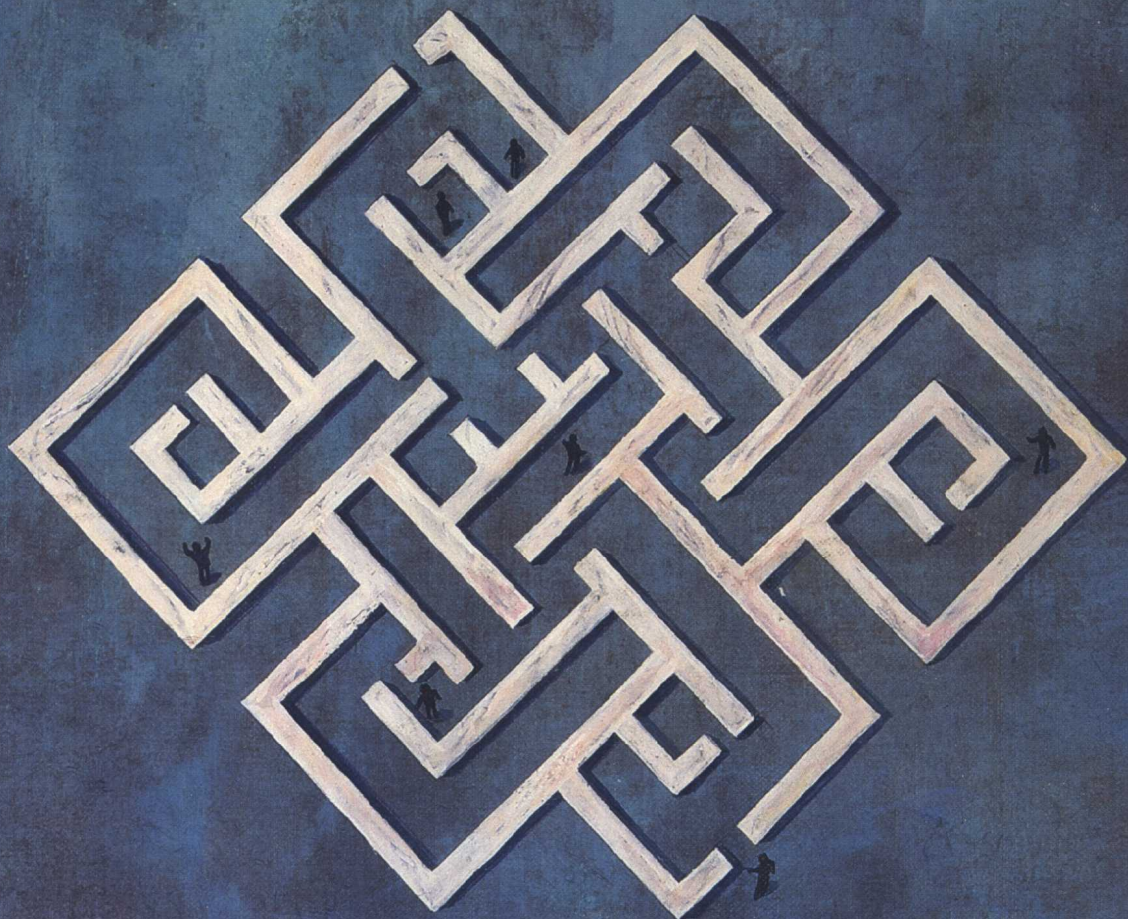

Quantitative Decision Making

Guisseppe A. Forgionne





Quantitative Decision Making

Guisseppe A. Forgionne
Bucknell University

Wadsworth Publishing Company
Belmont, California
A Division of Wadsworth, Inc.

Economics Editor: Stephanie Surfus
Editorial Assistant: Holly Allen
Production Editor: Sandra Craig
Print Buyer: Ruth Cole
Cover and Interior Designer: Andrew H. Ogus
Cover Illustrator: Philip Li
Copy Editor: Janet Greenblatt
Technical Illustrator: Art by Ayxa
Compositor: Composition House Limited

The symbol used on the cover and part and chapter opening pages was adapted from Peter S. Stevens *Handbook of Regular Patterns: An Introduction to Symmetry in Two Dimensions*, copyright 1981 by Peter S. Stevens, published by The MIT Press. Used by permission.

