

Jeffrey Slater

Practical Business Math Procedures

Second Edition



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Jeffrey Slater

**North Shore Community College
Beverly, Massachusetts**

Second Edition

1987

IRWIN

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Practical Business Math Procedures

*Dedicated to my family
Shelley, Rusty, Abby, and Scupper
With love*

Acknowledgments

People told me revisions are easy and quick. *NOT THIS ONE*. The Second Edition of *Practical Business Math Procedures* is not a cosmetic revision. It reflects feedback from over 60,000 students who used the First Edition. The process of revision has in fact taken as long as the preparation of the First Edition.

I am truly proud of the finished package. I would like to thank the following for their help in making *Practical Business Math Procedures* a true learning system for students.

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The Wall Street Journal

Special thanks to Cheryl Bogart and Eva Haight in the typing of the manuscript.

Note to Students

Special Feature

Inside front cover

Fold-out newspaper that teaches you how to read selected financial data in *The Wall Street Journal*. Page references are also included relating business math theory in newspaper to content found within text.

Structure of *Practical Business Math Procedures*, Second Edition:
The student support system

Chapters

21 chapters, broken up
into learning units

Objectives are presented at the beginning of each chapter. Page references are provided.

Mini-Quizzes

Self-quizzes at the end
of each unit, with
solutions at the end of
each chapter

Provides instant feedback. Solutions to mini-quizzes are at the ends of chapters with page references.

Problems

Complete sets of both
drill (Level 1) and word
problems (Level 2) at
the end of each chapter

Check figures for odd-numbered problems are found in Appendix 4.

Extra Problems

One more time: 210
additional word
problems to review
chapters

Appendix 1 has 10 word problems per chapter as an additional set of supplementary homework word problems. Your professor has solutions to these.

Vocabulary

Vocabulary review with
page references

At the end of each chapter is a list of key terms along with specific page references.

Chapter Organizer: A Reference Guide

Outline of chapter at
end of chapter that
presents key points,
formulas, procedures,
etc., along with worked-
out problems

Includes page references. The organizer provides you with a complete set of "Student Notes" chapter by chapter.

Summary Practice Test

Sample test that reviews the chapter

Take a test before the actual one. Your professor has solutions.

Audio Cassette Tapes

Chapter mini-quizzes are reviewed on audio tapes

Your lab or professor will have access to these tapes. The tape reviews key concepts in the chapter along with a discussion of the mini-quizzes.

New to this edition. Computer software is available. Check with your professor for specifics.

In the Appendixes, be sure to look at:

Appendix 1

One more time: 210 additional word problems

Metric System

A simple introduction to understanding the metric system

Basic Business Statistics with Computer Applications

Basic calculations of mean, median, mode, etc., plus examples of graphs illustrated on computer screens

Check Figures for Odd-Numbered Problems

Answers to drill and word problems

Glossary

All terms simply defined

Note to Professor

The total package of *Practical Business Math Procedures*, Second Edition, includes the following:

1. Student Edition of text.
2. Teacher's Edition of text with worked out solutions.
3. Manual Test Bank (four exams per chapter), including pre- and post-skill tests along with final exam.
4. Instructor's Resource Manual containing lecture outlines, crossword puzzles, and a complete set of reproducible tables that are found in the text.
5. Audio cassette tapes to review chapters and mini-quizzes.
6. Box of overhead *plastic* transparencies for solutions to end of chapter drill and word problems.
7. Set of *colored* plastic teaching transparencies.
8. Computer software.
9. Computerized test bank with over 1,000 true-false and multiple choice questions.
10. Special fold-out newspaper in the inside front cover of the text on how to read selected financial data in *The Wall Street Journal*, along with how to apply your Business Mathematics to it. Page references are provided.
11. Special supplement on how to use the "touch method" with the electronic calculator. Time tests and problem materials will be furnished.

Students need your time and hopefully this "industry-leading package" will provide the needed faculty support system you need.

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Review of Basic Computational Skills

On completion of this chapter you should be able to:

The Defense Rests

"The average American male spends 3,350 hours of his life shaving." My love for my beard is suddenly stronger, now that I can sleep 3,000 hours longer.

Arnold J. Zarrett

LU 1-1: Applying Business Math in Today's Business World: Writing of Numbers; Rounding Whole Numbers

1. Explain how business math is used in the decision-making process of today's business world. [2]
2. Convert written numbers into verbal form. [3]
3. Write numbers from verbal form. [3]
4. Identify digits to be rounded. [4]
5. Round whole numbers to indicated position (tens, hundreds, thousands, and so on). [4]

LU 1-2: Whole Numbers—Addition and Subtraction

1. Develop speed and accuracy. [5]
2. Add columns by grouping of tens. [5]
3. Prove addition and subtraction computations. [5,6]
4. Estimate addition and subtraction computations. [5,6]
5. Compare and contrast "common sense" with the process of estimating. [6]
6. Complete horizontal and vertical addition and subtraction. [6]

LU 1-3: Whole Numbers—Multiplication and Division

1. Explain the relationship of multiplication to addition. [7]
2. Estimate and prove multiplication and division calculations. [7,9]
3. Complete multiplication and division calculations by shortcut methods (zero, 25, 50). [8,10]
4. Complete short division. [9]
5. Complete long division. [10]

BLOOPERS: About 6.5 million individual income tax returns last year had math errors and other careless mistakes, the IRS says. That's out of a total of more than 96 million individual returns. Many people erred on medical costs or took the wrong amount of tax from the tables.

