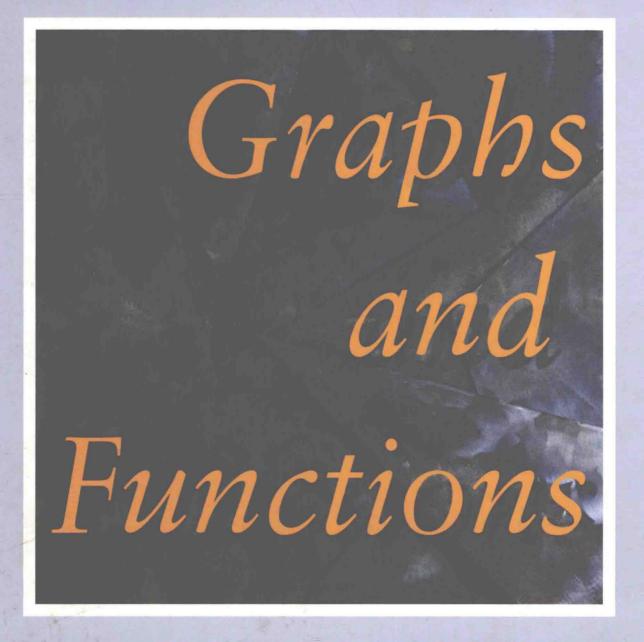
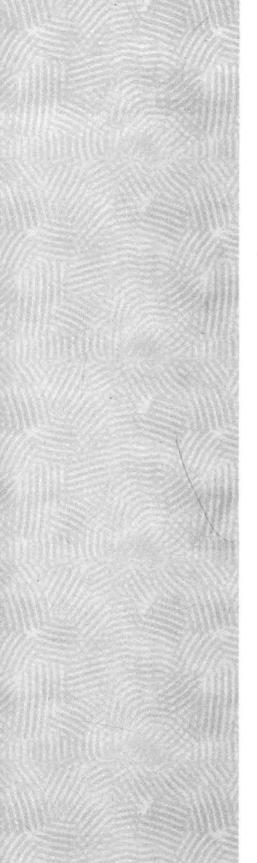
## ESSENTIALS O

## INTERMEDIATE ALGEBRA



LARSON HOSTETLER NEPTUNE

S E C O N D E D I



## Essentials of Intermediate Algebra Graphs and Functions

Second Edition

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### **Preface**



## A word from the authors ...

Welcome to Essentials of Intermediate Algebra: Graphs and Functions, Second Edition! In the revision of this early graphing and functions text, we focused on fine-tuning our student-oriented approach and incorporating the best aspects of reform in a meaningful yet easy-to-use manner. We hope you will be as excited about the Second Edition as we are after you take a look at it.

#### A student-oriented approach ...

Some students must take intermediate algebra more than once because they do not know how to study mathematics. The Second Edition helps students break out of this cycle by outlining a straightforward program of study with continual reinforcement and progressive confidence building.

This practical approach begins with Strategies for Success, a new feature found at the beginning of each chapter. In addition to outlining the key skills to be covered in the chapter, this checklist provides page references for the various study tools in the chapter. The Chapter Summary at the end of each chapter reinforces the Strategies for Success with a comprehensive list of the skills covered in the chapter, section references, and a correlation to the Review Exercises for guided practice.

Throughout each chapter there are many opportunities for students to assess their progress: at the end of each section (Warm-Ups and section exercises); in the middle of each chapter (Mid-Chapter Quiz); and at the end of each chapter (Review Exercises, Chapter Test, and Cumulative Test). The test items and text exercises are carefully crafted and graded in difficulty to give students a higher comfort level with algebraic skill building and problem solving.

These study tools reinforce the message that mathematics is a continuing story that requires constant synthesis and review. Along the way, students are guided by Study Tips that address special cases, expand on concepts, and help them avoid common errors.

Foremost for us, this text was written to be read and understood by students—not to be merely a source of homework assignments. We paid careful attention to the presentation—using precise mathematical language, innovative full-color design for emphasis and clarity, and a level of exposition that appeals to students—to create an effective teaching and learning tool.

#### ... that incorporates the best aspects of reform

We wholeheartedly embrace many of the features of the mathematics reform movement. Our First Edition led the way in developing many innovative learning techniques and our Second Edition is maintaining the pace.

In the Second Edition, we have increased the coverage of technology and integrated it throughout the text at point of use. Students are encouraged to use a graphing utility as a tool for exploration, discovery, and problem solving. Our reviewers were pleased to notice that technology is always introduced in support of the concepts, rather than being the central focus of the text.

We introduce graphing and functions early and integrate them throughout, always stressing visualization. We have increased the emphasis on real-life applications, problem solving, conceptual exercises (for example, Think About It and Section Projects), and motivational features (for example, Explorations and Group Activities). In addition, we added two new sections on modeling data: Section 3.2, Modeling Data with Linear Functions, and Section 6.6, Modeling Data with Quadratic Functions. This new material gives students the opportunity to focus on generating, exploring, and analyzing data.