© 1986 by Wadsworth, Inc. All rights reserved. No part of this book may be reproduced, stored in a retrieval system, or transcribed, in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise, without the prior written permission of the publisher, Wadsworth Publishing Company, Belmont, California 94002, a division of Wadsworth, Inc.

Printed in the United States of America

1 2 3 4 5 6 7 8 9 10—90 89 88 87 86

ISBN 0-534-05364-5

Library of Congress Cataloging in Publication Data

Forgionne, Guisseppi A., 1945—

Quantitative decision making.

Includes bibliographies and index.

1. Management science. I. Title.

HD30.23.F69 1986 658.4'03 85-13920

Quantitative Decision Making

To my mother, Mary, and to Jesus

Preface

This book gives an introductory survey of management science/operations research. The text provides complete coverage of today's major quantitative models and shows how they are applied to managerial problems in public and private organizations. Much effort has been spent in making each topic interesting and easy to read. The purpose is to provide the user with a sound conceptual understanding of the role of quantitative analysis in the decision-making process.

FOCUS The focus is on the practical and applied. The text explains how to formulate decision problems, how to solve them with an appropriate quantitative analysis, and how to apply the recommended solution. However, there is an emphasis on concepts rather than mechanical manipulation. Hence, a significant part of the discussion is devoted to problem formulation, technique assumptions, potentials, limitations, and interpretation of the results of the analysis from the perspective of the decision maker.

There is a simplified, logical presentation of quantitative tools with extensive use of examples, graphs, tables, and other illustrative devices. Furthermore, each chapter has technique summaries incorporated at appropriate points within the discussion. In addition, the discussion highlights the connection between management science/operations research and computer information systems. Appropriate batch and interactive computer programs are identified. Computer data and models are presented, solution procedures are discussed, and the results are interpreted. There are also end-of-chapter glossaries for easy reference.

Quantitative decision making, like athletics and music, is best learned by doing. Beginners can facilitate their understanding by practicing the concepts in the types of situations actually encountered by decision makers. Therefore, there is an abundance of realistic examples that are scaled-down versions of problems encountered in public and private

organizations. Each chapter contains several examples in the body of the text and numerous exercises and a case at the end.

End-of-chapter exercises are divided into thought exercises (extension of basic concepts), technique exercises (practice of procedures), and applications exercises (selection of concepts and techniques, and development of solution). Each chapter concludes with a modified version of an actual private- or public-sector case. Cases require an integration and extension of text concepts, quantitative analysis, formulation of a decision recommendation, and presentation of results in a form understandable to management.

Mathematics is kept at an accessible level for the beginning user of quantitative decision making. The only prerequisites are college algebra, elementary probability, and basic statistics. Other relevant mathematics is developed as needed. The orientation should put the material within reach of a junior, senior, or beginning MBA student.

ORGANIZATION

The book is organized in a way that leads to a coherent treatment of the subject. First, major topics are divided into modules, or parts. Part I provides the foundations. It defines the nature of management science, discusses its role in the decision-making process, and identifies the steps necessary for successful implementation. The second part presents a general decision-making framework and shows how strategies can be formed in various decision environments. Part III addresses linear and other mathematical (integer, goal, heuristic, and nonlinear) programming problems and methods. The next part provides a comprehensive review of general network flow problems, including transportation, transshipment, assignment, minimal spanning trees, cycles and routes, maximal flows, and PERT/CPM. Part V considers some standard situations involving sequential decisions, queuing, and inventory problems. Simulation is the topic of the final module.

Although each module after Part I is essentially independent, the modules are arranged in a logical progression. Part II deals mainly with decisions made in an uncertain or risky environment. The mathematical programming module, Part III, extends the analysis to constrained optimization problems that involve primarily certain circumstances. In Part IV, the mathematical programming concepts are applied to network flow problems. Part V considers some standard analytical models that build on the concepts developed in preceding modules. In many cases, available analytical models are of little value because of the complex or unstructured nature of the problem. The final module presents an approach designed for these situations.

