Statisticians, reproduced as Appendix Tables F-12 and F-19 and as Charts 10-2, 10-3, 14-4, and 14-5. The Biometrika trustees have granted permission to reproduce the illustration of the Quincunx in Chapter 8 and "Student's" illustrations in Section 6.5. Professor M. S. Bartlett has given permission to reproduce Appendix Table F-13 which shows selected pages from Tracts for Computers No. 26. Chart 13-5 is reproduced from Introduction to the Theory of Statistics by G. U. Yule and M. G. Kendall, Charles Griffin & Co., Ltd., by permission of author and publishers. Professor Maurice G. Kendall and Charles Griffin & Co., Ltd. have granted permission to reproduce Chart 17-7 from The Advanced Theory of Statistics. The author is indebted to Professor Sir Ronald A. Fisher, F.R.S., Cambridge, to Dr. Frank Yates, F.R.S., Rothamsted, and to Messrs. Oliver & Boyd, Ltd., Edinburgh, for permission to reprint Table VII from their book Statistical Tables for Biological, Agricultural and Medical Research; also to Professor Fisher to quote from his book Design of Experiments the extract in Section 2.6.

xiv----Acknowledgments

The American Management Association has given permission to use the material "What's Ahead? The Gentle Art of Business Forecasting," prepared by Al Hormel and Lydia Strong, which is reproduced as Chart 18-1. The American Society for Testing and Materials has given permission to reproduce Appendix Table F-21 as well as the Standard Recommended Practice statement, reprinted in full in Section 9.7. These ASTM Standards are under constant surveillance by technical committees and are subject to change, to keep abreast of changes in technology; the Standard Recommended Practice in respect to probability sampling was made Standard in 1961.

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When I consider a single state, I discern a vast number of things actually to be found therein. Among them are some which concern obviously its prosperity either in obstructing it or contributing to it. Such things we might call "Staatsmerkwürdigkeiten" (the remarkable things of the state). The totality of these "Staatsmerkwürdigkeiten" of a kingdom or a republic, makes up its constitution in the broadest sense, and the account of such constitutions of one or more states is "statistik."

GOTTFRIED ACHENWALL, 1749

Statistics can give us three kinds of knowledge: (1) Statistics give us knowledge which can be obtained by mere enumeration or by a succession of enumerations. (2) Statistics, in the course of these enumerations, often betray certain fixed relations which have the character of natural laws. (3) Statistics are sometimes able to trace relations of cause and effect which can be ascertained in no other way.

RICHMOND MAYO SMITH, 1888

The conception of statistics as the study of variation is the natural outcome of viewing the subject as the study of populations; for a population of individuals in all respects identical is completely described by a description of any one individual, together with the number in the group. The populations which are the object of statistical study always display variation in one or more respects. To speak of statistics as the study of variation also serves to emphasize the contrast between the aims of modern statisticians and those of their predecessors.

RONALD AYLMER FISHER, 1925

Contents

	Preface	ix
	Acknowledgments	xiii
	Acknowledgments List of Tables List of Charts Why Statistics? 1.1 Statistics Defined 1 1.2 The Origins of Statistics 3 1.3 Statistics in the Social Sciences 5 1.4 Econometrics and Statistics 6 1.5 Statistics in Business 7 1.6 The Statistical View of Nature 9 Design of Statistical Investigations 2.1 The Role of Statistical Intelligence 13 2.2 The Design of a Statistical Program 15 2.3 Census-Type Surveys 18 2.4 The 1960 Census 22 2.5 Planning and Executing Sampling Surveys 25 2.6 The Design of Experiments 28 Data Processing 3.1 From Babbage to Electronic Data Processing 30 3.2 Use of the Desk Calculator 33 3.3 Edge Punch Cards 37 3.4 Punched Card Methods 42 3.5 Elements of a Computing System 47 3.6 Programming a Computer 49 3.7 The Impact of Computer Technology on Statistics 55	xxi
	List of Charts	xxii
1.	Why Statistics?	1
	1.2 The Origins of Statistics 3	
	1.4 Econometrics and Statistics 6	
	1.6 The Statistical View of Nature 9	
2.	Design of Statistical Investigations	13
	 2.2 The Design of a Statistical Program 15 2.3 Census-Type Surveys 18 2.4 The 1960 Census 22 2.5 Planning and Executing Sampling Surveys 25 	
3.	Data Processing	30
	 3.2 Use of the Desk Calculator 33 3.3 Edge Punch Cards 37 3.4 Punched Card Methods 42 3.5 Elements of a Computing System 47 3.6 Programming a Computer 49 	
4.	Organizing Univariate Data	58
	4.1 Observations and Variables 584.2 Populations and Samples 60	

