The background of the book cover is a dark blue gradient. It features several technical illustrations: a faint gear-like pattern at the top, a color-coded stress distribution on an I-beam cross-section on the left, a circular interference pattern in the center, and a detailed diagram of X-ray diffraction on the right. The diffraction diagram shows incident and diffracted beams, lattice planes, and labels for wavelength  $\lambda$ , distance  $d$ , and angle  $2\theta_B$ .

# Practical Residual Stress Measurement Methods

Editor | GARY S. SCHAJER

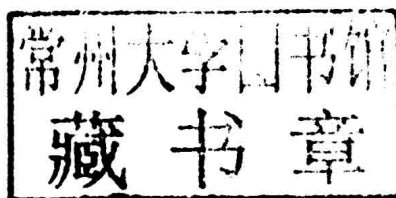
 **WILEY**

# PRACTICAL RESIDUAL STRESS MEASUREMENT METHODS

Edited by

**Gary S. Schajer**

*University of British Columbia, Vancouver, Canada*



 **WILEY**

A John Wiley & Sons, Ltd., Publication

This edition first published 2013

© 2013 John Wiley & Sons Ltd

*Registered office*

John Wiley & Sons Ltd, The Atrium, Southern Gate, Chichester, West Sussex, PO19 8SQ, United Kingdom

For details of our global editorial offices, for customer services and for information about how to apply for permission to reuse the copyright material in this book please see our website at [www.wiley.com](http://www.wiley.com).

The right of the author to be identified as the author of this work has been asserted in accordance with the Copyright, Designs and Patents Act 1988.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, except as permitted by the UK Copyright, Designs and Patents Act 1988, without the prior permission of the publisher.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books.

Designations used by companies to distinguish their products are often claimed as trademarks. All brand names and product names used in this book are trade names, service marks, trademarks or registered trademarks of their respective owners. The publisher is not associated with any product or vendor mentioned in this book.

**Limit of Liability/Disclaimer of Warranty:** While the publisher and author have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. It is sold on the understanding that the publisher is not engaged in rendering professional services and neither the publisher nor the author shall be liable for damages arising herefrom. If professional advice or other expert assistance is required, the services of a competent professional should be sought.

Library of Congress Cataloging-in-Publication Data

Practical residual stress measurement methods / edited by Gary S. Schajer.

pages cm

Includes bibliographical references and index.

ISBN 978-1-118-34237-4 (hardback)

1. Residual stresses. I. Schajer, Gary S., editor of compilation.

TA648.3.P73 2013

620.1'123-dc23

2013017380

A catalogue record for this book is available from the British Library.

ISBN 9781118342374

Set in 10/12 Times by Laserwords Private Limited, Chennai, India  
Printed and bound in Singapore by Markono Print Media Pte Ltd

# **PRACTICAL RESIDUAL STRESS MEASUREMENT METHODS**



*This book is dedicated to the memory of*

*Iain Finnie*

*late Professor of Mechanical Engineering at the University of  
California, Berkeley, a pioneer developer of the Slitting Method for  
measuring residual stresses.*

*Respectfully dedicated in appreciation of his encouragement,  
teaching, mentorship and personal friendship.*

*The royalties from the sale of this book have been directed to the  
Leonard and Lilly Schajer Memorial Bursary at the University of  
British Columbia, to provide bursaries to Mechanical Engineering  
students on the basis of financial need.*



# List of Contributors

**Don E. Bray**, Don E. Bray, Inc., Texas, USA

**David J. Buttle**, MAPS Technology Ltd., GE Oil & Gas, Oxford, UK

**Adrian T. DeWald**, Hill Engineering, LLC, California, USA

**Michael R. Hill**, Department of Mechanical and Aerospace Engineering, University of California, Davis, California, USA

