Plasma
Physics and
Controlled
Nuclear Fusion
Research 1974
Volume 3

Fifth Conference Proceedings

PROCEEDINGS SERIES

PLASMA PHYSICS AND CONTROLLED NUCLEAR FUSION RESEARCH 1974

PROCEEDINGS OF THE
FIFTH INTERNATIONAL CONFERENCE ON PLASMA PHYSICS
AND CONTROLLED NUCLEAR FUSION RESEARCH
HELD BY THE
INTERNATIONAL ATOMIC ENERGY AGENCY
IN TOKYO, 11-15 NOVEMBER 1974

In three volumes

VOL. III

The following States are Members of the International Atomic Energy Agency:

AFGHANISTAN ALBANIA ALGERIA ARGENTINA AUSTRALIA ALISTRIA BANGLADESH BELGIUM BOLIVIA BRAZIL BULGARIA BURMA BYELORUSSIAN SOVIET SOCIALIST REPUBLIC CAMBODIA CANADA CHILE COLOMBIA COSTA RICA CUBA CYPRUS CZECHOSLOVAKIA DEMOCRATIC PEOPLE'S REPUBLIC OF KOREA DENMARK DOMINICAN REPUBLIC **ECUADOR** EGYPT EL SALVADOR **ETHIOPIA** FINLAND FRANCE GABON GERMAN DEMOCRATIC REPUBLIC GERMANY, FEDERAL REPUBLIC OF GHANA

GREECE

GUATEMALA

HAITI HOLY SEE HUNGARY **ICELAND** INDIA INDONESIA IRA N **IRAQ** IRELAND ISRAEL ITALY IVORY COAST IAMAICA **JAPAN** JORDA N KENYA KOREA, REPUBLIC OF KUWAIT LEBANON LIBERIA LIBYAN ARAB REPUBLIC LIECHTENSTEIN LUXEMBOURG MADAGASCAR MALAYSIA MALI **MAURITIUS** MEXICO MONACO MONGOLIA MOROCCO NETHERLANDS NEW ZEALAND NIGER **NIGERIA** NORWAY PAKISTAN

PARAGUAY PERH **PHILIPPINES** POLAND **PORTUGAL** ROMANIA SAUDI ARABIA SENEGAL. SIERRA LEONE SING APORE SOUTH AFRICA SPAIN SRI LANKA SUDAN SWEDEN SWITZERLAND SYRIAN ARAB REPUBLIC THAILAND TUNISIA TURKEY UGANDA UKRAINIAN SOVIET SOCIALIST REPUBLIC UNION OF SOVIET SOCIALIST REPUBLICS UNITED KINGDOM OF GREAT BRITAIN AND NORTHERN **IRELAND** UNITED REPUBLIC OF CAMPROON UNITED STATES OF AMERICA URUGUAY VENEZUELA VIET-NAM YUGOSLAVIÁ ZAIRE

ZAMBLA

The Agency's Statute was approved on 23 October 1956 by the Conference on the Statute of the IAEA held at United Nations Headquarters, New York, it entered into force on 29 July 1957. The Headquarters of the Agency are situated in Vienna. Its principal objective is "to accelerate and enlarge the contribution of atomic energy to peace, health and prosperity throughout the world".

PANAMA .

FOREWORD

Substantial progress towards the demonstration of the scientific feasibility of controlled fusion and towards the design and construction of the first controlled thermonuclear power reactor is shown in the three volumes of these Proceedings of the Fifth IAEA Conference on Plasma Physics and Controlled Nuclear Fusion Research.

The Conference, held in Tokyo from 11 to 15 November 1974, was organized by the Agency with the assistance and cooperation of the Japanese Government and the Japan Atomic Energy Research Institute. Nearly 500 participants from 24 countries and three international organizations attended. A total of 187 papers was presented on research ranging from plasma physics to the design of fusion reactors. The papers are published here in the original language; English translations of the Russian papers will be published in a Special Supplement of the Nuclear Fusion Journal.

By regularly organizing conferences on controlled nuclear fusion and by holding seminars and specialists' meetings on selected topics the Agency promotes the close international collaboration among plasma physicists of all countries. These activities will, we hope, contribute to the rapid use of this new source of energy by mankind.

