# Artificial Intelligence and Statistics

Edited by

William A. Gale

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AT&T Bell Laboratories



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## Preface

This book will be of interest to statisticians or AI researchers who want to apply AI techniques in statistics. It will also be of interest to AI researchers or statisticians studying propagation of uncertainty or learning (clustering, concept formation).

Most of the papers in this book were prepared for the Workshop on Artificial Intelligence and Statistics, held in April 1985. Most of the talks presented at the Workshop are represented here by papers.

My intention in arranging the Workshop was to raise the visibility of the possible applications of AI in statistics and of statistics in AI. The goal was to bring together people interested in the various interactions of AI and statistics, giving a broader view of the total work at this point than would be possible for any one group. AT&T Bell Laboratories, which has been a leader in developing applications of AI in statistics, agreed to sponsor the Workshop.

The Workshop was a catastrophe of success, attracting four times as many requests to attend as I had planned space for, and not all could be accommodated at the Workshop. It therefore seemed that it would be worth preparing a book based on the conference to give those who could not be at the Workshop access to the papers presented there.

This book substantially increases the published literature on AI in statistics and contains some important contributions from statistics to AI. It can give you a working knowledge of current capabilities in the application of AI to statistics or some suggestions of useful research in applying statistics to AI. All the papers contain new results, and some present in-depth reviews of specific areas.

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Murray Hill, N.J.

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## Contents

	•
1.	Overview 1
	William A. Gale
1.1	Opportunities 1
1.2	Background 4
1.3	Introduction to Chapters 10.
2.	A Statistical View of Uncertainty in Expert Systems 17
	David J. Spiegelhalter
2.1	Introduction 17
2.2	The Aims of Expert Systems 18
2.3	Uncertainty in Expert Systems 20
2.4	Probability: Is It Appropriate, Necessary, or Practical? 31
2.5	Expert Systems and Subjectivist Bayesian Statistics 33
2.6	Aspects of Probabilistic Reasoning 39
2.7	Conclusions 48
3.	Knowledge, Decision Making, and Uncertainty 57
	John Fox
3.1	Introduction 57
3.2	A Brief Review of Uncertainty in Expert Systems 59
3.3	A Generalized View of Belief 61
3.4	An Analysis of Knowledge and Belief 62
3.5	Applications 66
3.6	Precision and the Attachment of Numerical Procedures 67
3.7	Combination of Beliefs 69
3.8	Validity 71
3.9	Conclusion and Postscript 72
4.	Conceptual Clustering and Its Relation to Numerical Taxonomy 77
	Douglas Fis <b>her</b> Pat Langley
4.1	Introduction 77
4.2	Numerical Taxonomy and Conceptual Clustering 78

4.3 4.4 4.5	Some Conceptual Clustering Algorithms 91 Concluding Remarks 113
5.	Learning Rates in Supervised and Unsupervised Intelligent Systems 117
	Stephen C. Hora
5.1 5.2 5.3 5.4 5.5 5.6 5.7 5.8	Introduction 117 Existing Results for Obtaining Learning Rates 118 Developing the Inefficiencies 119 Likelihood Theory 121 Comparing Supervised and Unsupervised Learning 122 Learning on Demand 126 Extensions to a Larger Problem Domain 129 Additional Topics 129
6.	Pinpointing Good Hypotheses with Heuristics 133
	Steven Salzberg
6.1 6.2 6.3 6.4 6.5 6.6	Introduction 133 The Straightforward Approach: Statistics 134 Heuristics for Pruning Search 139 Rationalization 153 HANDICAPPER's Performance and Conclusions 154 Conclusions 155
7.	Artificial Intelligence Approaches in Statistics 159
	Robert I. Phelps P. B. Musgrove
7.1 7.2 7.3 7.4	Introduction 159 Al Approaches in Statistics 160 Cluster Discrimination 161 Discussion 170
8.	REX Review 173
	William A. Gale
8.1 8.2 8.3	Introduction 173 Summary 174 How REX Looks to the User 176