We hope you will enjoy the Second Edition. It is a readable text that incorporates the best aspects of reform. The straightforward approach and effective study tools should appeal to your students.

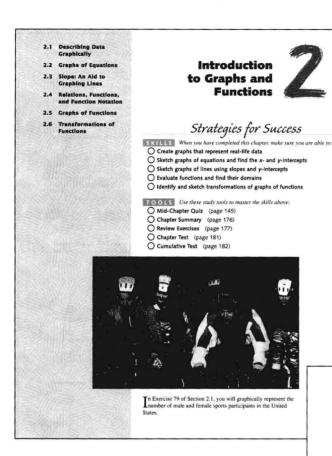
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#### **Section Topics**

Each section begins with a list of important topics that are covered in that section. These topics are also the subsection titles and can be used for easy reference and review by students.

#### Definitions, Rules, and Formulas

All of the important definitions, rules, and formulas are highlighted for emphasis. Each is also titled for easy reference.

## Features of the Text

#### Chapter Openers NEW

Each chapter opens with Strategies for Success. This new checklist outlines the key skills to be covered in the chapter and gives a list of the study tools in the chapter—with page references that will help students master the key skills. Each chapter opener also contains a list of the section topics, as well as a photo referring students to an interesting exercise in the chapter.

SECTION 5.2 Rational Exponents and Radicals

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#### 6.2

#### **Rational Exponents and Radicals**

Roots and Radicals • Rational Exponents • Radicals and Calculators • Radical Functions

#### Roots and Radicals

In Section 1.1, you reviewed the use of radical notation to represent nth roots of real numbers. Recall from that section that b is called an nth root of a if  $a = b^n$ . Also recall that the principal nth root of a real number is defined as follows.

**NOTE** "Having the same sign" means that the principal nth root of a is positive if a is positive and negative if a is negative. For example,  $\sqrt{4} = 2$  and  $\sqrt{3} - 8 = -2$ 

#### Principal nth Root of a Number

Let a be a real number that has at least one (real number) nth root. The **principal** nth root of a is the nth root that has the same sign as a, and it is denoted by the **radical symbol** 

√a. Princ

The positive integer n is the **Index** of the radical, and the number a is the **radicand.** If n=2, omit the index and write  $\sqrt{a}$  rather than  $\sqrt[3]{a}$ .

Therefore,  $\sqrt{49} = 7$ ,  $\sqrt[4]{1000} = 10$ , and  $\sqrt[4]{-32} = -2$ . You need to be aware of the following properties of *n*th roots. (Remember that for *n*th roots, *n* is an integer that is greater than or equal to 2.)

#### Properties of nth Roots

- If a is a positive real number and n is even, then a has exactly two (real) nth roots, which are denoted by \$\nabla a\$ and \$-\nabla a\$.
- If a is any real number and n is odd, then a has only one (real) nth root, which is denoted by \$\sqrt{a}\$.
- If a is a negative real number and n is even, then a has no (real) nth root.

Integers such as 1, 4, 9, 16, 49, and 81 are called **perfect squares** because they have integer square roots. Similarly, integers such as 1, 8, 27, 64, and 125 are called **perfect cubes** because they have integer cube roots.

#### **Explorations NEW**

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Before students are exposed to selected topics, Explorations invite them to discover concepts and patterns on their own, often taking advantage of the power of technology. This active participation by students strengthens their intuition and their criticalthinking skills and makes it more likely that they will remember the results. These new, optional boxed features can be omitted if the instructor desires with no loss of continuity in the coverage of material.

CHAPTER 4 Systems of Linear Equations and Inequalities

of the inequality  $2r - 3v \le 15$  Plot the points A(-1, -3) and B(5, 2) and sketch the line segment from A to B. How could you went from A to B. How could you verify that point C(2, -0.5) is the midpoint of the segment? Why is it not sufficient to show that the es from A to C and from C to 8 are equal? Find a formula for the coordinates of the midpoint of