EDITORIAL NOTE

The papers and discussions have been edited by the editorial staff of the International Atomic Energy Agency to the extent considered necessary for the reader's assistance. The views expressed and the general style adopted remain, however, the responsibility of the named authors or participants. In addition, the views are not necessarily those of the governments of the nominating Member States or of the nominating organizations.

Where papers have been incorporated into these Proceedings without resetting by the Agency, this has been done with the knowledge of the authors and their government authorities, and their cooperation is gratefully acknowledged. The Proceedings have been printed by composition typing and photo-offset lithography. Within the limitations imposed by this method, every effort has been made to maintain a high editorial standard, in particular to achieve, wherever practicable, consistency of units and symbols and conformity to the standards recommended by competent international bodies.

The use in these Proceedings of particular designations of countries or territories does not imply any judgement by the publisher, the IAEA, as to the legal status of such countries or territories, of their authorities and institutions or of the delimitation of their boundaries.

The mention of specific companies or of their products or brand names does not imply any endorsement or recommendation on the part of the IAEA.

Authors are themselves responsible for obtaining the necessary permission to reproduce copyright material from other sources

CONTENTS OF VOL.III

HIGH-BETA SYSTEMS I (Session XI)

MHD-stability of the Scyllac configuration (IAEA-CN-33/E 1-1)	3
G. Berge, J.P. Freidberg Plasma experiments in the Scyllac toroidal theta pinch (IAEA-CN-33/E 1-2) E.L. Cantrell, W.R. Ellis, H.W. Harris, F.C. Jahoda, R. Kristal, M.D. Machelek, I.B. McConnell, W.F. Origin, F.L. Bibs, C. A. Saures	13
M.D. Machalek, J.R. McConnell, W.E. Quinn, F.L. Ribe, G.A. Sawyer, F.T. Seibel, R.E. Siemon Discussion on papers IAEA-CN-33/E 1-1, E 1-2	23
Garching toroidal high-beta stellarator experiments (IAEA-CN-33/E 2) W. Braun, D. Correa, W. Engelhardt, E. Fünfer, J. Gruber, F. Herrnegger, M. Kaufmann, W. Köppendörfer, D. Lortz, W. Lotz, M. Münich, J. Neuhauser, W. Schneider, G. Schramm, U. Seidel, J. Sommer	25
Discussion on paper IAEA-CN-33/E 2	33
Plasma parameters and stability of the ZT-1 pinch experiment (IAEA-CN-33/E 3)	35
Discussion on paper IAEA-CN-33/E 3	45
The Garching Belt-Pinch experiments (IAEA-CN-33/E 4-1).	
G. Becker, A. Eberhagen, O. Gruber, H. Herold, J.M. Peiry, H. Röhr, R. Wilhelm, H. Zwicker	71
High-beta-confinement in TENQ, an axisymmetric toroidal experiment	
with non-circular cross-section (IAEA-CN-33/E 4-2)	57
K.H. Dippel, E. Graffmann, F. Hoenen, L. Janicke, A. Kaleck, H. Kever,	
L. Koenen, A. Nicolai, U. Plantikow, J. Schlüter	
Discussion on papers IAEA-CN-33/E 4-1, E 4-2	67
HIGH-BETA SYSTEMS II (Session XII)	
Импульсная тороидальная система с автономной камерой удержания (IAEA-CN-33/E 5)	71
А.Г. Еськов, О.А. Золотовский, А.Г. Калыгин,	-
Р.Х. Куртмуллаев, Я.Н. Лаухин, А.И. Малютин, А.И. Маркин, А.П. Прошлецов, В.Н. Семенов	
(Pulsed toroidal system with automated confinement chamber:	
A.G. Es'kov et al.)	
Etude de l'émission neutronique et de la turbulence dans l'expérience Focus avec	
une résolution temporelle de l'ordre de la nanoseconde (IAEA-CN-33/E 6-1)	83