**Thomas M. Holden**, National Research Council of Canada, Ontario, Canada (Retired)

**Conal E. Murray**, IBM T.J. Watson Research Center, New York, USA

**Drew V. Nelson**, Stanford University, Stanford, California, USA

**I. Cevdet Noyan**, Columbia University, New York, USA

**Michael B. Prime**, Los Alamos National Laboratory, New Mexico, USA

**Clayton O. Ruud**, Pennsylvania State University, Washington, USA (Retired)

**David J. Smith**, University of Bristol, Bristol, UK

**Philip S. Whitehead**, Stresscraft Ltd., Shepshed, Leicestershire, UK

**Philip J. Withers**, University of Manchester, Manchester, UK



# Preface

Residual stresses are created by almost every manufacturing process, notably by casting, welding and forming. But despite their widespread occurrence, the fact that residual stresses occur without any external loads makes them easy to overlook and ignore. This neglect can cause great design peril because residual stresses can have profound influences on material strength, dimensional stability and fatigue life. Sometimes alone and sometimes in combination with other factors, unaccounted for residual stresses have caused the failure of major bridges, aircraft, ships and numerous smaller structures and devices, often with substantial loss of life. At other times, residual stresses are deliberately introduced to provide beneficial effects, such as in pre-stressed concrete, shot-peening and cold hole-expansion.

Starting from early curiosities such as “Rupert’s Drops,” understanding of the character and mechanics of residual stresses grew with the rise in the use of cast metals during the Industrial Revolution. The famous crack in the Liberty Bell is due to the action of residual stresses created during casting. Early methods for identifying the presence of residual stresses involved cutting the material and observing the dimension changes. With the passage of time, these methods became more sophisticated and quantitative. Complementary non-destructive methods using X-rays, magnetism and ultrasonics were simultaneously developed.

Modern residual stress measurement practice is largely based on the early historical roots. However, the modern techniques bear the same relationship to their predecessors as modern jet planes to early biplanes: they share similar conceptual bases, but in operational terms the current measurement techniques are effectively “new.” They have attained a very high degree of sophistication due to greatly increased conceptual understanding, practical experience and much more advanced measurement/computation capabilities. All these factors join to give substantial new life into established ideas and indeed to produce “new lamps for old.”

Conceptual and technological progress has been a collective endeavor by a large group of people. The list of names is a long and distinguished one. To paraphrase Isaac Newton’s words, the present Residual Stress community indeed “stands on the shoulders of giants.” A particular one of these giants that several of the contributors to this book were privileged to know and learn from, was Iain Finnie, late Professor of Mechanical Engineering at the University of California, Berkeley. Professor Finnie was a pioneer of the Slitting Method, described in detail in Chapter 4 of this book. I join with the other authors in dedicating this book to him as a sign of respect and of appreciation for his encouragement, teaching,

mentorship and personal friendship. Those of us who aspire to be researchers and teachers can do no better than look to him for example.

On a personal note, I would like to express my sincere gratitude and appreciation to all the chapter authors of this book. The depth of their knowledge and experience of their various specialties and their generous willingness to share their expertise makes them a true “dream team.” They have been extraordinarily patient with all my editorial requests, both large and small, and have worked with me with grace and patience. Thank you, you have been good friends!

I also would like to thank the staff at John Wiley & Sons for the support and encouragement of this project, and for the careful way they have carried forward every step in the production process.

And finally, more personally, I would like to acknowledge my late parents, Leonard and Lilly Schajer, whose fingerprints are to be found on these pages. They followed the biblical proverb “Train up a child in the way he should go: and when he is old, he will not depart from it.” In keeping with their philosophy, the royalties from the sale of this book have been directed to support students in financial need through the Leonard and Lilly Schajer Memorial Bursary at the University of British Columbia. All book contributors have graciously supported this endeavor and in this way hope to add to the available shoulder-space on which the next generation may stand.

Gary Schajer  
Vancouver, Canada  
April 2013

# Contents

<b>List of Contributors</b>	<b>xv</b>
<b>Preface</b>	<b>xvii</b>
<b>1 Overview of Residual Stresses and Their Measurement</b>	<b>1</b>
<i>Gary S. Schajer and Clayton O. Ruud</i>	
1.1 Introduction	1
1.1.1 Character and Origin of Residual Stresses	1
1.1.2 Effects of Residual Stresses	3
1.1.3 Residual Stress Gradients	4
1.1.4 Deformation Effects of Residual Stresses	5
1.1.5 Challenges of Measuring Residual Stresses	6
1.1.6 Contribution of Modern Measurement Technologies	7
1.2 Relaxation Measurement Methods	7
1.2.1 Operating Principle	7
1.3 Diffraction Methods	13
1.3.1 Measurement Concept	13
1.3.2 X-ray Diffraction	14
1.3.3 Synchrotron X-ray	15
1.3.4 Neutron Diffraction	15
1.4 Other Methods	16
1.4.1 Magnetic	16
1.4.2 Ultrasonic	17
1.4.3 Thermoelastic	17
1.4.4 Photoelastic	18
1.4.5 Indentation	18
1.5 Performance and Limitations of Methods	18
1.5.1 General Considerations	18
1.5.2 Performance and Limitations of Methods	19
1.6 Strategies for Measurement Method Choice	19
1.6.1 Factors to be Considered	19
1.6.2 Characteristics of Methods	24
References	24