8.4 8.5 8.6 8.7	Why We Built REX 194 The Inference Engine 201 Strategy 222 Conclusions 225
9.	Representing Statistical Computations: Toward  a Deeper Understanding 229
	Thomas Ellman
9.1 9.2 9.3 9.4 9.5 9.6	Introduction 229 Representing Statistical Computations 230 Generating Explanations 233 Extensions to the Representation 235 Using the Representation to Aid Knowledge Acquisition 237 Conclusions 238
10.	Student Phase 1 - A Report on Work in Progress 239
	William A. Gale
10.1 10.2 10.3 10.4 10.5	Overview 239 Acquiring and Using Initialization Knowledge 246 Learning How to Detect and Fix Problems 253 Inference Techniques 257 Control Modules 262
11.	Representing Statistical Knowledge for Expert Data Analysis Systems 267
	Ronald A. Thisted
11.1 11.2 11.3 11.4 11.5	Groundwork; A Context for Expert Systems Research in Data Analysis 267 Knowledge Engineers, Statistical Consultants, and Computers 273 A Paradigm for Data Analysis 275 Strategies for Data Analysis 278 A Brief Note on the Semantic Map 281
12.	Environments for Supporting Statistical Strategy 285
	Peter J. Huber
12.1 12.2	Background: The Data Analysis Paradigm 285 The Human-Human Interaction and Implications for System Design 287

12.3 12.4 12.5 12.6	The Data Analysis Environment 287 Analysis Sessions and Record Keeping 288 The Laboratory Assistant 289 Artificial Intelligence and Expert Systems 291
13.	Use of Psychometric Tools for Knowledge Acquisitions A Case Study 295
	Keith A. Butler James E. Corter
13.1	Introduction 295
13.2	Knowledge Transfer Task Requirements 296
13.3	Measurement Models and Scaling Methods 300
13.4	Unidimensional Scaling 300
13.5	Case Study: Using EXTREE to Guide Feature Elicitation Interviews 307
13.6	Discussion 313
14.	The Analysis Phase in Development of Knowledge Based Systems 321
	Annie G. Brooking
14.1	Introduction 321
14.2	Analysis 323
14.3	The Human Analysis Approach 325
14.4	The Knowledge Elicitation Phase 326
14.5	Phases in Knowledge Elicitation 328
14.6	The Knowledge Engineer 331
14.7	Conclusion 333
15.	Implementation and Study of Statistical Strategy 335
	R. Wayne Oldford
	Stephen C. Peters
15.1	Introduction 335
15.2	The Problem 336
15.3	What Can Be Done? 339
15.4	Implementing Low-level Strategies 341
15.5	Implementing Higher-level Strategies 344
15.6	Evaluation 348
15.7	Summary and Concluding Remarks 349

16.	Patterns in Statistical Strategy 335
	David J. Hand
16.1	Introduction 356
16.2	Types of Statistical Expert System 357
16.3	The Structure of the Strategy of Statistical Analysis 358
16.4	MANOVA Strategy 364
16.5	Discriminant Analysis 371
16.6	The Role of Artificial Intelligence Techniques 373
16.7	Conclusion 375
	Appendix 1: Examples of Interviews by Keyboard 376
17.	A DIY Guide to Statistical Strategy 389
	Daryl Pregibon
17.1	Introduction 389
17.2	Some Do's and Don'ts of Strategy Development 390
17.3	Developing Your Strategy 392
17.4	Implementation 395
17.5	Epilogue 399
18.	An Alphabet for Statisticians' Expert Systems 401
	John Tukey
18.1	A Is for All-Importance, Amelioration, and Areas 401
18.2	B Is for Branching 402
18.3	C Is for Cycles, Costs, Complexity, and Cheap Pie
	in the Sky 403
18.4	D Is for Difficulties, Dangers, Development,
	and Data-Dredging 404
18.5	E Is for Education 406
18.6	F Is for Fix-It, Functionality, and the Future 407
	-

## Overview of Artificial Intelligence and Statistics

William A. Gale

### 1.1 OPPORTUNITIES

Exciting applications of Artificial Intelligence (AI) technology are opening a new field of research in statistics. This new field seeks to integrate previously known tests and transformations into coherent total approaches to data analysis. This is AI in statistics. At the same time, AI researchers are turning to work by statisticians in seeking solutions to problems involving uncertainty. Representing the uncertainty of conclusions established from uncertain facts by uncertain rules is one such problem. This is statistics in AI. The chapters in this book represent the first stage of the development of AI in statistics, as well as a continuation of statistics in AI, and are together a report on AI and statistics.