xvi-	Conte	nts	
	4.3	Reduction of Data by Classification 65	
	4.4	Frequency Distributions in Tabular Form 67	
	4.5	Graphic Presentation of Frequency Distributions 75	
	4.6	Common Types of Frequency Distributions 83	
5.	Avera	ges	87
	5.1	Criteria for a Satisfactory Average 87	
	5.2	The Arithmetic Mean 88	
	5.3	Computational Methods Using Coding 91	
		Order Statistics, the Median, and Other Quantiles 94	
	5.5	The Mode 96	
	5.6	Comparative Characteristics of Averages 97	
	5.7	Graphic Methods for Estimating Averages 100	
6.	Measu	res of Variation	104
	6.1	The Range 104	
	6.2	Location-based Measures of Dispersion 105	
	6.3	The Variance and the Standard Deviation 106	
	6.4	Computation of the Standard Deviation 107	
	6.5	Moments and Measures of Skewness and Kurtosis 113	
	6.6	The Measurement of Relative Dispersion 115	
7.	Proba	bility in Practice	117
	7.1	Bayes, Laplace, and Inductive Reasoning 117	
	7.2	·	
	7.3	The Binomial and Poisson Distributions 123	
	7.4	The Normal Distribution 127	
	7.5	Student's t Distribution 130	
	7.6	Reading Probability Tables 133	
	7.7	Use of Normal Probability Paper 134	
8.	Princi	ples of Sampling	137
	8.1	The Sampling Problem 137	
	8.2	Random Selection in Scientific Sampling 139	
	8.3	Experimental Derivation of the Sampling Distribution of the Mean	140
	8.4	The Central Limit Theorem 146	

8.5 The Standard Error of the Mean 147

The Statement of Reliability 149

9.1 Requirements of a Good Sample 153

9.2 The Sampling Frame and Sampling Units 155

153

8.7 Statistical Inference 151

Sampling in Practice

8.6

9.

	9.3	Use of Maps and Aerial Photographs in Sampling 159	
	9.4		
	9.5	•	
	9.6		169
	9.7		170
10.	Mak	ing Estimates of Means and Proportions	174
	10.1	Characteristics of a Good Statistic or Estimate 174	
	10.2		
	10.3	Confidence Interval Estimates of the Mean 178	
	10.4	Estimating Procedures with Small Samples 180	
	10.5	Comparison of Two Sample Means 181	
	10.6	Confidence Interval Estimates of a Proportion 182	
	10.7	Determination of Sample Size in Estimation Procedures 188	
11.	Testi	ng Hypotheses and Statistical Decision Making	191
	- 11.1	Statistics Regarded as Decision Making Under Uncertainty 191	
	11.2	Null and Alternative Hypotheses 195	
	11.3		
	11.4	The Power of a Statistical Test 199	
	11.5	Hypotheses Concerning Means and Proportions 201	
	11.6	Hypotheses Concerning Differences Between Two Samples 206	
12.	Samp	ling Methods in Auditing	211
	12.1	Control of Clerical Errors 211	
	12.2	Sampling of Physical Property 212	
	12.3	Application of Sampling Methods to Accounting Records 214	
	12.4	Sampling Plans in an Audit Test 216	
	12.5	How Much to Sample 218	
	12.6	Discovery Sampling 220	
13.	Bivar	iate Data and Regression Analysis	222
	13.1	The Scatter Diagram and Stereogram 222	
	13.2		
	13.3	The Least Squares Method in Linear Prediction 233	
	13.4	Confidence Intervals in Regression Analysis 235	
	13.5	Regression Analysis in Economic and Business Problems 237	
14.	Corre	lation and the Analysis of Variance	240
	14.1	Measuring the Degree of Correlation 240	
	14.2	Coefficients of Correlation and Determination 243	
	14.3	Sampling Significance of Correlation Coefficient 245	