Comparative studies of plasma focus devices (IAEA-CN-33/E 6-2)	99
Observation of 10 ⁸ Gauss fields and production of 14-MeV D-T neutrons	
in a deuterium plasma (IAEA-CN-33/E 6-3)	109
W.H. Bostick, V. Nardi, W. Prior	
Анализ геометрии, динамики и магнитной структуры плазменного	
фокуса метод ом лазерной интерферометрии	
(IAEA-CN-33/E 6-4)	123
Н.В. Филиппов, В.Д. Иванов, М.П. Моисеева,	
М.М. Степаненко, Н.К. Сухарева	
(Analysis of the geometry, dynamics and magnetic structure of a plasma pinch by	
the laser interferometry method: N.V. Filippov et al.)	
Процессы вблизи границы плазма-металл в режимах со	
"срывом" в системах типа "плазменный фокус"	
(IAEA-CN-33/E 6-5)	133
Н.В. Филиппов, С.В. Базденков, И.Ф. Беляева,	
В.А. Безбатченко, К.Г. Гуреев, Т.И. Филиппова,	
В.С. Имшенник, Я.М. Каждан, Л.А. Плинер	
(Process near the plasma-metal boundary under disruptive conditions in plasma	
focus systems: N.V. Filippov et al.)	
Discussion on papers IAEA-CN-33/E 6-1, E 6-2, E 6-3, E 6-4, E 6-5	
Роль самоорганизации пинчевых разрядов в нагреве	1.40
и удержании плазмы (IAEA-CN-33/E 6-6)	149
И.Ф. Кварцхава, Ю.В. Матвеев, И.Я. Бутов	
А.А. Самарский, С.П. Курдюмов, Ю.П. Попов	
(The importance of self-forming processes in pinch discharges for plasma heating	
and confinement: I.F. Kvartskhava et al.)	r
A keV collisionless theta-pinch plasma confined in the caulked-cusp torus (CCT) field (IAEA-CN-33/E 7-1)	1.61
· · · · · · · · · · · · · · · · · · ·	101
T. Uchida, K. Sato, N. Noda, T. Aizawa, Y. Osanai, T. Itagaki, R. Akiyama Screw pinch shaped by toroidal-current-bar control (IAEA-CN-33/E 7-2)	171
	171
K. Yokoyama, Y. Nogi, M. Ito, T. Itagaki, I. Kawakami, H. Yoshimura Stability and toroidal equilibrium conditions of a theta-pinch plasma in a	
multiple mirror field (IAEA-CN-33/E 7-3)	101
T. Itagaki, T. Karakizawa, K. Saito, S. Shiina, J. Todoroki	101
Discussion on papers IAEA-CN-33/E 7-1, E 7-2, E 7-3	102
Discussion on papers transcressife 1-1, E 1-2, E 1-3	173
	13
PLASMA HEATING (Session XIII)	
Progress on CO. Joseph and Surjey (LABA CNL 22/C L 1)	107
Progress on CO ₂ laser gas fusion (IAEA-CN-33/C 1-1)	197
O.C. Vuises, H. Rutkowski, A. Hertzberg, A. Hoffman, L. Steinnauer,	
J. Dawson, D.R. Cohn, W. Halverson, B. Lax, J.D. Daugherty,	
J.E. Eninger, E.R. Pugh, T.K. Chu, L.C. Johnson, R.V. Lovelace Self-focusing and filamentation of laser light in plasmas (IAFA-CN-33/C 1-2)	207
Self-focusing and filamentation of laser light in plasmas (IAEA-CN-33/C 1-2)	201
CO ₂ laser breakdown and heating of hydrogen in a magnetic mirror field	
(IAEA-CN-33/C 1-3)	217
A.A. Offenberger, N.H. Burnett	
Discussion on papers IAEA-CN-33/C 1-1, C 1-2, C 1-3	229