The key use of AI in statistics has been to enable statisticians to study strategies of data analysis. The term strategy has been used to denote a coherent total approach to a data analytic task, following Chambers (1981). However, there is, as yet no generally accepted definition of this term. Daryl Pregibon and I (Gale and Pregibon, 1982) suggested that a definition would be the answer to questions such as

<sup>&</sup>quot;What do I look for?"

<sup>&</sup>quot;When do I look for it?"

<sup>&</sup>quot;How do I look for it?"

<sup>&</sup>quot;Why do I look for it?"

<sup>&</sup>quot;What do I have to do to look for it?"

In Chapter 15 of this book, Wayne Oldford and Steve Peters write "The term 'statistical strategy' will be used here to label the reasoning used by the experienced statistician in the course of the analysis of some aspect of a substantive statistical problem." David Hand, in Chapter 16, writes "statistical strategy has been defined as a formal description of the choices, actions, and decisions to be made while using statistical methods in the course of a study." These definitions give the general flavor of the subject matter beginning to be addressed.

We need to make statistical strategy available to more people to prevent misuse of statistical packages. Statisticians have frequently noted that current statistical packages are open to misuse, as will be clear from the background discussion that follows. The current packages provide excellent numerical processing, but the user is responsible for determining whether the processing is appropriate, and what the results mean. Statistical strategy is simply missing from the packages and is necessary to use the packages wisely. Mechanization of statistical strategy would make it widely available.

The tools developed by AI may allow us to mechanize statistical strategy. In the last decade AI researchers have demonstrated techniques for mechanizing symbolic information processing tasks that otherwise would have been assumed to be the preserve of human intelligence. These tasks include understanding the spoken or written word, interpreting still or moving images, and solving intellectual problems from playing chess to synthesis of complex molecules. In particular, the widespread success of "expert systems" in addressing problems in other fields has suggested that they might prove useful in statistics. (Fox (1985) is a readable introduction to expert systems.) AI techniques have been used in statistics for provocative demonstrations that software can now be written to do such things as translate a medical hypothesis into a statistical study, help a user select an appropriate statistical technique, and check automatically for the validity of the assumptions behind a statistical technique.

Now that several systems have demonstrated the utility of AI techniques in statistics, leading statisticians have begun to point out the opportunities for research. John Tukey (1985) recently pointed out to a meeting of statisticians "we have been unwilling to think hard about what our strategies (not just individualized tactics) really have been or should be," and "one just cannot build an expert system without thinking through a strategy." A major advantage of mechanization for statisticians is that it will support systematic testing and analysis of strategies. David Cox, one of the few statisticians to think about strategies before AI methods made them testable (Cox and Snell, 1981), spoke at the same meeting citing the need for "provision of concepts to guide the strategy of the collection and analysis of data" (Cox, 1985).

Although AI has contributed to many areas, statistics is one of relatively few discipances that can contribute back to AI. Statistics has focused on

Overview 3

numerical methods for estimating limits to knowledge when measurements have a random component, whereas AI has been concerned with symbolic representations of knowledge and their use. As the AI representations become deeper and represent their roots, they will always be found to rest on measurement, which always has a random component, so there is a clear need for statistics in AI.

The need for statistics in AI has so far shown itself mainly in the two areas of uncertainty and learning. In the first area, reasoning in AI systems must take into account the uncertainty of empirical relationships. The developers of the well-known Mycin system (Buchanan and Shortliffe, 1984) found uncertainty to be an essential property in representing knowledge for their domain of medical diagnosis. Their treatment of uncertainty has highlighted its importance, perhaps unduly so. The discussion of probabilistic methods in AI literature has revolved around the assumptions necessary to use Bayesian methods. Even those defending probabilistic methods in the AI literature, such as Charniak (1983), have usually been discussing the limitations of what Spiegelhalter (Chapter 2) calls "idiot Bayes." There has also been some interest among AI researchers in Shafer's (1976) theory of evidence. As Spiegelhalter points out, more sophisticated methods are available.