CHAPTER 2 Introduction to Graphs and Functions To develop a general formula for the distance between two points, let  $(x_1, y_1)$ and  $(x_2, y_3)$  represent two points in the plane (that do not lie on the same horizon and  $(x_2, y_2)$  represent two points in the plane that do not need a substitution that it is a repetited line). With these two points, a right triangle can be formed, as shown in Figure 2.13. Note that the third vertex of the triangle is  $(x_1, y_2)$ . Because  $(x_1, y_1)$  and  $(x_1, y_2)$  lie on the same vertical line, the length of the vertical side of the triangle is  $|y_2 - y_1|$ . Similarly, the length of the horizontal side is  $|x_2 - x_1|$ . By the Pythagorean Theorem, the square of the distance between  $(x_1, y_1)$  and  $(x_2, y_2)$  is  $d^2 = |x_2 - x_1|^2 + |y_2 - y_1|^2.$ Because the distance d must be positive, you can choose the positive square root  $d = \sqrt{|x_2 - x_1|^2 + |y_2 - y_1|^2}$ Finally, replacing  $|x_2 - x_1|^2$  and  $|y_2 - y_1|^2$  by the equivalent expressions  $(x_2 - x_1)^2$  and  $(y_2 - y_1)^2$  gives you the **Distance Formula**. The Distance Formula The distance d between two points  $(x_1, y_1)$  and  $(x_2, y_2)$  is  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}.$ Note that for the special case in which the two points lie on the same vertical r horizontal line, the Distance Formula still works. For instance, applying the Distance Formula to the points (2, -2) and (2, 4) produces  $d = \sqrt{(2-2)^2 + [4-(-2)]^2} = \sqrt{6^2} = 6$ which is the same result obtained in Example 6.

#### **EXAMPLE 7** Finding the Distance Between Two Points

Find the distance between the points (-1, 2) and (2, 4), as shown in Figure 2.14.

Let  $(x_1, y_1) = (-1, 2)$  and  $(x_2, y_2) = (2, 4)$ , and apply the Distance Formula.

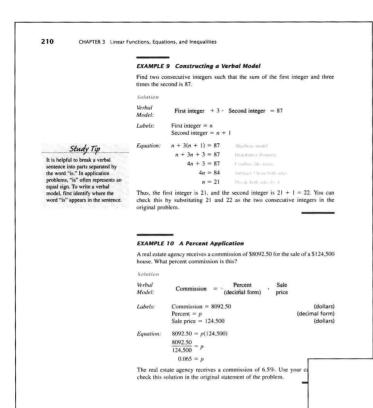
$$\begin{split} d &= \sqrt{[2-(-1)]^2+(4-2)^2} & \text{Substitute coordinates of points} \\ &= \sqrt{3^2+2^2} & \text{Simplify}, \\ &= \sqrt{13} & \text{Simplify}, \end{split}$$

 $y \ge \frac{2}{3}x - 5$ Solution To begin, rewrite the inequality in slope-intercept form.  $-3y \le -2x + 15$ Subtract 2s from both sales  $y \ge \frac{2}{2}x - 5$ Divide both aides by - 3 and revene the institution combined From this form, you can conclude that the solution is the half-plane lying on or above the line  $y = \frac{2}{3}x - 5.$ The graph is shown in Figure 4.19. echnology A graphing utility can be used to graph an inequality. The actual keystrokes used depend on the graphing utility, but here is an example of how to graph 3x + 2y < 41. Solve the inequality for y to obtain  $y < -\frac{3}{2}x + 2$ . 2. Press (y=) and enter − (3/2)X + 2 for Y₁. 3. Move the cursor to the left of Y Press ENTER until the ▲ icon appears. 5. Press GRAPH The graph is shown at the left. Try using a graphing utility to graph the following inequalities. (a)  $2x + 3y \ge 3$ (b)  $x - 2y \le 2$ 

EXAMPLE 4 Sketching the Graph of a Linear Inequality Use the slope-intercept form of a linear equation as an aid in sketching the graph

#### **Graphics**

Visualization is a critical problem-solving skill. Graphing is introduced in Chapter 2, and from that point on, students are encouraged to use graphs to reinforce algebraic or numeric solutions, to interpret data, and to explore concepts. The numerous figures in this text—all computer generated for accuracy help students develop these skills.



#### Examples

Each of the nearly 600 examples was carefully chosen to illustrate a particular concept or problem-solving technique and to enhance students' understanding. Students are taught a five-step strategy in the spirit of the AMATYC and NCTM standards, which starts with constructing a verbal model and ends with checking the answer. The examples are titled for easy reference, and comments adjacent to the solutions offer additional explanations.

#### **Applications**

A rich and varied selection of real-world applications are integrated throughout the text in examples and in exercises. These applications offer students a constant review of problem-solving skills and emphasize the relevance of the mathematics. Many of the applications use current, real data, and are titled for easy reference.

#### Group Activities NEW

Group Activities appear at the end of each section. They encourage students to think, talk, and write about mathematics in a peer-assisted learning environment.

SECTION 6.6 Modeling Data with Quadratic Functions

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#### Application

#### EXAMPLE 4 Finding a Quadratic Model

The total amounts A (in millions of tons) of solid waste materials recycled in the United States in selected years from 1980 through 1993 are shown below. Decide whether a linear model or a quadratic model better fits the data. Then use the model to predict the amount that will be recycled in the year 2000. In the list of data points (t,A), t represents the year, with t=0 corresponding to 1980.

(0, 14.5), (5, 16.4), (6, 18.3), (7, 20.1), (8, 23.5), (9, 29.9), (10, 32.9), (11, 37.3), (12, 41.5), (13, 45.0)

Solution

Begin by entering the data into a calculator or computer that has least squares regression programs. Then run the regression programs for linear and quadratic models.

