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# The Modula-2 Software Component Library

Volume 3

With 30 Illustrations



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Dedicated to Doris Regina  
whose love made this possible

and  
to Robert, Lori, and Heather  
and  
to Modula-2 programmers everywhere

# Contents

## 0 Introduction to Volume 3

1

## Part 1 — Preliminaries

### 1 Specification

5

#### 1.1 Specification of Procedure Abstractions

5

- 1.1.1 Header Section
- 1.1.2 Requires Section
- 1.1.3 Where Section
- 1.1.4 Modifies Section
- 1.1.5 Effects Section
- 1.1.6 Signals Section

6

6

6

6

6

6

#### 1.2 Specification of Data Abstractions

7

#### 1.3 Special Symbols

7

#### References

8

### 2 Module Guide

9

#### 2.1 Purpose

9

#### 2.2 Characterization of Modules

9

#### 2.3 Module Guide Organization

11

#### 2.4 Binary Trees

12

##### 2.4.1 Tree Types

13

##### 2.4.2 AVL Tree — Sequential Unbounded Managed Iterator

13

##### 2.4.3 BB Tree — Sequential Unbounded Managed Iterator

13

##### 2.4.4 Binary Tree — Sequential Bounded Managed Iterator

14

##### 2.4.5 Binary Tree — Sequential Unbounded Managed Iterator

15

##### 2.4.6 IPB Tree — Sequential Unbounded Managed Iterator

15

<b>2.5 Graphs</b>	16
2.5.1 Graph Types	16
2.5.2 Graph — Directed Sequential Bounded Managed Iterator	17
2.5.3 Graph — Directed Sequential Unbounded Managed Iterator	17
2.5.4 Graph — Undirected Sequential Bounded Managed Iterator	18
2.5.5 Graph — Undirected Sequential Unbounded Managed Iterator	18
<b>2.6 Graph Utilities</b>	19
<b>2.7 Module Names</b>	19
<b>References</b>	21

## Part 2 — Trees

<b>3 Tree Abstraction</b>	23
<b>3.1 Concepts and Definitions</b>	23
3.1.1 Basic Tree Definitions	23
3.1.2 Attributes of Nodes	24
3.1.3 Relationships Between Nodes	25
3.1.4 Attributes of Trees	25
3.1.5 Kinds of Trees	26
3.1.6 Tree Traversals	26
3.1.6.1 General Tree Traversals	26
3.1.6.2 Binary Tree Traversals	27
3.1.7 Forests	27
<b>3.2 Applications and Uses</b>	29
<b>3.3 Binary Search Tree Operations</b>	29
<b>3.3.1 Constructors</b>	31
3.3.1.1 Create	31
3.3.1.2 Destroy	31
3.3.1.3 Clear	31
3.3.1.4 Assign	32
3.3.1.5 Insert	32
3.3.1.6 MakeTree	33
3.3.1.7 Remove	33

## Table of Contents

3.3.2	Selectors	34
3.3.2.1	IsDefined	34
3.3.2.2	IsEmpty	34
3.3.2.3	IsEqual	34
3.3.2.4	ExtentOf	35
3.3.2.5	IsPresent	35
3.3.3	Passive Iterators	35
3.3.3.1	Preorder	35
3.3.3.2	Inorder	36
3.3.3.3	Postorder	36
3.3.4	Active Iterators	36
3.3.4.1	RootOf	37
3.3.4.2	LeftOf	37
3.3.4.3	RightOf	37
3.3.4.4	IsNull	37
3.3.4.5	KeyOf	38
3.3.4.6	DataOf	38
3.4	Balanced Binary Trees	38
3.4.1	Height-Balanced (AVL) Trees	39
3.4.2	Weight-Balanced (BB) Trees	39
3.4.3	Path-Balanced (IPB) Trees	39
3.4.4	Rotations	40
3.5	Tree Exceptions	40
3.5.1	Initialization Failed	40
3.5.2	Overflow	40
3.5.3	Tree is Null	42
3.5.4	Type Error	42
3.5.5	Undefined	42
3.6	Summary	42
3.6.1	Operations Summary	42
3.6.2	Exceptions Summary	43
	References	45
4	The Unbounded Binary Tree	47
4.1	Tree Types Module	47
4.1.1	Tree Operations	47
4.1.2	Tree Exceptions	48
4.1.3	Tree Types and Procedure Types	49