Statistics can also contribute to the study of learning and concept formation (or, in statistical terminology, clustering). AI is particularly concerned with finding clustering methods that can be applied to data that have categorical labels in addition to or instead of numerical attributes, whereas statisticians have long dealt with clustering on numerical attributes. The obvious area of common concern would be that with both numerical and categorical attributes. But as Fisher and Langley (Chapter 4) point out, there are strong correspondences between the purely symbolic techniques and the purely numerical techniques. Also, the AI work has not paid sufficient attention to the problem of error in the input symbolic data.

When I first thought about the workshop that led to this book, I was thinking about a workshop on "AI in Statistics." But it soon became apparent that this was a mistake, because what the statisticians need to learn is what the AI researchers know well, and vice versa. To get experts in both areas at one meeting, there must be something for both to learn, so maximum value comes from having both sides present. I believe the same holds for this book. Those particularly interested in learning from some of these chapters may well find that they could easily contribute to a discussion raised by another chapter. I hope that such will happen frequently, and that what is written here is soon outmoded.

### 1.2 BACKGROUND

This section presents a review of background literature on AI in statistics. I have included a thorough review of this literature because papers on AI in statistics are neither very numerous nor very accessible. I have not, however, included a similar review of statistics in AI because that literature is too extensive to be summarized readily and because it is more readily available to readers. Certain chapters of this book do include fairly extensive reviews of statistics in AI for certain key areas. David Spiegelhalter's chapter, Chapter 2, provides a review of some of the most relevant papers in propagation of uncertainty, whereas in Chapter 4 Doug Fisher and Pat Langley include a considerable review of papers in concept formation.

### 1.2.1 What Has Been Done

The earliest paper I have seen that explicitly called for more intelligence in statistical software is a paper by John Nelder (1977), "Intelligent Programs, the Next Stage in Statistical Computing." He motivated the discussion by pointing out that algorithmic procedures in common use in statistics packages would accept any data set of the right shape (the right lengths of vectors, or sizes of matrices). The packages did not give a warning if something was wrong, and therefore the program relied on the user to know what to check and to make the checks. He expressed the opinion, which I believe is widely shared, that "the amount of uncritical use of standard procedures is enormous." He then turned to a discussion of what might be done, using regression as an example. Nelder suggested three sources of distortion that a regression analysis should "ideally" be protected against: (1) faults in the data, (2) faults in the model - systematic part, and (3) faults in the model - random part. But, in 1977, the techniques Nelder could suggest for carrying out his ideas were not extensive and probably lacked sufficient power to accomplish the job.

John Chambers (1981) was the first to argue that expert system techniques from AI would be useful for achieving more intelligent software. He echoed Nelder in decrying reliance on "blind computational algorithms," and also argued that declining computation costs, making computers more widely available for statistics, would "precipitate much uninformed, unguided, and simply incorrect data analysis." He went on to argue that "passive solutions," such as reporting diagnostics or multiple answers, would not go far enough. He therefore suggested that expert system techniques be used to devise software playing an active role in proposing answers and actions based on the data set. He introduced the term strategy and mentioned regression diagnostics and robust estimation as currently available statistical tools that would be useful in a strategy.

Chambers, Pregibon, and Zayas presented a paper at Buenos Aires in 1981 reporting the result of an experiment undertaken by the three authors

at AT&T Bell Laboratories in the summer of 1980. They chose regression analysis as an initial target, citing as reasons that it was a relatively small but not insignificant area, and well studied. Their work was the first to use a symbolic reasoning system to direct statistical software. They identified the broad structures needed by a consultation program as diagnostics, action rules, explanations, and dialogue. They attempted to implement an expert system with production rules using OPS4. However, as far as I could tell from an examination of the program when I started work on REX, they used very few production rules and quite a bit of Lisp programming. A program to conduct user interaction was well developed. The paper reports discussions of statistical strategy in analysis of collinearity, outliers, re-expression, and non-normality of errors. This program attempted more than REX, with fewer resources, so that it could only be described as an "initial experiment."