Theoretical studies of plasma heating by relativistic electron beams	
(IAEA-CN-33/C 2-1)	23
K. Papadopoulos, K.R. Chu, R.W. Clark, T. Coffey, R.C. Davidson,	
I. Haber, C. Kapetanakos, M. Lampe, R. Lee, P.C. Liewer,	
W. Manheimer, R. Shanny, P. Sprangle, C.D. Striffler, C.E. Wagner	
Plasma heating using strong turbulence and relativistic electron beams	
(IAEA-CN-33/C 2-2)	241
R.E. Kribel, C.E. Ekdahl, M. Greenspan, J. Sethian, F. Sandel,	1
C.B. Wharton	
Plasma heating with a rotating relativistic electron beam (IAEA-CN-33/C 2-3)	249
K. Molvig, N. Rostoker, F. Dothan	
Нагрев плазмы мощным релятивистским электронным пучком	
в сильном магнитном поле (IAEA-CN-33/C2-4)	257
А.В. Аржанников, Б.Н. Врейзман, Л.Н. Вячеславов,	
В.С. Койдан, В.В. Конюков, Д.Д. Рютов	
(Heating of a plasma by a powerful relativistic electron beam in a strong magnetic	,
field: A.V. Arzhannikov et al.)	
Discussion on papers IAEA-CN-33/C 2-1, C 2-2, C 2-3, C 2-4	269
Turbulent heating of plasmas in high magnetic fields by means of strong currents	
(IAEA-CN-33/C 3-1)	271
H. Schrijver, W.R. Rutgers, J.A. Van Elst, H.A. Post, H.W. Kalfsbeek,	•
H.W. Piekaar, H. De Kluiver	
Dynamic behaviour of turbulent heating of plasmas (IAEA-CN-33/C 3-3)	28,7
Y. Nakagawa, M. Tanikawa, K. Watanabè, K. Adati, H. Iguchi, K. Ishii,	
Y. Ito, J. Jacquinot, T. Kawabe, T. Kawamura, K. Mulaoka, T. Oda, R. Sugihara	* *.
Turbulent heating of plasma in toroidal experiments (IAEA-CN-33/C 3-4)	299
A. Hirose, Y. Amagishi, M.R. Shubaly, H.M. Skarsgard, B.F. White	
Discussion on papers IAEA-CN-33/C 3-1, C 3-3, C 3-4	307
Parametric instabilities of plasmas in the frequency ranges $\omega \gtrsim \omega_{LH}$ and $\omega < \omega_{LH}$	-
(IAEA-CN-33/C 4-1)	309
A. Rogister, G. Hasselberg, K.D. Harms	
Radio-frequency heating of large thermonuclear tori (IAEA-CN-33/C 4-2)	319
A.M. Messiaen, P.E.M. Vandenplas	
A new low-frequency parametric instability and its effect on toroidal plasma	
diffusion (IAEA-CN-33/C 4-3).	333
E. Canobbio	
Discussion on papers IAEA-CN-33/C 4-1, C 4-2, C 4-3	345
	1
HIGH-BETA SYSTEMS III (Session XIV)	
St. BETT STOTE III (BUSSION ALT)	
Heating, relaxation and stability of collisionless high-β-plasma in straight theta-	
1 1 CLER COLONIO AN	349
P. Bogen, K.J. Dietz, E. Hintz, K. Höthker, Y.T. Lie, A. Pospieszczyk	349
A Acceptant light to the first term of the contract of the con	365
E. Oktay, A.W. Desilva, P.C. Liewer, Y.G. Chen, H.R. Griem, R. Hess,	203
N.A. Krall	
The section to the section of the se	373
N.A. Krall, S. Hamasaki, R.C. Davidson, P.C. Liewer, C. Wagner, N.T. Gladd,	
D.W. Hewett, C.W. Nielson, T.A. Oliphant, A.G. Sgro	

Implosion heating studies in the Scylla 1B, implosion heating, and staged theta-pinch experiments (IAEA-CN-33/E 8-4)	389			
(IAEA-CN-33/E 8-6) R. Chodura, C.T. Dum, M. Keilhacker, M. Kornherr, H. Niedermeyer, R. Protz, F. Söldner, KH. Steuer				
Discussion on papers IAEA-CN-33/E 8-1, E 8-2, E 8-3, E 8-4, E 8-5, E 8-6				
reversed-field pinch (1AEA-CN-33/E 9-2) E.P. Butt, C.W. Gowers, R.F. Gribble, Li Yin-An, A.A. Newton, B.A. Norton, D.C. Robinson, A.J.L. Verhage, H.A.B. Bodin, J.C. Taylor, W.J. Sharp	417			
Reverse-field-pinch experiments in the ETA-BETA device (IAEA-CN-33/E 9-3) A. Buffa, S. Costa, L. Fellin, G. Malesani, P.L. Mondino, G.F. Nalesso, S. Ortolani, G. Rostagwi, A. Stella	431			
Toroidal pinch experiment in ETL TPE-1 (IAEA-CN-33/E 9-4) K. Ogawa, S. Kiyama, Y. Maejima, T. Shimada, Y. Hirano, I. Hirota, Y. Sato, S. Takeda, E. Yahagi, T. Tamaru				
Experiment on STP, an axisymmetric fast toroidal pinch with very small aspect ratio (1AEA-CN-33/E 9-5)	463			
M. Wakatani Computer simulation of a toroidal pinch (IAEA-CN-33/E 9-6)	471			
Discussion on papers IAEA-CN-33/E 9-1, E 9-2, E 9-3, E 9-4, E 9-5, E 9-6	481			
FUSION REACTOR STUDIES (Session XV)				
Design of a minimum-size toroidal DT experimental reactor (FINTOR) (IAEA-CN-33/G 1-1) E. Bertolini, B. Brunelli, F. Engelmann, M. Hoffman, N. Merzagora, ' G. Pasotti, M. Ricci, N. Sacchetti, G. Sacerdoti, M. Spadoni, M. Biggio, G. Casini, R. Cuniberti, F. Farfaletti-Casali, F. Peter, S. Bobbio, E. Coccorese, L. Egiziano, O. Greco	485			
Major design features of the conceptual D-T tokamak power reactor, UWMAK-II (IAEA-CN-33/G 1-2) R. W. Conn, G. L. Kulcinski, M. A. Abdou, R. W. Boom, G. A. Emmert, J. Kesner, C. W. Maynard, A.T. Mense, J. E. Scharer, T. Sung, I. Sviatoslavsky, D. Sze, W. Vogelsang, L. Wittenberg, T. Yang, W. Young	497			