Linear: y = ax + b a = 2.624 b = 6.684Quadratic:  $y = ax^2 + bx + c$  a = 0.243 b = -0.655 c = 14.037From the graphs in Figure 6.27, you can see that the quadratic model fits better.

(The correlation coefficient is r=0.994, which implies that the model is a good fit to the data.) From this model, you can predict the amount that will be recycled

 $A = 0.243(20)^2 - 0.655(20) + 14.037 = 98.137$  million tons,

which is more than two times the amount recycled in 1993.

#### Group Activities

FIGURE 6.27

#### **Problem Solving**

**Modeling Data** The amounts y (in gallons) of bottled water consumed in the United States in the years 1980 through 1993 are listed below. The data is given as ordered pairs of the form (t, y), where t is the year, with t = 0 representing 1980. Create a scatter plot of the data. With others in your group, decide which type of model best fits the data. Then find the model

(0, 2.4), (1, 2.7), (2, 3.0), (3, 3.4), (4, 4.0), (5, 4.5), (6, 5.0), (7, 5.7), (8, 6.5), (9, 7.4), (10, 8.0), (11, 8.0), (12, 8.2), (13, 9.2)

#### Technology NEW

Students are encouraged to use a graphing utility as a tool for exploration, discovery, and problem solving. Many opportunities to visualize concepts, to discover alternative approaches, to execute computations or programs, and to verify the results of other solution methods using technology are integrated throughout the text at point of use. However, students are not required to have access to a graphing utility to use this text effectively. In addition to describing the benefits of using technology, the text also pays special attention to its possible misuse or misinterpretation.

SECTION 7.3 Adding and Subtracting Rational Expressions

denominators and is called the **least common denominator** (or LCD) of the original rational expressions. Once the rational expressions have been written with like denominators, you can simply add or subtract the rational expressions using the rule given at the beginning of this section.

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#### EXAMPLE 5 Adding with Unlike Denominators

Add the rational expressions:  $\frac{7}{6x} + \frac{5}{8x}$ 

Solution

Technology

You can use a graphing utility to check your results when adding or subtracting rational expres-

sions. In Example 5, for instance,

in the same viewing rectangle, If the two graphs coincide, as shown below, you can conclude that the solution checks.

try graphing the equations

 $y_2 = \frac{43}{24x}$ 

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By factoring the denominators,  $6x = 2 \cdot 3 \cdot x$  and  $8x = 2^3 \cdot x$ , you can conclude that the least common denominator is  $2^3 \cdot 3 \cdot x = 24x$ .

$$\begin{split} \frac{7}{6x} + \frac{5}{8x} &= \frac{7(4)}{6x^44} + \frac{5(3)}{8x^44} \\ &= \frac{28}{24x} + \frac{15}{24x} & \text{Marrie fractions using least common decominator} \\ &= \frac{28+15}{24x} & \text{old Fractions} \\ &= \frac{43}{24x} & \text{Simplified from} \end{split}$$

#### **EXAMPLE 6** Subtracting with Unlike Denominators

Subtract the rational expressions:  $\frac{3}{r-3} - \frac{5}{r+2}$ 

Solution

The only factors of the denominators are (x-3) and (x+2). Therefore, the least common denominator is (x-3)(x+2).

$$\frac{3}{x-3} - \frac{5}{x+2} = \frac{3(x+2)}{(x-3)(x+2)} - \frac{5(x-3)}{(x-3)(x+2)}$$

$$= \frac{3x+6}{(x-3)(x+2)} - \frac{5x-15}{(x-3)(x+2)}$$

$$= \frac{(3x+6) - (5x-15)}{(x-3)(x+2)}$$

$$= \frac{3x+6 - 5x+15}{(x-3)(x+2)}$$

$$= \frac{-2x+21}{(x-3)(x+2)}$$

SECTION 6.3 The Quadratic Formula and the Discriminant

#### Solving Equations by the Quadratic Formula

When using the Quadratic Formula, remember that before the formula can be applied, you must first write the quadratic equation in standard form.

#### EXAMPLE 1 The Quadratic Formula: Two Distinct Solutions

$$x^2 + 6x = 16$$
 Uriginal equation  $x^2 + 6x - 16 = 0$  Write an standard form.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  Quadrate Formula 
$$x = \frac{-6 \pm \sqrt{6^2 - 4(1)(-16)}}{2}$$
 Substitute  $a = 1, b = 6, c = 16$ . Simplify 
$$x = \frac{-6 \pm \sqrt{100}}{2}$$
 Simplify 
$$x = \frac{-6 \pm 10}{2}$$
 Nimplify 
$$x = 2 \text{ or } x = -8$$
 Solutions.

The solutions are 2 and -8. Check these in the original equation. Or, try using a graphic check, as shown in Figure 6.6.