Each module, or part, is also designed to eliminate the effect of variability in student capabilities and motivation. Starting at the simplest

level, there is a gradual development of ideas and applications. Eventually, the student progresses to near the state of the art in the field. Similar independent modularity is provided within the chapters. Each chapter starts with elementary concepts, progresses through increasingly complex material, and ends with the most advanced topics.

With this arrangement, students can be assigned a continuous sequence of pages within a module. Then, when the level within the module exceeds the course objectives, students can be directed to another part of the book. In this way, the instructor can easily control the level for any particular topic. Furthermore, by directing the sequence of modules, the instructor can readily satisfy different course plans. These features provide the topical flexibility necessary for matching content with course objectives and student profiles.

The selection of topics reflects the introductory nature of the text. The book emphasizes the most popular quantitative approaches used today by public and private organizations. Unfortunately, some techniques, like nonlinear programming, require a preparatory background in management science/operations research. In these instances, the topic is merely identified and illustrated, and text notations and a bibliography refer the user to appropriate advanced treatments. However, the book provides the essential, relevant material covered in almost all one-semester/two-quarter introductory survey courses in quantitative decision making.

SUPPLEMENTARY MATERIAL

The Instructor's Manual contains fully worked-out solutions, hints in selecting problems for student assignments, and a bank of potential examination problems complete with solutions. The hints include a brief description of the problems, an assessment of their level of difficulty, and the relationships between the concepts and problems. In addition, the Manual provides sample course outlines and chapter-by-chapter ideas for presenting the material.

ACKNOWLEDGMENTS

I wish to thank the staff of Wadsworth Publishing Company for their helpful suggestions. In particular, Jon Thompson and Stephanie Surfus, my acquisition editors, did an excellent job. I also appreciated the work of the designer, Andrew H. Ogus, and the production editor, Sandra Craig. I would like to express my appreciation to my colleagues, students, and family, who have contributed greatly to the project. Also, I am indebted to the administration of California State Polytechnic University, Pomona, for their support, especially Gerry White and the rest of the staff of the School of Business Administration Steno Pool. Pamela Scroggs, a student

assistant, deserves special commendation for her help in assembling the final draft of the manuscript. Finally, I'd like to thank the reviewers of the manuscript: Bruce Bowerman, Miami University of Ohio; Harrison S. Carter, Georgia Southern College; Lawrence Ettkin, University of Tennessee at Chattanooga; John A. Lawrence, California State University at Fullerton; Michael Middleton, University of San Francisco; Alan Neebe, University of North Carolina at Chapel Hill; Paul Rackow, Fordham University; Harold J. Schleef, University of Oregon; Michael Sklar, University of Georgia; Willbann Terpenning, University of Notre Dame; Frederick P. Williams, North Texas State University.

Guisseppe A. Forgionne

Contents

PREFACE xvii

PART I FOUNDATIONS 2

Chapter 1 Introduction 4

EVOLUTION OF QUANTITATIVE DECISION MAKING 5

Origins 6

Early Development 7

Maturity 8

CHARACTERISTICS 9

Focus on Problems 9

Systems Approach 9

Scientific Method 10

Team Approach 11

Mathematics and Computers 11

APPLICATIONS 12

Summary 15 Thought Exercises 16

Glossary 15 Technique Exercises 17

References 16 Applications Exercises 18

CASE: *The Cookbook Conspiracy* 19

Chapter 2 The Management Science Process 20

QUANTITATIVE FORMULATION 21

Defining the Problem 23

Formulating a Quantitative Model 24

Types of Models 25

Mathematical Models 26

Gathering Relevant Quantitative Data 29

ANALYSIS AND SOLUTION 29

MIS Process 29

Preparing Summary Reports 30

Processing Inquiries	32
Solving the Quantitative Model	35
Decision Support Systems	37
IMPLEMENTATION	39
Barriers to Implementation	39
Implementation Strategies	39
Summary	41
Glossary	42
References	43
Thought Exercises	44
Technique Exercises	45
Applications Exercises	47
CASE: <i>Jane Allen's Career Choice</i>	49

PART II DECISION ANALYSIS 50

Chapter 3 Decision Theory 52

STRUCTURE OF THE PROBLEM	53
Elements	54
Decision Tables	56
DECISION CRITERIA	57
Types of Situations	57
Dominance	59
Decision Making Under Uncertainty	60
Decision Making Under Risk	68
Decision Making Under Certainty	73
SEQUENTIAL DECISIONS	74
Decision Trees	76
Finding the Solution	79
Applications	83
Summary	83
Glossary	84
References	86
Thought Exercises	87
Technique Exercises	92
Applications Exercises	99
CASE: <i>The Healthy Food Store</i>	101