At the same meeting, Campbell and Woodings (1981) called for software which would "mimic the steps and checks that experienced statisticians carry out automatically" They cited inexperienced users as a source of statistical errors, pointing out that current statistical packages did little checking. They included a detailed discussion of some checks and transformations, key ingredients to a strategy, for multivariate discrimination. Their suggestions for implementation included ideas on descriptors to be kept with the data and records of actions taken using the data. Although they cited AI as a promising source of help, they did not relate the statistical needs to demonstrated AI systems.

Hajek and Ivanek (1982) described another early system. A system using 34 rules to decided among six choices of statistical test was built and run on a dozen problems. This system was not connected to a statistical package, but merely asked the user all the information it wanted, including such items determinable from the data as the number of data points. The paper did not argue the necessity or desirability of consultation systems in statistics, but suggested two types of systems based on analogies with expert systems which had been described in other domains. The two suggestions were systems to advise on the use of specific statistical packages and systems modeling the exploratory data analysis process.

Bob Blum's thesis (1982) on the RX system was slow to be recognized as an important contribution for AI in statistics. Because it was considered part of medical literature, it was overlooked by statisticians. By specializing to medicine as a ground domain, Blum was able to produce a feasibility demonstration system for translating research goals into a specific data analysis agenda. RX included hierarchical representations of medical concepts and statistical methods, together with a causal network among the medical concepts. The data available to the system were longitudinal medical records on rheumatic patients. The patients were seriously ill, with multiple diseases and therapies, which made establishing a valid study design challenging. RX was intended to (1) propose a new causal relation worth

studying; (2) design a study by controlling confounding relations, finding data, and chosing an analytic method; and (3) to carry out the analysis. The first and third of these goals were not accomplished, but the second alone is a valuable example of an AI application in statistics.

Daryl Pregibon and I began work on REX late in 1981. REX gave advice on regression analysis, searching for problems in the data and proposing actions to remediate any problems found. Reading John Nelder's paper after building REX was very interesting because the three main stages of REX's analysis — checking each variable separately, establishing linearity of the model, and reviewing the residuals for problems — correspond precisely to Nelder's three sources of distortion. REX was the first system to successfully use expert system techniques to choose commands for a statistical package and to carry out complete analyses. We reported our work in Gale and Pregibon (1982) and Pregibon and Gale (1984). Chapter 8 of this book gives more detail on REX than is available in those earlier papers.

Three points stand out from John Tukey's (1982) talk at the 14th Interface Symposium. First, he emphasized the need for statistical explanations. In statistics, explanations are rarely certain. Multiple possible reasons to more or less explain what is going on will be harder to generate but more honest than recounting a single line of reasoning. Second, he made clear the importance of search in data analysis, saying, "A competent data analysis of an even moderately complex set of data is a thing of trials and retreats, of dead ends and branches." This discussion of search in statistics led me to devise the trace in Student (Chapter 10), and the work by Oldford and Peters (Chapter 15) and Huber (Chapter 12) reflects the same concern. Third, the talk proposed "cognostics," diagnostics designed for interpretation by a computer rather than by a human. We have gotten along with diagnostics off the shelf for interactive systems, but when we want to say "Do those 5000 cases like I am doing this one, and tell me of any interesting differences," then we will need more than is now available.

In 1983, Portier and Lai described a system, STATPATH, which is the only system yet to tackle the problem of a user not understanding a question or misunderstanding a question. STATPATH uses production rules to encode a binary choice tree to help the user select an analytic technique. The decisions in the choice 'ree are made by asking the user carefully phrased questions. If the user did not understand a question, several lines of help were available. First, the user could ask for a more fully worded question. Alternatively, the user could reply "unknown" to the question, instead of "yes" or "no," and get both further lines of questioning. Having followed more than one line of questioning to a recommended analytic technique, the user could then browse textual annotations to the techniques. This problem of user misunderstanding is an important one, and one for which AI techniques may be useful.