 $y = x^2 + 6x - 16$ FIGURE 6.6

NOTE In Example 1, the

solutions are rational numbers.

which means that the equation

could have been solved by factoring. Try solving the equation by factoring.



#### **EXAMPLE 2** The Quadratic Formula: Two Distinct Solutions

$$-x^2 - 4x + 8 = 0$$

$$x^2 + 4x - 8 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-4 \pm \sqrt{4^2 - 4(1)(-8)}}{2}$$

$$x = \frac{-4 \pm \sqrt{48}}{2}$$

$$x = \frac{-4 \pm \sqrt{43}}{2}$$

$$x = \frac{-4 \pm \sqrt{3}}{2}$$

$$x = \frac{2(-2 \pm 2\sqrt{3})}{2}$$

$$x = 2\sqrt{2}$$
Divide our common factor  $x = -2 \pm 2\sqrt{3}$ 

The solutions are  $-2 + 2\sqrt{3}$  and  $-2 - 2\sqrt{3}$ . Check these in the original equation.

#### Notes

Many instructional notes accompany definitions, rules, and examples to give additional insight or describe generalizations.

#### Study Tips NEW

Study Tips help students avoid common errors, address special cases, and expand upon concepts. They appear in the margin at point of use.

SECTION 6.4 Applications of Quadratic Equations

#### 64

#### Evercises

- 1. Unit Appliede Describe the units of the product 9 dollars • (20 hours)
- 2. Unit Analysis Describe the units of the product. 20 feet minute · 1 minute · (45 seconds)

umber Problems In Exercises 3-6, find two positive integers that satisfy the requirement

- 3. The product of two consecutive integers is 8 less than 10 times the smaller integer
- 4. The product of two consecutive integers is 80 more than 15 times the larger integer.
- 5. The product of two consecutive even integers is 50 more than 3 times the larger integer. 6. The product of two consecutive odd integers is 22
- less than 15 times the smaller integer

plete the table of widths, lengths, perimeters, and areas of rectangles.

	Width	Length	Perimeter	Area
7.	0.751	1	42 in.	
8.	w	1.5w	40 m	
9.	w	2.5w		250 ft <sup>2</sup>
10.	W.	1.5w		216 cm <sup>2</sup>
11.	1/1	1		192 in.2
12.	31	T		2700 in.2
13.	w	w + 3	54 km	
14.	1-6	I	108 ft	
15.	l - 20	1		12,000 m <sup>2</sup>
16.	W:	w + 5		500 ft <sup>2</sup>

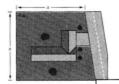


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17. Lumber Storage Area A retail lumberyard plans to store lumber in a rectangular region adjoining the sales office (see figure). The region will be fenced on three sides and the fourth side will be bounded by the wall of the office building. Find the dimensions of the region if 350 feet of fencing is available and the area of the region is to be 12,500 square feet.



- 18. Fencing the Yard You have 100 feet of fencing. Do you have enough to enclose a rectangular region whose area is 630 square feet? Is there enough to enclose a circular region of area 630 square feet? Explain
- 19. Fencing the Yard A family has built a fence around three sides of their property. In total, they used 550 feet of fencing. By their calculations, the lot is one acre (43,560 square feet). Is this correct?



#### **Exercises**

The nearly 5000 section exercises contain numerous computational and applied problems dealing with a wide range of topics. The exercise sets are designed to build competence, skill, and understanding; each exercise set is graded in difficulty to allow students to gain confidence as they progress. Each pair of consecutive problems is similar, with the answers to the odd-numbered problems given at the end of the text. Detailed solutions to all odd-numbered exercises are given in the Student Study and Solutions Guide.

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#### CHAPTER 3 Linear Functions, Equations, and Inequalities

#### 3.2

#### Exercises

1. Falling Object In an experiment, students measured the speed s (in meters per second) of a falling object t seconds after it was released. The results are given in

1	0	E	2	3	4
s	0	11.0	19.4	29.2	39.4

A model for the data is s = 9.7t + 0.4.

- (a) Plot the data and graph the model on the same set of coordinate axes.
- (b) Create a table showing the given data and the approximations given by the model. (c) Use the model to predict the speed of the object
- after falling 5 second (d) Interpret the slope in the context of the problem
- 2. Cable TV The average monthly basic rate R (in dollars) for cable TV for the years 1989 through 1994 in 🚆 5. The English and Metric Systems The label on a roll the United States is given in the table. (Source: Paul

Year	1989	1990	1991
R	15.21	16.78	18.10
Year	1992	1993	1994
	19.08	10.30	21.62

the time in years, with t = 0 corresponding to 1990.

- (a) Plot the data and graph the model on the same set of coordinate axes. (b) Create a table showing the given data and the
- approximations given by the model.
- (c) Use the model to predict the average monthly basic rate for cable TV for the year 2000.
- (d) Interpret the slope in the context of the problem.