Con	tents	
14.4	Correlation Table for Grouped Data 250	
14.5		
14.6		
Distr	ibution-Free Methods in Statistics	259
15.1	Non-parametric Tests of Statistical Hypotheses 259	
15.2	Chi-Square Test of Goodness of Fit 261	
15.5	The Theory of Runs 273	
		05.
Mana	agement	274
16.1	Statistical Surveillance of Repetitive Processes 274	
16.2	Manufacturing Process Control 275	
16.6	Risks in Quality Control 290	
Statis	tical Analysis of Time Series Data	294
17.1	Components of Time Series 294	
17.3	Additive and Multiplicative Time Series Models 300	
17.6	Moving Averages 313	
Descr	ription of the Components in Time Series	318
18.1	Time Series Analysis and Forecasting 318	
18.2		
18.3	Growth Curves 332	
18.4	Determination of Seasonal Index and Seasonal Adjustment 339	
18.5	Estimation of Cyclical-Irregular Movements 362	
18.6	Economic Indicators and Business Cycle Analysis 364	
The l	Making and Using of Index Numbers	3 7 0
19.1	-	
19.2		
19.3	Consumer Price Index 384	
19.4		
	14.4 14.5 14.6 Distr. 15.1 15.2 15.3 15.4 15.5 Statis Mana 16.1 16.2 16.3 16.4 16.5 16.6 Statis 17.1 17.2 17.3 17.4 17.5 17.6 Descr. 18.1 18.2 18.3 18.4 18.5 18.6 The I	14.4 Correlation Table for Grouped Data 250 14.5 Problem of Multiple Relations 252 14.6 Analysis of Variance; the One-way Classification 255 Distribution-Free Methods in Statistics 15.1 Non-parametric Tests of Statistical Hypotheses 259 15.2 Chi-Square Test of Goodness of Fit 261 15.3 Tests Using Signs and Ranks 265 15.4 Rank Correlation Methods 270 15.5 The Theory of Runs 273 Statistical Quality Control in Production and Management 16.1 Statistical Surveillance of Repetitive Processes 274 16.2 Manufacturing Pracess Control 275 16.3 Control Charts for Variables 278 16.4 Control Charts for Attributes 283 16.5 Sampling Plans 286 16.6 Risks in Quality Control 290 Statistical Analysis of Time Series Data 17.1 Components of Time Series 294 17.2 Some Examples of Time Series 296 17.3 Additive and Multiplicative Time Series Models 300 17.4 Distribution-free Test for Cycle 311 17.6 Moving Averages 313 Description of the Components in Time Series 18.1 Time Series Analysis and Forecasting 318 18.2 Fitting of Linear and Non-linear Trends 325 18.3 Growth Curves 332 18.4 Determination of Seasonal Index and Seasonal Adjustment 339 18.5 Estimation of Cyclical-Irregular Movements 362 18.6 Economic Indicators and Business Cycle Analysis 364 The Making and Using of Index Numbers 19.1 Statistical Methods in Index Number Construction 370 19.2 Measurement of Price and Quantity Changes 378 19.3 Consumer Price Index 384