<b>2</b>	<b>Hole Drilling and Ring Coring</b>	<b>29</b>
	<i>Gary S. Schajer and Philip S. Whitehead</i>	
2.1	Introduction	29
2.1.1	<i>Introduction and Context</i>	29
2.1.2	<i>History</i>	30
2.1.3	<i>Deep Hole Drilling</i>	31
2.2	Data Acquisition Methods	31
2.2.1	<i>Strain Gages</i>	31
2.2.2	<i>Optical Measurement Techniques</i>	33
2.3	Specimen Preparation	35
2.3.1	<i>Specimen Geometry and Strain Gage Selection</i>	35
2.3.2	<i>Surface Preparation</i>	38
2.3.3	<i>Strain Gage Installation</i>	40
2.3.4	<i>Strain Gage Wiring</i>	40
2.3.5	<i>Instrumentation and Data Acquisition</i>	41
2.4	Hole Drilling Procedure	42
2.4.1	<i>Drilling Cutter Selection</i>	42
2.4.2	<i>Drilling Machines</i>	43
2.4.3	<i>Orbital Drilling</i>	44
2.4.4	<i>Incremental Measurements</i>	45
2.4.5	<i>Post-drilling Examination of Hole and Cutter</i>	46
2.5	Computation of Uniform Stresses	47
2.5.1	<i>Mathematical Background</i>	47
2.5.2	<i>Data Averaging</i>	49
2.5.3	<i>Plasticity Effects</i>	50
2.5.4	<i>Ring Core Measurements</i>	50
2.5.5	<i>Optical Measurements</i>	50
2.5.6	<i>Orthotropic Materials</i>	50
2.6	Computation of Profile Stresses	51
2.6.1	<i>Mathematical Background</i>	51
2.7	Example Applications	54
2.7.1	<i>Shot-peened Alloy Steel Plate – Application of the Integral Method</i>	54
2.7.2	<i>Nickel Alloy Disc – Fine Increment Drilling</i>	54
2.7.3	<i>Titanium Test-pieces – Surface Processes</i>	56
2.7.4	<i>Coated Cylinder Bore – Adaptation of the Integral Method</i>	57
2.8	Performance and Limitations of Methods	57
2.8.1	<i>Practical Considerations</i>	57
2.8.2	<i>Common Uncertainty Sources</i>	58
2.8.3	<i>Typical Measurement Uncertainties</i>	59
	References	61
<b>3</b>	<b>Deep Hole Drilling</b>	<b>65</b>
	<i>David J. Smith</i>	
3.1	Introduction and Background	65