Learning Unit 1-1: Applying Business Math in Today's Business World: Writing of Numbers; Rounding Whole Numbers

Christmas Shopping at Marshall Field's Flagship Store on State Street

CHICAGO—An emergency shipment of cashmere-lined gloves hasn't arrived. An expensive new display of designer leather-bags isn't ready. Some racks are empty, and the company's chairman suggests a rather discouraging solution: Turn part of the purse boutique into a stall for mints.

The golden Christmas shopping bags the store had planned to use stymie the electronic security system, but new bags aren't available yet. And it takes more than two hours in line if you want to visit Santa.

But the cash registers are crunching out the good news. The crowds, perhaps 70,000 people today, seem to be buying. In offices across the way from Santa's Cozy Cloud Cot-

tage, the store's manager Richard R. Donat, and his merchandise executives sweat out the figures, department by department. They cheer as they discern a trend—and get their Christmas wish: double-digit sales increases.

The six-week Christmas shopping season makes or breaks many retailers. At State Street, about 30% of annual sales and 70% of profit come in November and December. So Field's has been preparing for this Christmas for nearly two years. The 21-store company's investment in Christmas personnel, events, displays, advertising and supplies exceeds \$5 million.

The decision-making process of a business is the key to its success in today's business world. In the case of Marshall Field, the problems during the Christmas shopping season were out-of-stock merchandise and wrong shopping bags. Marshall Field attempted to solve its out-of-stock merchandise problem with an alternative strategy and turned part of the purse boutique into a stall for mints. The solution made sense because people kept buying, and the result was a double-digit sales increase. From this example we can list the four steps in the decision-making process of a business:

Steps

1. State the problem(s)—out of stock.
2. Decide the best method to solve it—add candy to empty shelves.
3. Is the solution making sense—people are buying.
4. Evaluate the end result—double-digit sales increase.

Although Marshall Field's alternative business strategy proved to be financially successful, not all strategy solutions to business problems have such a happy ending. The solution to many problems can also be found by using mathematics. As you study *Practical Business Math Procedures*, 2nd edition, you will learn how a business math course is an invaluable tool in the decision-making process. Topics that you will study in this course will include the following types of business problems:

Career Choices

Surveyed college freshmen said their probable career choices will be:

Men		Women	
Engineer	18.5%	Business executive	11.4%
Business executive	12.5	Nurse	7.5
Computer analyst	7.7	Accountant	6.8
Accountant	5.2	Teacher	6.1

Source: Cooperative Institutional Research Program

1. In which selling seasons can we raise or lower our markups or markdowns?
2. Are we allocating enough floor space to winter clothing?
3. Should we keep the store open on Saturday night?
4. Are we taking advantage of all our trade and cash discounts?
5. What is the present value of the money we are borrowing?
6. What is the annual percentage rate we are paying on the company truck?
7. How is our property assessed?
8. Should our business utilize credit cards or only accept cash?
9. Do we need business interruption insurance?
10. Are we complying with the Truth in Lending Act?

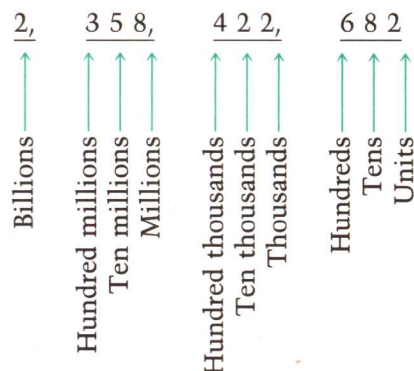
Before presenting advanced business math topics, it is important to review the basic math skills used for speed and accuracy. Too often a calculator, cash register, or computer will break down, and we will have to rely on our "manual" backup system. So let's first look at how whole numbers are written and then learn how to quickly estimate calculations by rounding.

Writing of Numbers

Using our decimal number system, the **whole number** 2,634 is in actuality:

$$2,634 = (2 \times 1,000) + (6 \times 100) + (3 \times 10) + (4 \times 1)$$

This is true because our number system has positions of units, tens, hundreds, thousands, and so on. Let's look at how the number two billion, three hundred fifty-eight million, four hundred twenty-two thousand, six hundred eighty-two is written.



Raising Children

The projected cost of raising one boy born in 1980 to age 22 is \$214,957—not including college costs.