Chapter 4 Bayesian Analysis 103

VALUE OF INFORMATION	105
Sensitivity of the Decision	106
Perfect Information	108
Expected Opportunity Loss	109
Measuring the Benefit of Additional Knowledge	112
UPDATING PROBABILITIES	112
Sample Data	113
Revised Probabilities	117
Tabular Approach	118

DECISION MAKING WITH ADDITIONAL INFORMATION	119
Sequence of Decisions	120
Evaluating the Information	122
Developing a Strategy	126
Computer Analysis	127
Applications	131
Summary	131
Glossary	133
References	134
Thought Exercises	135
Technique Exercises	138
Applications Exercises	142
CASE: <i>Municipal Transit Authority</i>	145

Chapter 5 Utility and Game Theory 147

UTILITY ANALYSIS	148
Measuring Utility	149
Using Utility for Decision Making	153
Attitudes Toward Risk	154
Limitations	159
MULTIPLE CRITERIA	160
Priority Systems	162
Transformations	165
Multiattribute Utility Theory	166
Limitations	170
CONFLICT SITUATIONS	171
Characteristics	172
Dominance	174
Pessimistic Criterion	175
Mixed Strategy	178
Extensions	186
Summary	189
Glossary	190
References	191
Thought Exercises	192
Technique Exercises	196
Applications Exercises	203
CASE: <i>Rural Vehicles, Inc.</i>	209

PART III MATHEMATICAL PROGRAMMING 210

Chapter 6 Linear Programming 213

NATURE OF LINEAR PROGRAMMING	215
Formulating the Problem	215
Characteristics	218
Classes of Problems	221
GRAPHIC SOLUTION PROCEDURE	222
Feasible Solutions	224

Finding the Best Solution	230
Minimization Problems	237
DECISION CONSIDERATIONS	240
Redundant Restrictions	240
Unbounded Problems	242
Infeasible Problems	243
Ties for the Best Solution	246
Summary	248
Glossary	249
References	250
Thought Exercises	252
Technique Exercises	255
Applications Exercises	257
CASE: <i>Aviation Unlimited</i>	260

Chapter 7 Simplex Method 261

FUNDAMENTAL METHODOLOGY	262
Standard Form	264
Basic Feasible Solutions	267
Initial Basic Feasible Solution	268
Evaluating a Solution	269
Improving a Solution	270
Iteration Process	272
Finding the Optimal Solution	275
SIMPLEX TABLES	278
Initial Simplex Table	278
Second Simplex Table	285
Optimal Simplex Table	293
DECISION CONSIDERATIONS	294
Constraint Formats	294
Minimization Problems	305
Special Situations	309
Summary	315
Glossary	316
References	317
Thought Exercises	318
Technique Exercises	323
Applications Exercises	327
CASE: <i>Lowe Chemical, Inc.</i>	330

Chapter 8 Postoptimality Analysis 332

THE DUAL	334
Shadow Prices	335
Dual Linear Program	341
Minimization Problems	347
SENSITIVITY ANALYSIS	351
Objective Function	352
System Constraint Amount	360

Exchange Coefficients	367
Other Postoptimality Analysis	369
COMPUTER ANALYSIS	369
User Input	370
Computer Output	372
Management Benefits	373
Summary	373
Glossary	374
References	375
Thought Exercises	376
Technique Exercises	382
Applications Exercises	387
CASE: <i>The Tennis Shop</i>	392

Chapter 9 Mathematical Programming Topics 393

LINEAR PROGRAMMING LIMITATIONS	394
Indivisibility	395
Multiple Objectives	397
Uncertainty	397
Nonlinear Relationships	399
Sequential Problems	404
Decision Situations	404
INTEGER PROGRAMMING	405
Rounding Fractional Solutions	406
Graphic Approach	409
Enumeration	412
Cutting Plane Method	412
Branch and Bound Method	416
Computer Analysis	421
Extensions	424
GOAL PROGRAMMING	426
Formulating the Problem	428
Graphic Solution	431
Computer Analysis	435
Extensions	437
Summary	439
Glossary	439
References	441
Thought Exercises	443
Technique Exercises	450
Applications Exercises	454
CASE: <i>Federated Motors, Inc.</i>	459