<b>4.2 Unbounded Binary Search Tree Interface</b>	<b>50</b>
4.2.1 Type Declarations	51
4.2.2 Exception Handling	52
4.2.3 Constructors	52
4.2.4 Selectors	54
4.2.5 Passive Iterators	55
4.2.6 Active Iterators	55
<b>4.3 Unbounded Binary Search Tree Implementation</b>	<b>58</b>
4.3.1 Internal Representation	59
4.3.2 Exception Handling	60
4.3.3 Local Operations	61
4.3.4 Constructors	62
4.3.5 Selectors	69
4.3.6 Passive Iterators	72
4.3.7 Active Iterators	74
4.3.8 Module Initialization	76
<b>4.4 Unbounded Binary Search Tree Utilities Interface</b>	<b>76</b>
4.4.1 Utility Selectors	77
4.4.2 Debugging Iterators	77
<b>4.5 Unbounded Binary Search Tree Utilities Implementation</b>	<b>78</b>
4.5.1 Utility Selectors	78
4.5.2 Debugging Iterators	79
<b>References</b>	<b>80</b>
<b>5 The Bounded Binary Tree</b>	<b>81</b>
<b>5.1 Bounded Binary Search Tree Interface</b>	<b>81</b>
5.1.1 Type Declarations	82
5.1.2 Exception Handling	82
5.1.3 Constructors	83
5.1.4 Selectors	84
5.1.5 Passive Iterators	86
5.1.6 Active Iterators	86
<b>5.2 Bounded Binary Search Tree Implementation</b>	<b>89</b>
5.2.1 Internal Representation	90
5.2.2 Exception Handling	91
5.2.3 Free List Management	92
5.2.4 Local Operations	94

## Table of Contents

5.2.5	Constructors	94
5.2.6	Selectors	101
5.2.7	Passive Iterators	105
5.2.8	Active Iterators	107
5.2.9	Module Initialization	109
References		110
<b>6 The Unbounded AVL Tree</b>		111
6.1	Unbounded AVL Tree Interface	111
6.1.1	Type Declarations	112
6.1.2	Exception Handling	112
6.1.3	Constructors	113
6.1.4	Selectors	115
6.1.5	Passive Iterators	115
6.1.6	Active Iterators	116
6.2	Unbounded AVL Tree Implementation	119
6.2.1	Internal Representation	120
6.2.2	Exception Handling	121
6.2.3	Local Operations	122
6.2.4	Constructors	125
6.2.5	Selectors	135
6.2.6	Passive Iterators	138
6.2.7	Active Iterators	140
6.2.8	Module Initialization	142
6.3	Unbounded AVL Tree Utilities Interface	142
6.3.1	Utility Selectors	143
6.3.2	Debugging Iterators	143
6.4	Unbounded AVL Tree Utilities Implementation	144
6.4.1	Utility Selectors	144
6.4.2	Debugging Iterators	145
References		146
<b>7 The Unbounded BB Tree</b>		147
7.1	Unbounded BB Tree Interface	147
7.1.1	Type Declarations	148
7.1.2	Exception Handling	149

## Table of Contents

7.1.3	Constructors	149
7.1.4	Selectors	151
7.1.5	Passive Iterators	152
7.1.6	Active Iterators	152
7.2	Unbounded BB Tree Implementation	155
7.2.1	Internal Representation	156
7.2.2	Exception Handling	157
7.2.3	Local Operations	158
7.2.4	Constructors	160
7.2.5	Selectors	168
7.2.6	Passive Iterators	172
7.2.7	Active Iterators	174
7.2.8	Module Initialization	175
	References	176
8	The Unbounded k-Balanced Binary Tree	177
8.1	Unbounded k-Balanced Binary Tree Interface	177
8.1.1	Type Declarations	178
8.1.2	Exception Handling	179
8.1.3	Constructors	179
8.1.4	Selectors	181
8.1.5	Passive Iterators	182
8.1.6	Active Iterators	182
8.2	Unbounded k-Balanced Binary Tree Implementation	185
8.2.1	Internal Representation	186
8.2.2	Exception Handling	187
8.2.3	Local Operations	189
8.2.4	Constructors	192
8.2.5	Selectors	200
8.2.6	Passive Iterators	204
8.2.7	Active Iterators	205
8.2.8	Module Initialization	207
8.3	Unbounded k-Balanced Binary Tree Utilities Interface	208
8.3.1	Utility Selectors	208
8.3.2	Debugging Iterators	208

## Table of Contents

8.4	Unbounded k-Balanced Binary Tree Utilities	
	Implementation	209
8.4.1	Utility Selectors	209
8.4.2	Debugging Iterators	210
References		212