Food	\$69,585
Housing	65,007
Transportation	29,255
Health	14,973
Clothing	8,959
Other	27,178

Source: Costs of Children, Lawrence Olson

Note how each number is positioned (the commas help separate from right to left every three digits). When we read (or write in verbal) a whole number, we do not use the word *and*. This is used for the decimal point and discussed later in the course. Also, any numbers written between twenty-one to ninety-nine are hyphenated. For example, the number **4,959** in verbal is written as **four thousand, nine hundred fifty-nine**.

As we work with numbers and try to estimate results, the process of **rounding** can be a great tool to verify actual calculations. Let's look at the rounding-off process, keeping in mind that this process of rounding tries to **approximate** the actual answer.

Rounding Whole Numbers

The three steps used to **round whole numbers** are:

Steps

1. Identify the digit to be rounded.
2. If digit to right of place identified in step 1 is 5 or more, increase identified digit by one (round up). (If not, identified digit is not changed.)
3. Change all of the digits to the right of the identified digit to zeros.

Rounded to nearest thousand, 38,725 rounds to 39,000. Rounded to nearest ten, 38,725 rounds to 38,730. Rounded to nearest hundred, 38,725 rounds to 38,700.

Example. 38,725 rounded to the nearest thousand.

Step 1. 38,725

Identified digit in thousand position—8.

Step 2.

7 is 5 or more; thus 8, the identified digit (step 1), is now rounded to a 9.

39,725

Step 3. 39,000

Change the 725 to zeros, since these are the digits to the right of the number rounded off.

Additional Example. 7,458 rounded to nearest thousand.

Step 1. 7,458

Identified digit in thousand position—7.

Step 2.

Digit to right of 7 is not 5 or more; thus identified digit is not changed. We only change if digit to right is 5 or more.

Step 3. 7,000

Change the 458 to zeros.

Rounding affects accuracy in calculations.

In this case we are rounding **all the way**. This means that after rounding we have **only one nonzero digit remaining**. By rounding all the way our estimate is not as exact. For example, 4,895 rounded all the way is 5,000. Remember, rounding to a specific digit depends on what degree of accuracy you seek in your estimate.

LU 1-1 Mini-Quiz Applying Business Math in Today's Business World: Writing of Numbers; Rounding Whole Numbers

Solutions to Mini-Quiz on P. 11.

At the end of each unit you will have a chance to check your progress with a mini-quiz. If you are having difficulty, these mini-quizzes will help identify your area of weakness. It is suggested that you work out the problems on scrap paper and check your answers with the solutions given on the page number following the mini-quiz title in the margin. After checking your answers, a page number in the margin of the solutions refers you back to the page you left off.

1. Write in verbal form:

a. 9,258

b. 28,758

c. 425,416,052

d. 6,000,010

<u>Nearest Ten</u>	<u>Nearest Hundred</u>	<u>Nearest Thousand</u>	<u>Rounded All the Way</u>
a. 43	b. 468	c. 7,980	d. 120
e. 86	f. 541	g. 6,105	h. 1,650

In today's fast-moving business world there is a great need for speed and accuracy in the adding and subtracting of numbers. Too often a calculator or computer is not available, and you must quickly add or subtract manually.

A quick method to add a large group of numbers is to group them by 10s. This method is used by many accountants. The various combinations of numbers adding to 10 are:

1	2	2	5	3	4	3	2
1	7	3	4	3	4	2	2
8	1	5	1	4	2	5	6

2 ₈	8 ₂	3 ₇	7 ₃	5 ₅	4 ₆	6 ₄	1 ₉	9 ₁
----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------

$$\begin{array}{r} 7 \\ 3 \end{array} \begin{array}{l} \nearrow \\ \searrow \end{array} 10$$

$$\begin{array}{r} 8 \\ 2 \end{array} \begin{array}{l} \nearrow \\ \searrow \end{array} 10$$

$$\begin{array}{r} 3 \\ 4 \end{array} \begin{array}{l} \nearrow \\ \searrow \end{array} 10$$

$$\begin{array}{r} 3 \\ \hline 30 \end{array}$$

7	>	8	
1	>	8	18
8	>	10	
2	>	10	32
9	>	14	
5	>	14	
6	>	10	42
4	>	10	
42			

The Adding and Proving Process

Proving bottom to top	↑	$\begin{array}{r} \overset{2}{1},\overset{2}{4}23 \\ 3,891 \\ 2,750 \\ 7,190 \\ \hline 15,254 \end{array}$	↓	Adding top to bottom
-----------------------------	---	---	---	----------------------------

Add each column as a separate total and then combine:

$$\begin{array}{r} 1,423 \\ 3,891 \\ 2,750 \\ 7,190 \\ \hline 4 \\ 25 \\ 20 \\ 13 \\ \hline 15,254 \end{array}$$

Another method to use when adding long columns is to divide the columns into two parts, obtain a subtotal for each part, and add subtotals for the grand total.