19.5 Statistical Tests of Index Numbers 396

20. Statis	stical Methods in Forecasting and Market Research	398
20.1	Forecasting Techniques 398	
20.2	Econometric Methods 402	
20.3	Input-output Analysis 407	
20.4	Market and Distribution Research 410	
20.5	Surveys of Consumer Buying Plans 418	
Appendix	A. Principles of Statistical Presentation	423
Appendix	B. How to Calculate	436
Appendix	C. How to Use a Library of Statistical Sources	453
Appendix	D. Greek Alphabet	456
Appendix	E. List of References	456
Appendix	F. Statistical Tables	464
Appendix	G. Final Comments of Committee on Broadcast Ratings	520
Index		529

List of Tables

TABL	£ 1	PAGE
2-1	Compendium of the Census of 1850	21
4-1	Weekly Earnings of Typists in Manufacturing Firms	62
4-2	Estimated Distribution of Production Workers in Manufacturing	70
4-3	Percent Distribution of Production Workers in Manufacturing by Sex	72
4-4	Percent Distribution of Production Workers in the Men's and Boys' Suit	
	and Coat Manufacturing Industry	73
12-1	Sampling in Railroad Accounting	215
13-1	Relationship Between Number of Police Officers and Population in 33	
	Large Cities in the United States	230
14-1	Correlation Table for Grades of Four Hundred Students in Mathematics	
	and Statistics	252
17-1	Average Annual Temperature in New York City, 1900-1959	296
17-2	Average Monthly Temperature in New York City, 1941-1959	298
17-3	Death Rate from Tuberculosis in the United States, 1900-1959	300
17-4	Estimated Monthly Sales of Variety Stores in the United States, 1941-1959	302
17-5	Moving Averages of Average Annual Temperature in New York City,	
	1900–1959	315
18-1	Least Squares Method for Linear Trend	328
18-2	Least Squares Method for Second-Degree Trend	330
18-3	Procedure for Finding the 12 Month Centered Moving Average	344
18-4	UNIVAC Print-Out for Variety-Store Sales	346
18- 5	Dates of Peaks and Troughs of Business Cycles in the United States, 1834-	
	1958	365
18-6	Duration of Business Cycle Expansions and Contractions in the United	
	States, 1854–1958	368
19-1	Economic Progress, United States, 1900-1959	376
19-2	Goods and Services Priced for the Consumer Price Index	386
19-3	Consumer Price Index	388
19-4	Index of Industrial Production	392
19-5	Index of Industrial Production, Market Groupings by Month, 1959	394
19-6	Index of Industrial Production, 1919-1959	396
20-1	Interindustry Flow of Goods and Services, 1947	408
20-2	Exposure to an Issue of the Saturday Evening Post	415
20-3	Questionnaire Used in Study of Air Travelers	417
20-4	Questionnaire Used in Survey of Consumer Buying Intentions	418
20-5	Plans to Buy Durable Goods, 1959-1960	120