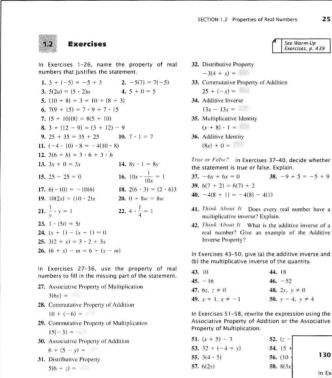
- 3. Property Tax The property tax in a township is directly proportional to the assessed value of the property. The tax on property with an assessed value of \$17,072 is \$1067.
  - (a) Find a mathematical model that gives the tax T in terms of the assessed value v.
  - (b) Use the model to find the tax on property with an assessed value of \$11,500.
  - (c) Determine the tax rate.
- 4. Revenue The total revenue R is directly proportional to the number of units sold x. When 25 units are sold, the revenue is \$6225.
  - (a) Find a mathematical model that gives the revenue R in terms of the number of units sold x.
  - (b) Use the model to find the revenue when 32 units are sold.
  - (c) Determine the price per unit.
- of tape gives the amount of tape in inches and centimeters. These amounts are 500 and 1270.
  - (a) Use the information on the label to find a mathe matical model that relates inches to centimeters.
  - (b) Use part (a) to convert 15 inches to centimeters.
  - (c) Use part (a) to convert 650 centimeters to inches. (d) Use a graphing utility to graph the model in part (a). Use the graph to confirm the results in parts
- (b) and (c). A model for the data is R = 1.17t + 16.61, where t is 36. The English and Metric Systems The label on a bottle of soft drink gives the amount in liters and fluid ounces. These amounts are 2 and 67.63.
  - (a) Use the information on the label to find a mathematical model that relates liters to fluid ounces

  - (b) Use part (a) to convert 27 liters to fluid ounces.
  - (c) Use part (a) to convert 32 fluid ounces to liters. (d) Use a graphing utility to graph the model in part (a). Use the graph to confirm the results in parts

(b) and (c).

#### Warm-Ups

For each text section (except for Section 1.1), there is a corresponding set of ten Warm-Up exercises in the Appendix, as indicated by an icon. The Warm-Ups enable students to review and practice the previously learned skills necessary to master the new skills presented in the section. Answers to Warm-Ups appear in the Appendix as well.



#### True or False NEW

To help students understand the logical structure of algebra, a set of True or False questions is included toward the end of selected exercise sets. These questions help students focus on concepts, common errors, and the correct statements of definitions and rules.

#### Think About It NEW

These exercises are thought-provoking, conceptual problems that help students grasp underlying theories.

#### **Graphing Utilities**

Many exercises in the text can be solved using technology; however, the symbol identifies all exercises in which students are specifically instructed to use a graphing utility. Students are encouraged to use scientific and graphing calculators to discover patterns, to experiment, to calculate, and to create graphic models.

130 CHAPTER 2 Introduction to Graphs and Function

In Exercises 63-66, explain how the x-intercepts of the graph correspond to the solutions of the polynomial equation when y = 0.

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See Warm-Up Exercises, p. A39

38. -9 + 5 = -5 + 9

44, 18

52. (-

54. 15 4

56, (10

58. 8(3x

46. -52

48.  $2y, y \neq 0$ 

50. y - 4,  $y \neq 4$ 





In Exercises 67-70, use a graphing utility to graph the equation and find any x-intercepts of the graph. Verify algebraically that any x-intercepts are solu tions of the polynomial equation when v = 0.

67.  $y = \frac{1}{2}x - 2$ 68. y = -3x + 6

69.  $y = x^2 - 6x$ 

70.  $y = x^2 - 11x + 28$ 

In Exercises 71-80, use a graphing utility to solve

the equation graphically. 71. 7 - 2(x - 1) = 072. 2x - 1 = 3(x + 1)73.  $4 - x^2 = 0$ 74.  $x^2 + 2x = 0$ 

75.  $x^2 - 2x + 1 = 0$ 76.  $1 - (x - 2)^2 = 0$ 77.  $2x^2 + 5x - 12 = 0$  78.  $(x - 2)^2 - 9 = 0$ 

**79.**  $x^3 - 4x = 0$ 

**80.**  $2 + x - 2x^2 - x^3 = 0$ 

81. Hooke's Law The force F (in pounds) to stretch a spring x inches from its natural length is given by



(a) Use the model to complete the table

x	0	3	6	9	12

- (b) Sketch a graph of the model.
- (c) Use the graph in part (b) to determine how the length of the spring changes each time the force is doubled.

82. Dairy Farms The number of farms in the United States with milk cows has been decreasing. The numbers of farms N (in thousands) for the years 1988 through 1994 are given in the table.