Fusion dynamics of lossy reactor systems and power balance implications (IAEA-CN-33/G 1-3)			
J. Rand McNally, Jr., J.F. Clarke, R.H. Fowler, T. Hiraoka, R.D. Sharp,	511		
D. Steiner			
The Princeton reference design fusion power plant (IAEA-CN-33/G 1-4)	525		
W.G. Price, Jr.	323		
·	535		
Design study of a tokamak reactor (IAEA-CN-33/G 1-5)	333		
Y. Ohkubo, T. Takeda, S. Mori			
	549		
Discussion on papers IAEA-CN-33/G 1-1, G 1-2, G 1-3, G 1-4, G 1-5			
Computational studies of two-component mirror reactors (IAEA-CN-33/G 2-1) J.A. Byers, R.P. Freis, J. Killeen, E.P. Lee, B. McNamara, A.A. Mirin,	551		
M.E. Rensink			
Parametric survey for the linear two-component system (IAEA-CN-33/G 2-2)	557		
· · · · · · · · · · · · · · · · · · ·	540		
Two-energy-component toroidal fusion devices (IAEA-CN-33/G 2-3)	202		
H.L. Berk, H.P. Furth, D.L. Jassby, R.M. Kulsrud, C.S. Liu,			
M.N. Rosenbluth, P.H. Rutherford, F.H. Tenney, T. Johnson,			
J. Killeen, A.A. Mirin, M.E. Rensink, C.W. Horton, Jr.			
Discussion on papers IAEA-CN-33/G 2-1, G 2-2, G 2-3	581		
Direct conversion of plasma energy to electricity for mirror fusion reactors			
(IAEA-CN-33/G 3-1)	583		
R.W. Moir, W.L. Barr, G.A. Carlson			
Conceptual design of a mirror reactor for a fusion engineering research facility			
(FERF) (IAEA-CN-33/G 3-2)	593		
T.H. Batzer, R.C. Burleigh, G.A. Carlson, W.L. Dexter, G.W. Hamilton,			
A.R. Harvey, R.G. Hickman, M.A. Hoffman, E.B. Hooper, Jr., R.W. Moir,			
R.L. Nelson, L.C. Pittenger, B.H. Smith, C.E. Taylor, R.W. Werner, T.P. Wilcox			
Engineering design of a fusion test reactor (FTR) and fusion engineering research			
facility (FERF) based on a toroidal theta pinch (IAEA-CN-33/G 3-3)	605		
M. Abdou, R.J. Burke, P.V. Dauzvardis, M. Foss, S.A.W. Gerstl,			
V.A. Maroni, A.W. Pierce, A.F. Turner, R.A. Krakowski, R.K. Linford,			
T.A. Oliphant, F.L. Ribe, K.I. Thomassen			
Discussion on papers IAEA-CN-33/G 3-1, G 3-2, G 3-3	617		
Heliotron as a steady fusion reactor (IAEA-CN-33/G 4)	619		
A. liyoshi, K. Uo			
The pulsed reversed-field pinch reactor (IAEA-CN-33/G 5)	631		
H.A.B. Bodin, E.P. Butt, R. Carruthers, T.E. James, A.A. Newton,			
G. Rostagni			
The Interesting possibilities of fusion-fission (IAEA-CN-33/G 6-1)	641		
R.W. Werner, J.D. Lee, R.W. Moir, G.A. Carlson, M.A. Peterson,	٠.,		
W.C. Wolkenhauer, B.R. Leonard, Jr.			
Progress toward the development of a mirror hybrid (fusion-fission) reactor			
(IAEA-CN-33/G 6-2)	640		
B.R. Leonard, Jr., W.C. Wolkenhauer	047		
SUMMARY OF THE CONFERENCE (Session XVI)			
Summary of magnetic confinement (experiments)	659		