## Part 3 Graphs

9	Graph Abstraction	213
9.1	Concepts and Definitions	213
9.1.1	Directed Graphs	213
9.1.2	Undirected Graphs	214
9.1.3	Labeled and Weighted Graphs	216
9.2	Applications and Uses	217
9.3	Directed Graph Specifications	217
9.3.1	Directed Graph Types	217
9.3.2	Directed Graph Constructors	218
9.3.2.1	Create	218
9.3.2.2	Destroy	219
9.3.2.3	Clear	219
9.3.2.4	Assign	219
9.3.2.5	Insert	220
9.3.2.6	Remove	220
9.3.2.7	SetLabel	221
9.3.2.8	Link	221
9.3.2.9	Unlink	222
9.3.2.10	SetAttribute	222
9.3.3	Directed Graph Selectors	223
9.3.3.1	IsDefined	223
9.3.3.2	IsEmpty	223
9.3.3.3	OrderOf	223
9.3.3.4	SizeOf	224
9.3.3.5	OutDegree	224
9.3.3.6	InDegree	224
9.3.3.7	LabelOf	224

9.3.3.8	IsVertex	225
9.3.3.9	GraphOf	225
9.3.3.10	IsEdge	225
9.3.3.11	AttributeOf	225
9.3.3.12	InitialOf	226
9.3.3.13	FinalOf	226
9.3.4	Directed Graph Passive Iterators	226
9.3.4.1	TraverseVertices	227
9.3.4.2	TraverseEdges	227
9.3.4.3	Iterate	227
9.3.4.4	LoopVertices	227
9.3.4.5	LoopEdges	228
9.3.4.6	LoopIterate	228
9.3.5	Directed Graph Active Iterators	228
9.3.5.1	FirstVertex	228
9.3.5.2	NextVertex	229
9.3.5.3	FirstEdge	229
9.3.5.4	NextVertex	229
9.4	Undirected Graph Specifications	230
9.4.1	Undirected Graph Constructors	230
9.4.1.1	Remove	230
9.4.1.2	Link	231
9.4.2	Undirected Graph Selectors	231
9.4.2.1	DegreeOf	231
9.4.2.2	FirstOf	232
9.4.2.3	SecondOf	232
9.4.2.4	IncidentOn	232
9.4.3	Undirected Graph Passive Iterators	232
9.5	Graph Exceptions	233
9.5.1	EdgeIsNull	233
9.5.2	EdgeNotInGraph	233
9.5.3	Initialization Failed	233
9.5.4	Overflow	233
9.5.5	Undefined	234
9.5.6	VertexIsNull	234
9.5.7	VertexNotInGraph	234
9.6	Graph Utilities	234
9.6.1	BreadthFirstSearch	235
9.6.2	DepthFirstSearch	235
9.6.3	HasSelfLoops	236
9.6.4	IsIsolated	236

## Table of Contents

9.6.5	IsReachable	237
9.6.6	IsTerminal	237
9.6.7	MaxDegree	237
9.6.7	MinDegree	238
<b>9.7</b>	<b>Summary</b>	<b>238</b>
9.7.1	Directed Graph Operations Summary	238
9.7.2	Directed Graph Exceptions Summary	239
9.7.3	Undirected Graph Operations Summary	241
9.7.4	Undirected Graph Exceptions Summary	242
9.7.5	Graph Utility Operations Summary	243
9.7.6	Graph Utility Exceptions Summary	244

<b>References</b>	<b>245</b>
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## 10 The Unbounded Directed Graph

<b>10.1</b>	<b>Graph Types Interface</b>	<b>247</b>
<b>10.2</b>	<b>Unbounded Directed Graph Interface</b>	<b>248</b>
10.2.1	Type Declarations	250
10.2.2	Exception Handling	251
10.2.3	Graph Constructors	252
10.2.4	Vertex Constructors	253
10.2.5	Edge Constructors	253
10.2.6	Graph Selectors	254
10.2.7	Vertex Selectors	255
10.2.8	Edge Selectors	256
10.2.9	Passive Iterators	257
10.2.10	Active Iterators	258
<b>10.3</b>	<b>Unbounded Directed Graph Implementation</b>	<b>260</b>
10.3.1	Internal Representation	261
10.3.2	Exception Handling	264
10.3.3	Local Routines	265
10.3.4	Graph Constructors	269
10.3.5	Vertex Constructors	277
10.3.6	Edge Constructors	279
10.3.7	Graph Selectors	282
10.3.8	Vertex Selectors	284
10.3.9	Edge Selectors	287
10.3.10	Passive Iterators	288
10.3.11	Active Iterators	292
10.3.12	Module Initialization	293