PART IV NETWORKS 460

Chapter 10 Distribution 462

TRANSPORTATION	463
Nature of the Problem	464

First Feasible Solution	468
Evaluating the Solution	476
Improving the Solution	484
Finding the Optimal Solution	487
DECISION CONSIDERATIONS	488
Unbalanced Supply and Demand	488
Prohibited Routes	492
Maximization	494
Degeneracy	497
Multiple Optima	500
Computer Analysis	502
Limitations	504
ASSIGNMENT	505
Nature of the Problem	506
Solving the Problem	508
Special Situations	515
Computer Analysis	520
Applications	522
Summary	523
Glossary	524
References	525
Thought Exercises	526
Technique Exercises	530
Applications Exercises	532
CASE: <i>Oriental Carpets, Inc.</i>	537

Chapter 11 Network Topics 538

LAYOUTS	539
Nature of the Problem	540
Finding the Optimal Design	541
Computer Analysis	544
Applications	546
ROUTES	546
Shortest Route Problem	547
Finding the Shortest Route	548
Computer Analysis	553
Applications	555
Traveling Salesperson Problem	556
Finding the Best Tour	558
Extensions	567
FLOWS	567
Maximal Flow Problem	567
Finding the Maximal Flow	568
Computer Analysis	572
Applications	575
Transfer Shipping	577
Optimal Distribution Pattern	579

Summary	582	Thought Exercises	585
Glossary	583	Technique Exercises	592
References	584	Applications Exercises	596
CASE: <i>General Parcel Service</i> 600			

Chapter 12 PERT/CPM 602

PERT	603
Project Network	605
Activity Times	606
Project Completion Date	610
Activity Schedule	613
Critical Activities	616
Project Duration Variability	617
Computer Analysis	620
CPM	624
Crashing Activity Times	625
Crashing Decision	626
Linear Programming	627
Computer Packages	629
PERT/COST	632
Planning and Scheduling Costs	633
Controlling Costs	636
Limitations	638
Summary	638
Glossary	639
References	640
Thought Exercises	641
Technique Exercises	643
Applications Exercises	649
CASE: <i>Universal Research Corporation</i> 654	

PART V MANAGEMENT SCIENCE TOPICS 656

Chapter 13 Inventory 659

CONTINUOUS AND INDEPENDENT DEMAND	662
Economic Order Quantity	662
Order Timing and Frequency	667
DECISION CONSIDERATIONS	669
Quantity Discounts	669
Planned Shortages	673
Economic Production Quantity	676
Risk and Uncertainty	681
Safety Stocks	682
Optimal Service Level	687
Inventory Systems	689

NONCONTINUOUS AND DEPENDENT DEMAND	692
Single-Period Inventory	692
Incremental Analysis	694
Material Requirements Planning	697
Other Considerations	703
Summary	705
Glossary	706
References	707
Thought Exercises	709
Technique Exercises	711
Applications Exercises	715
CASE: <i>Willington Hospital</i>	719

Chapter 14 Queuing Theory 721

STRUCTURE OF A QUEUING SYSTEM	723
Source Population	723
Arrival Process	723
Queue Accommodations and Behavior	730
Selection Process	731
Service Process	732
Departure	736
BASIC QUEUING ANALYSIS	736
Assumptions	737
Performance Measures	738
Comparative Analysis	742
Cost Considerations	744
PRACTICAL EXTENSIONS	746
Finite Source Population	746
Limited Waiting Capacity	749
Multiple Servers	751
Other Models	755
Summary	757
Glossary	758
References	759
Thought Exercises	760
Technique Exercises	763
Applications Exercises	766
CASE: <i>Sommerville Savings & Loan Association</i>	769

Chapter 15 Sequential Problems 772

MARKOV SYSTEMS	773
Characteristics	774
Transition Pattern	776
MARKOV ANALYSIS	778
State Probabilities	778
Matrix Approach	780
Steady State	783
Computer Analysis	788