Summary of plasma theory		665
B.B. Kadomtsev		
Discussion on summary paper by B.B. Kadomtsev.		671
Summary of reactor systems		
S. Mori	$(\mathbf{x}_{t}, \dots, \mathbf{x}_{t}) = (\mathbf{x}_{t}, \dots, \mathbf{x}_{t})$	
	* * *	
Corrigendum to paper by J.G. Cordey, Vol.1, p.623		67 7
Chairmen of Sessions, and Secretariat of the Conference		679
List of Participants		681
Author index		707
Transliteration index		719
	• • • • • • • • • • • • • • • • • • • •	, 1,

Session XI HIGH-BETA SYSTEMS I

Chairman: C.M. BRAAMS (The Netherlands)

Papers E 1-1 and E 1-2 (Scyllac) were presented by G.A. SAWYER as Rapporteur

Papers E 4-1 and E 4-2 (Belt pinch) were presented by H. ZWICKER as Rapporteur

MHD-STABILITY OF THE SCYLLAC CONFIGURATION

G. BERGE*, J. P. FREIDBERG
University of California,
Los Alamos Scientific Laboratory,
Los Alamos, N. Mex.,
United States of America

Abstract

MHD-STABILITY OF THE SCYLLAC CONFIGURATION.

The results of a stability analysis for a diffuse high- θ , $\ell=1$ helical configuration are presented. It is shown that there exists a gross m=1 mode whose properties are quite similar to those predicted by the sharp-boundary model. In addition, two new classes of m=1 modes are found, one localized on the inside of the plasma, the other one outside. For any monotonic pressure profile, these modes are unstable although their growth rates are very small. A further study suggests that small changes in the profile may stabilize these modes:

I. Introduction

The basic idea of the Scyllac configuration is to create a toroidal high β equilibrium possessing many of the desirable properties of linear θ pinches but eliminating the end loss. Toroidal equilibrium is achieved [1,2] by superposing a small $\ell=1$ helical field and an even smaller $\ell=0$ bumpy field on the basic θ pinch configuration.

With regard to stability the e-pinch field is essentially neutral. The $\ell=0$ field required for equilibrium is so small that in many cases it can be neglected in the stability analysis. Consequently it is the $\ell=1$ field which determines the stability of the system.

Most of the theory to date has been concerned with the m=1, k=0 mode of a straight, $\ell=1$, helical system, as this appears to be the most important mode observed experimentally.[3,4] In addition, almost all of the calculations have treated the sharp boundary, constant pressure model. The results of these theories indicate that the m=1, k=0 instability is very subtle. Several different mathematical expansions have been devised and in each case instabilities, when they exist, occur as higher order effects in some appropriate expansion parameter.

The first of these theories, [5,6] referred to as the "old ordering", treats the case where the helical fields are assumed small but allows a finite helical period. In this case an instability arises basically due to the bad curvature associated with the £=l field. A second theory, [7] referred to as the "new ordering" assumes that the helical fields are finite but requires a long helical period. Here, instabilities can occur if the harmonic content of the £=l field is not properly adjusted. Finally a hybrid calculation[8] which includes the destabilizing effects of the £=l curvature and a particular harmonic content in the £=l field, indicates that the £=l curvature effect dominates in the range of current experimental parameters. This result is consistent with experimental measurements.[3,4]

^{*} Permanent address: University of Bergen, Bergen, Norway.

All of the sharp boundary models also predict a dipole wall stabilization term. In current experiments with highly compressed plasmas, this effect is negligible. It will become very important, however, in future experiments.[9]

Diffuse $\ell=1$ stability calculations[10,11] have been performed, but only using a very primitive ordering scheme which excludes all the known destabilizing terms. They do include the wall stabilization effect and the results are qualitatively similar to those of sharp boundary theory.