List of Charts

CHART	r · · · · · · · · · · · · · · · · · · ·	PAGE
	Sanborn Map Endpapers (fit	ont)
2-1	Censuses Grow with the Country	19
2-2	Enumerator's Schedule, 1960 Census	23
2-3	Household Questionnaire, 1960 Census	24
3-1	The Chinese Abacus	31
3-2	The Monroe Calculator	34
3-3	Keysort Cards	38
3-4	Sorting Keysort Cards	40
3-5	Punched Cards	44
3-6	IBM Card Punch	45
3-7	IBM Sorter	46
3-8	IBM Tabulating Machine	47
3-9		51
	IBM Disk Storage Unit	52
	Functional Organization Chart	53
•	Simple Programming	54
	FOSDIC	56
4-1	Frequency Polygon and Histogram of Weekly Earnings of Typists	75
4-2	Percent Distribution of Major Types of Consumer Units	76
4-3	Population Pyramids for Alaska 1939, and Germany 1946	78
4-4	Distribution of Heights of Soldiers in the Army of the Potomac	79
4-5	Distribution Curves of Weekly Earnings of Typists	80
4-6	Cumulative Percentage Distribution of Hourly Earnings by Sex	81
4-7	Lorenz Curve of Personal Income	82
4-8	Types of Frequency Distributions Illustrated	84
5-1	Relationship among the Arithmetic Mean, Median, and Mode	98
5-2	Graphic Estimation of the Arithmetic Mean	100
5-3	Graphic Method of Estimating the Median and Quartiles	101
5-4	Graphic Method of Estimating the Mode	102
6-1	Normal Curve Showing Points of Inflection	112
6-2	Normal Curve with Standard Deviation Units	113
7-1	Venn Diagrams	120
7-2	Normal Distributions	130
7-3	Probability Illustrations	133
7-4	Arithmetic Probability Paper	135
8-1	Pearson Binomial Apparatus	142
8-2	Comparison of Actual and Theoretical Frequencies in a Dice-Rolling	
	Experiment	143
vvii		1-15

List of Charts---xxiii

CHAR	Т	PAGE
9-1	Typical Sampling Operation	155
9-2	Rochester, New York, by Census Tracts and Blocks, 1950	158
9-3	Diagram of Sample Segment	160
9-4	Aerial Photograph and Map	162
9-5	Diagram of a Sampling Plan	164
9-6	How to Canvass in Built-Up Areas	165
9-7	Absolute Sample Size is Important	168
10-1	Effect of Sample Size on Confidence Intervals	180
10-2	Confidence Limits for Proportions: $\alpha = 0.95$	184
10-3	Confidence Limits for Proportions: $\alpha = 0.99$	186
10-4	Binomial Probability Paper	187
11-1	Type I and Type II Errors	198
11-2	Power Curve for a Two-Tail Test	200
11-3	One-Tail Test and Two-Tail Test for a Mean	204
11-4	One-Tail Test and Two-Tail Test for a Proportion	205
11-5	The F Distribution	209
13-1	Scatter Diagram of Land Areas and Number of Felonies	224
13-2	Types of Relationships Shown by Scatter Diagrams	225
13-3	Distribution of 4,157 Six-Year-Old Boys on Basis of Hip Girth and Chest	
	Girth	226
13-4	Stereogram of 69,661 Boys on the Basis of Stature and Hip Girths	227
13-5	The Ideal Symmetrical Frequency-Surface	228
13-6	Nonlinear Lines of Regression	229
13-7	Scatter Diagram of Population and Police Strength	231
13-8	The Least Squares Criterion	234
14-1	Types of Deviations in Bivariate Analysis	241
14-2	Ellipses from Correlation Surfaces	246
14-3 14-4	Distribution of r	247
14-5	Confidence Limits for Correlation Coefficient: $\alpha = 0.95$	248
14-6	Confidence Limits for Correlation Coefficient: $\alpha = 0.99$	249
15-1	Joint Regression	253
15-2	Distribution of χ^2 for Various Degrees of Freedom Distribution of χ^2 for Rolls of a Die	262
15-3	Binomial Probability Paper Applied to a Chi-Square Test	264
16-1	Control Charts for Mean and for Range	265 280
16-2	Mean Out of Control	281
16-3	Control Charts for Mean and for Standard Deviation	282
16-4	Control Charts for Percent Defective and for Defects per Unit	285
16-5	Method of Preparing a Sample of Coal	288
16-6	Operating Characteristic Curves	291
16-7	Operating Characteristic Curves from MIL-STD-105A	292
17-1	Average Annual Temperature in New York City, 1900–1959	297
17-2	Average Monthly Temperature in New York City, 1907–1959	299
17-3	Death Rate from Tuberculosis in the United States, 1900–1959	301
	Estimated Monthly Sales of Variety Stores in the United States, 1957–1959	
17-5	Components of a Synthetic Time Series	306
		200