Year	1988	1989	1990	1991	1992	1993	1994
N	216	203	193	181	171	159	150

A model for this data is

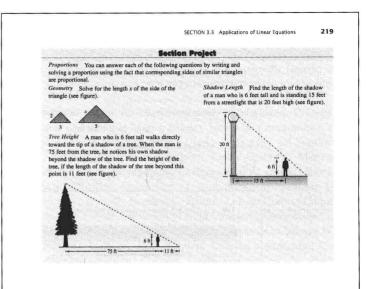
N = -11.0t + 192.9

where t is the time in years, with t = 0 corresponding to 1990. (Source: U.S. Department of

- (a) Use a graphing utility to plot the data and graph the model
- (b) How well does the model represent the data? Explain your reasoning.
- (c) Use the model to predict the number of farms with milk cows in 1997.
- (d) Explain why the model may not be accurate in the future.

#### Section Projects NEW

Section Projects appear at the end of every exercise set. These extended applications are often multipart exercises that make use of real data to develop critical-thinking and problem-solving skills. Section Projects are designed for individual or group assignments.



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#### Chapter Summary

After studying this chapter, you should have acquired the following skills. These skills are keyed to the Review Exercises that begin on page 99. Answers to odd-numbered Review Exercises are given in the back of the book.

- Plot real numbers on a real number line and compare them by using inequality symbols. (Section 1.1)
- Evaluate expressions containing operations with real numbers. (Section 1.1)
- Identify the rule of algebra that is illustrated by an equation. (Sections 1.2, 1.3)
- Expand expressions using the Distributive Property. (Sections 1.2, 1.3)
- Simplify expressions by removing symbols of grouping. (Section 1.3)
- Simplify expressions by applying the properties of exponents. (Section 1.3)
- \* Solve problems involving geometry. (Sections 1.3, 1.4)
- Use expressions or equations to solve real-life problems. (Sections 1.1, 1.8)
- \* Interpret graphs representing real-life data. (Sections 1.1-1.4, 1.7)
- Simplify expressions by performing arithmetic operations. (Section 1.4)
- Multiply polynomials using the special product formulas. (Section 1.4)
- Factor expressions completely. (Sections 1.5, 1.6)
- Solve linear equations. (Section 1.7)
- Solve literal equations. (Section 1.7)
- Solve polynomial equations. (Section 1.8)
- Use a calculator to evaluate expressions containing operations with real numbers. (Section 1.1)

Review Exercises 1-4

Review Exercises 5-24, 47

Review Exercises 25–30

Review Exercises 31-34 Review Exercises 35-38

Review Exercises 39-44

Review Exercises 45, 46,

Review Exercises 48, 127,

128

Review Exercises 49, 50 Review Exercises 51–66

Review Exercises 67-74

Review Exercises 75-96

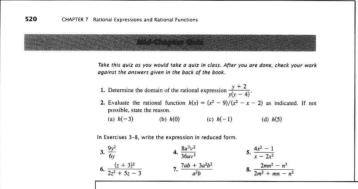
Review Exercises 97-104, 115, 116, 120, 121, 123,

Review Exercises 105, 106 Review Exercises 107-114,

117-119, 122, 125, 126 Review Exercise 131

#### Chapter Summary NEW

The Chapter Summary reviews the skills covered in the chapter. Section references make this an effective study tool, and correlation to the Review Exercises offers guided practice.



#### Mid-Chapter Quiz NEW

Each chapter contains a Mid-Chapter Quiz. This feature allows students to perform a self-assessment midway through the chapter. Answers to Mid-Chapter Quizzes appear at the end of the text.

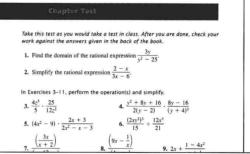
# The Exercises 1-4, find the domain of the rational expression. 1. $\frac{3y}{y-8}$ 2. $\frac{t+4}{t+12}$ 2. $\frac{4}{(x^2-16)}$ 2. $\frac{x^2-7x}{x+1} + \frac{x^2-14x+49}{x^2-1}$ 3. $\frac{u}{u^2-7u+6}$ 4. $\frac{x-12}{x(x^2-16)}$ 2. $\frac{4}{y} - \frac{11}{y}$ 2. $\frac{2}{y} - \frac{2}{y} + \frac{3}{y} - \frac{y}{y} + \frac{3}{y} - \frac{y}{y} + \frac{1}{y}$ 1. Exercises 5-12, simplify the rational expression. 2. $\frac{15}{5} - \frac{5}{24} - 1$ 2. $\frac{3}{5} + \frac{7}{5} - \frac{1}{12}$ 2. $\frac{5}{5} - \frac{15}{24} - 1$ 2. $\frac{3}{5} - \frac{7}{5} - \frac{1}{12}$ 3. $\frac{4}{5} - \frac{1}{5} - \frac{1}{2} - \frac{1}{5} - \frac{1}{2} -$

#### **Review Exercises**

The Review Exercises at the end of each chapter offer students an opportunity for additional practice. Answers to all the odd-numbered Review Exercises appear at the end of the text.