In the present calculation we examine the stability of a diffuse £=1 system using the old ordering expansion, since this theory appears to give rise to the most dangerous modes. Growth rates and eigenfunctions are calculated for a wide range of parameters. We find that there exists a gross mode which behaves qualitatively the same as the sharp boundary predictions, although the growth rates are somewhat lower. This mode can also be wall stabilized. In addition, for monotonic pressure profiles, two new classes of modes are found. One is localized on the inside of the plasma and the other on the outside. In general their growth rates are quite small. The exterior mode can be wall stabilized but the interior mode is present for any monotonic profile. A further study suggests that very slightly hollow profiles on the inside and flat profiles (i.e., zero 6 pinch current) on the outside could eliminate the new classes of unstable modes.

II. Equilibrium

We consider the equilibrium of a diffuse high β helically symmetric system governed by the ideal MHD equations. Because of the helical symmetry, it is possible to describe the equilibrium quantities in terms of a single flux function, ψ ,[12] which satisfies a partial differential equation of the form

$$\frac{1}{r} \frac{\partial}{\partial r} \frac{r}{1 + h^2 r^2} \frac{\partial \psi}{\partial r} + \frac{1}{r^2} \frac{\partial^2 \psi}{\partial \phi^2} = \frac{2 I}{(1 + h^2 r^2)^2} - \frac{1}{h^2} \left[\mu_0 p' + \frac{1}{2} \frac{(I^2)'}{1 + h^2 r^2} \right] \tag{1}$$

where φ = θ + hz is the helical angle and $p(\psi)$, $I(\psi)$ are two arbitrary functions of ψ .

This equation is solved using the old Scyllac expansion: that is we write $\psi(\mathbf{r},\phi)=\psi_0(\mathbf{r})+\psi_1(\mathbf{r})\cos\phi$ It then follows that $\psi_1(\mathbf{r})$ must satisfy the following equation

$$\left(\frac{r\psi_1'}{1+h^2r^2}\right)' - \left[\frac{1}{r} + \frac{1}{B} \left(\frac{rB'}{1+h^2r^2}\right)'\right]\psi_1 = 0$$
 (2)

where B(r) $\equiv \psi_0'$ (r)/r, the leading order 0 pinch field, is an arbitrary function of r. The boundary conditions on $\psi_1(r)$ are

$$\Psi_1(0) = 0$$

$$\Psi_1(b) = \frac{2I'_1(hb)}{hb} \frac{B_{\ell}}{B_0}$$
(3)

where I_1 is the modified Bessel function, h is the helical pitch number, B_0 is the amplitude of the applied θ pinch field far away from the plasma, b is the mean radius of the outer conducting shell and B_{ϱ} is the amplitude of the helical field[3] on axis without any plasma.

The magnetic fields are given in terms of ψ_1 as follows

$$B_{r}(r,\phi) = B_{r}(r) \sin \phi , \qquad B_{r}(r) = \frac{h\psi_{1}}{r}$$

$$B_{\theta}(r,\phi) = B_{\theta}(r) \cos \phi , \qquad B_{\theta}(r) = \frac{1}{1+h^{2}r^{2}} \left[\psi'_{1} - \frac{B'}{B} \psi_{1} \right]$$
(4)

The results presented here were obtained by solving Eq. (2) numerically for the rigid rotor profile

$$B(r) = B_0 \tanh (r^2/\gamma + \alpha)$$

$$\rho(r) = \rho_0 \operatorname{sech}^2(r^2/\gamma + \alpha)/\operatorname{sech}^2\alpha$$
(5)

where $\rho(r)$ is the density, $\alpha=\tanh^{-1}\sqrt{1-\beta}$ (here β is measured on axis), ρ_0 is the density on axis, and $Y=a^2[1+\sqrt{1-\beta}]$ with a the equivalent line density radius (i.e., line density $N=\pi\rho_0a^2$).

III. Stability

The equilibrium just described was tested for stability in the ideal MHD model. By using a proper normalization, we are able to compute actual growth rates. This is important, because the simpler question of determining thresholds (i.e., marginal stability) is essentially impossible as a result of the complicated nature of the frequency spectrum.