References	294
<b>11 The Bounded Directed Graph</b>	<b>295</b>
<b>11.1 Bounded Directed Graph Interface</b>	<b>295</b>
11.1.1 Type Declarations	296
11.1.2 Exception Handling	298
11.1.3 Graph Constructors	298
11.1.4 Vertex Constructors	299
11.1.5 Edge Constructors	300
11.1.6 Graph Selectors	301
11.1.7 Vertex Selectors	302
11.1.8 Edge Selectors	302
11.1.9 Passive Iterators	303
11.1.10 Active Iterators	304
<b>11.2 Bounded Directed Graph Implementation</b>	<b>307</b>
11.2.1 Internal Representation	308
11.2.2 Exception Handling	311
11.2.3 Local Routines	313
11.2.4 Graph Constructors	316
11.2.5 Vertex Constructors	325
11.2.6 Edge Constructors	328
11.2.7 Graph Selectors	331
11.2.8 Vertex Selectors	333
11.2.9 Edge Selectors	335
11.2.10 Passive Iterators	337
11.2.11 Active Iterators	341
11.2.12 Module Initialization	342
References	343
<b>12 The Unbounded Undirected Graph</b>	<b>344</b>
<b>12.1 Unbounded Undirected Graph Interface</b>	<b>345</b>
12.1.1 Type Declarations	346
12.1.2 Exception Handling	347
12.1.3 Graph Constructors	348
12.1.4 Vertex Constructors	349
12.1.5 Edge Constructors	350
12.1.6 Graph Selectors	350
12.1.7 Vertex Selectors	351

## Table of Contents

12.1.8	Edge Selectors	352
12.1.9	Passive Iterators	353
12.1.10	Active Iterators	354
<b>12.2</b>	<b>Unbounded Undirected Graph Implementation</b>	<b>357</b>
12.2.1	Internal Representation	358
12.2.2	Exception Handling	363
12.2.3	Local Routines	364
12.2.4	Graph Constructors	370
12.2.5	Vertex Constructors	379
12.2.6	Edge Constructors	382
12.2.7	Graph Selectors	384
12.2.8	Vertex Selectors	386
12.2.9	Edge Selectors	388
12.2.10	Passive Iterators	390
12.2.11	Active Iterators	393
12.2.12	Module Initialization	394
<b>References</b>		<b>396</b>
<b>13</b>	<b>Graph Utilities</b>	<b>397</b>
<b>13.1</b>	<b>DigraphSUMI Utilities Interface</b>	<b>397</b>
13.1.1	Graph Selector Utilities	398
13.1.2	Vertex Selector Utilities	398
13.1.3	Graph Traversal Utilities	399
<b>13.2</b>	<b>DigraphSUMI Utilities Implementation</b>	<b>399</b>
13.2.1	Graph Selector Utilities	400
13.2.2	Vertex Selector Utilities	402
13.2.3	Graph Traversal Utilities	404
<b>References</b>		<b>407</b>

## Appendices

<b>A Modula-2 Syntax Diagrams</b>	409
<b>B Standard Modula-2 Routines</b>	419
<b>C Modula-2 Compilers</b>	423
<b>D Module Tables</b>	427
<b>E Import Graphs</b>	443
<b>Bibliography</b>	447

# Table of Figures

Figure 2.1	Tree Module Organization	12
Figure 2.2	Graph Module Organization	16
Figure 2.3	Component Forms	20
Figure 3.1	Binary Tree Abstraction	22
Figure 3.2	Multiway Tree Abstraction	22
Figure 3.3	Ordered vs. Unordered Trees	24
Figure 3.4	A Forest of Trees	26
Figure 3.5	Binary Search Tree	28
Figure 3.6	Binary Search Tree Node	28
Figure 3.7	Single Left Rotation	39
Figure 3.8	Double Rotation	39
Figure 4.1	Unbounded Binary Tree Internal Representation	57
Figure 5.1	Bounded Binary Tree Internal Representation	89
Figure 6.1	Unbounded AVL Tree Internal Representation	119
Figure 7.1	Unbounded BB Tree Internal Representation	154
Figure 8.1	Unbounded IPB Tree Internal Representation	185
Figure 9.1	Directed Graph Abstraction	213
Figure 9.2	Undirected Graph Abstraction	213
Figure 9.3	The Directed Network Abstraction	214
Figure 9.4	A Multigraph	214
Figure 10.1	Unbounded Directed Graph Internal Representation	260
Figure 11.1	Bounded Directed Graph Internal Representation	307
Figure 12.1	Unbounded Undirected Graph Internal Representation	357
Figure 12.2	Relationship between Vertices, Edges, and Edge References	357
Figure E.1	Tree Types Import Graph	441
Figure E.2	Tree Definition Module Import Graph	441
Figure E.3	Tree Implementation Module Import Graph	442
Figure E.4	Graph Types Import Graph	442
Figure E.5	Graph Definition Module Import Graph	442
Figure E.6	Graph Implementation Module Import Graph	443