#### **Chapter Test**

Each chapter contains an endof-chapter test for students to assess their progress. Answers appear at the end of the text.

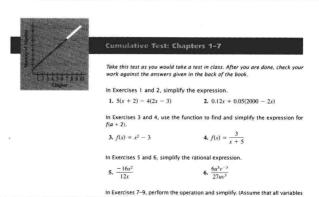


CHAPTER TEST

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#### **Cumulative Test**

In this edition, Cumulative Tests have been placed at the end of each chapter (except Chapter 1). These tests reinforce the message that is presented throughout the text—that mathematics is a continuing story and requires constant synthesis and review. Answers appear at the end of the text.



## Acknowledgments

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Roland E. Larson Robert P. Hostetler Carolyn F. Neptune

### Supplements

Essentials of Intermediate Algebra: Graphs and Functions, Second Edition by Larson, Hostetler, and Neptune is accompanied by a comprehensive supplements package. Most items are keyed directly to the text.

#### Printed Resources for the Instructor

Instructor's Annotated Edition by Larson, Hostetler, and Neptune

- Includes the entire student edition of the text
- · Answers to all exercises and tests
- · Teaching tips at point of use
- Additional examples and exercises with answers at point of use

Instructor's Guide by Carolyn F. Neptune, Johnson County Community College

- · Detailed solutions to all even-numbered Section Exercises
- Transparency Masters

Test Item File by David C. Falvo, The Pennsylvania State University, The Behrend College

- Over 4,000 test items keyed to the text by section and organized by objective
- · Six Chapter Tests per chapter
- · Questions given in both multiple-choice and fill-in formats
- · Answers to all test items and to chapter tests
- Also available as a computerized test bank

#### **Printed Resources for the Student**

Student Study and Solutions Guide by Carolyn F. Neptune, Johnson County Community College

 Step-by-step solutions to all odd-numbered Section Exercises, all Review Exercises, and all Mid-Chapter Quiz, Chapter Test, and Cumulative Test problems

Graphing Technology Guide: Algebra by Benjamin N. Levy and Laurel Technical Services

- Keystroke instructions for a wide variety of Texas Instruments, Casio, Sharp, and Hewlett-Packard graphing calculators, including the most current models
- · Examples with step-by-step solutions
- · Extensive graphics screen output
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#### Media Resources for the Instructor

#### Computerized Testing

- · Test-generating software for Windows and Macintosh
- Over 4,000 test items
- · Also available as a printed test bank

#### Media Resources for the Student

#### Videotape Series by Dana Mosely

- · Comprehensive section-by-section coverage
- Detailed explanation of important concepts
- Numerous examples and applications, often illustrated by computer-generated graphics

#### Tutorial Software

- Interactive tutorial software with comprehensive section-by-section coverage
- Diagnostic feedback
- · Additional examples
- · Chapter self-tests
- Glossary



## **How to Study Algebra**

**Studying Mathematics** Studying mathematics is a linear process: The material you learn each day builds upon material you learned previously. There are no shortcuts—you must keep up with the coursework every day.

**Making a Plan** Make your own course plan right now! A good rule of thumb is to study two to four hours for every hour in class. After your first major test, you will know if your efforts were sufficient. If you did not make the grade you wanted, then you should increase your study time, improve your study efficiency, or both.

**Preparing for Class** Before class, review your notes from the previous class. Then, read the portion of the text that is to be covered, paying special attention to the definitions and rules that are highlighted. This takes self-discipline, but it pays off because you will benefit much more from your instructor's presentation.

**Attending Class** Attend every class. Arrive on time with your text, a pen or pencil and paper for notes, and your calculator. If you must miss a class, get the notes from another student, go to your tutor for help, or view the appropriate mathematics videotape. You *must* learn the material that was covered in the missed class before attending the next class.

**Participating in Class** As you read the text before class, write down any questions you may have about the material. Ask your instructor these questions during class. This way, you will understand the material better, and you will be prepared to do your homework.

**Taking Notes** During class, take notes on definitions, examples, concepts, and rules. Focus on the instructor's cues to identify important material. Then, as soon after class as possible, review your notes and add any explanations that are necessary to make your notes understandable *to you*.

**Doing the Homework** Learning algebra is like learning to play the piano or basketball. You cannot develop skills just by watching someone do it; you must do it yourself. The best time to do your homework is right after class, when the concepts are still fresh in your mind. This increases your chances of retaining the information in long-term memory.

**Finding a Study Partner** When you get stuck on a problem, it may help to work with a partner. Even if you feel you are giving more help than you are getting, you will find that teaching others is an excellent way to learn.

**Building a Math Library** Build a library of books that can help you with your math courses. Consider using the *Student Study and Solutions Guide* for this text. As you will probably take other math courses after this one, we suggest that you keep the text. It will be a valuable reference book. Adding computer software and math videotapes is another way to build your math library.