Since the equilibrium is two dimensional, it is possible to Fourier analyze with respect to any independent (but not necessarily orthogonal) third coordinate. Thus all perturbed quantities can be assumed to vary as exp[i(me+kz)], m and k arbitrary but k/m not commensurate with h. In this work we treat only m=1, because (1) m=1 appears to be the most dangerous mode experimentally (2) theory predicts that $m\geq 2$ modes, which are MHD unstable may well likely be stabilized by finite gyro radii effects.[13] In addition we treat the k=0 mode, since it can be shown theoretically[14] that this is the worst k. Under these conditions the m=1 eigenfunction has the form

$$\xi_r = \xi \sin\theta + \eta_1 \sin\theta \cos\phi + \eta_2 \cos\theta \sin\phi$$

$$\xi_{\theta} = (r\xi)' \cos\theta + \tilde{\eta}_1 \sin\theta \sin\phi + \tilde{\eta}_2 \cos\theta \cos\phi$$
(6)

Here ξ represents the basic_m=1, k=0 displacement and $n_1,\ n_2,\ \bar{n}_1,\ \bar{n}_2$ are small sideband distortions, consistent with the old ordering, and which are required to produce instability. Note that there are two additional sidebands possible (with conjugate phase) for both ξ_r and ξ_θ . These terms are not included because they are always stabilizing.[14]

Equation (6) is substituted into the MHD energy principle with proper normalization and a minimization is performed with respect to $\bar{\eta}_1$ and $\bar{\eta}_2$. After a lengthy calculation, we arrive at the linearized equations of motion which can be written in the following convenient form

$$\underline{\underline{Z}}_{1}' = \underline{\underline{Z}}_{2}$$

$$\left[(\underline{\underline{A}} - \underline{\omega}^{2} \underline{\underline{D}}) \cdot \underline{\underline{Z}}_{2} \right]' = (\underline{\underline{B}} - \underline{\omega}^{2} \underline{\underline{E}}) \cdot \underline{\underline{Z}}_{1} + \underline{\underline{C}} \cdot \underline{\underline{Z}}_{2}$$
(7)

where Z_1 and Z_2 are the vectors

$$\underline{Z}_1 = \begin{pmatrix} \xi \\ \chi \\ \phi \end{pmatrix}$$
, $\underline{Z}_2 = \begin{pmatrix} \xi' \\ \chi' \\ \phi' \end{pmatrix}$

with χ and ϕ related to $\xi,~\eta_1$ and η_2 by

$$\chi = - hr(n_1 + n_2)/2 + (B_r/B)r\xi'$$

$$\phi = hr(n_1 - n_2)/2$$

The matrices \underline{A} , \underline{B} , \underline{C} , \underline{D} , and \underline{E} are given by

$$\underline{\underline{A}} = \begin{pmatrix} a_1 & a_2 & a_3 \\ a_2 & a_9 & 0 \\ a_3 & 0 & a_7 \end{pmatrix} , \underline{\underline{B}} = \begin{pmatrix} 0 & -a'_4 & -a'_5 \\ 0 & a_8 & 0 \\ 0 & 0 & a_8 \end{pmatrix}$$

$$\underline{\underline{C}} = \begin{pmatrix} 0 & -a_4 & -a_5 \\ a_4 & 0 & 0 \\ a_5 & 0 & 0 \end{pmatrix}, \quad \underline{\underline{D}} = \begin{pmatrix} a_{10} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \underline{\underline{E}} = \begin{pmatrix} a_6 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

where

$$a_{1} = \frac{2r[B_{r}-B_{\theta}-h^{2}r^{2}B_{\theta}/2]^{2}}{4+h^{2}r^{2}} + \frac{h^{2}r^{3}B_{\theta}^{2}}{2} , \qquad a_{6} = -2\omega^{2}r^{2}\rho$$

$$a_{2} = \frac{2rB[B_{r}-B_{\theta}-h^{2}r^{2}B_{\theta}/2]}{4+h^{2}r^{2}} , \qquad a_{7} = 2B^{2}/h^{2}r$$

$$a_{3} = rBB_{\theta} , \qquad a_{8} = 2B^{2}/r$$

$$a_{4} = B(B_{r}-B_{\theta}) , \qquad a_{9} = \frac{2rB^{2}}{4+h^{2}r^{2}}$$

$$a_{5} = -B(B_{r}+B_{\theta}) , \qquad a_{10} = 2\omega^{2}r^{3}\rho$$

The boundary conditions are $Z_1(0)=0$ and $Z_1(b)=0$ which corresponds to a perfectly conducting wall at a mean radius b. Note, that the plasma extends to the wall, and thus there is no vacuum region.