3.2	Basic Principles	68
3.2.1	<i>Elastic Analysis</i>	68
3.2.2	<i>Effects of Plasticity</i>	71
3.3	Experimental Technique	72
3.4	Validation of DHD Methods	75
3.4.1	<i>Tensile Loading</i>	75
3.4.2	<i>Shrink Fitted Assembly</i>	77
3.4.3	<i>Prior Elastic-plastic Bending</i>	78
3.4.4	<i>Quenched Solid Cylinder</i>	79
3.5	Case Studies	80
3.5.1	<i>Welded Nuclear Components</i>	80
3.5.2	<i>Components for the Steel Rolling Industry</i>	82
3.5.3	<i>Fibre Composites</i>	82
3.6	Summary and Future Developments	83
	Acknowledgments	84
	References	85
<b>4</b>	<b>The Slitting Method</b>	<b>89</b>
	<i>Michael R. Hill</i>	
4.1	Measurement Principle	89
4.2	Residual Stress Profile Calculation	90
4.3	Stress Intensity Factor Determination	96
4.4	Practical Measurement Procedures	96
4.5	Example Applications	99
4.6	Performance and Limitations of Method	101
4.7	Summary	106
	References	106
<b>5</b>	<b>The Contour Method</b>	<b>109</b>
	<i>Michael B. Prime and Adrian T. DeWald</i>	
5.1	Introduction	109
5.1.1	<i>Contour Method Overview</i>	109
5.1.2	<i>Bueckner's Principle</i>	110
5.2	Measurement Principle	110
5.2.1	<i>Ideal Theoretical Implementation</i>	110
5.2.2	<i>Practical Implementation</i>	110
5.2.3	<i>Assumptions and Approximations</i>	112
5.3	Practical Measurement Procedures	114
5.3.1	<i>Planning the Measurement</i>	114
5.3.2	<i>Fixturing</i>	114
5.3.3	<i>Cutting the Part</i>	115
5.3.4	<i>Measuring the Surfaces</i>	116
5.4	Residual Stress Evaluation	117
5.4.1	<i>Basic Data Processing</i>	117
5.4.2	<i>Additional Issues</i>	120

5.5	Example Applications	121
5.5.1	<i>Experimental Validation and Verification</i>	121
5.5.2	<i>Unique Measurements</i>	127
5.6	Performance and Limitations of Methods	130
5.6.1	<i>Near Surface (Edge) Uncertainties</i>	130
5.6.2	<i>Size Dependence</i>	131
5.6.3	<i>Systematic Errors</i>	131
5.7	Further Reading On Advanced Contour Method Topics	133
5.7.1	<i>Superposition For Additional Stresses</i>	133
5.7.2	<i>Cylindrical Parts</i>	134
5.7.3	<i>Miscellaneous</i>	134
5.7.4	<i>Patent</i>	134
	Acknowledgments	134
	References	135
<b>6</b>	<b>Applied and Residual Stress Determination Using X-ray Diffraction</b>	<b>139</b>
	<i>Conal E. Murray and I. Cevdet Noyan</i>	
6.1	Introduction	139
6.2	Measurement of Lattice Strain	141
6.3	Analysis of Regular $d_{\phi\psi}$ vs. $\sin^2\psi$ Data	143
6.3.1	<i>Dölle-Hauk Method</i>	143
6.3.2	<i>Winholtz-Cohen Least-squares Analysis</i>	143
6.4	Calculation of Stresses	145
6.5	Effect of Sample Microstructure	146
6.6	X-ray Elastic Constants (XEC)	149
6.6.1	<i>Constitutive Equation</i>	150
6.6.2	<i>Grain Interaction</i>	151
6.7	Examples	153
6.7.1	<i>Isotropic, Biaxial Stress</i>	153
6.7.2	<i>Triaxial Stress</i>	154
6.7.3	<i>Single-crystal Strain</i>	156
6.8	Experimental Considerations	159
6.8.1	<i>Instrumental Errors</i>	159
6.8.2	<i>Errors Due to Counting Statistics and Peak-fitting</i>	159
6.8.3	<i>Errors Due to Sampling Statistics</i>	159
6.9	Summary	160
	Acknowledgments	160
	References	160
<b>7</b>	<b>Synchrotron X-ray Diffraction</b>	<b>163</b>
	<i>Philip Withers</i>	
7.1	Basic Concepts and Considerations	163
7.1.1	<i>Introduction</i>	163
7.1.2	<i>Production of X-rays; Undulators, Wigglers, and Bending Magnets</i>	166
7.1.3	<i>The Historical Development of Synchrotron Sources</i>	167

7.1.4	<i>Penetrating Capability of Synchrotron X-rays</i>	169
7.2	Practical Measurement Procedures and Considerations	169
7.2.1	<i>Defining the Strain Measurement Volume and Measurement Spacing</i>	170
7.2.2	<i>From Diffraction Peak to Lattice Spacing</i>	173
7.2.3	<i>From Lattice Spacing to Elastic Strain</i>	173
7.2.4	<i>From Elastic Strain to Stress</i>	178
7.2.5	<i>The Precision of Diffraction Peak Measurement</i>	179
7.2.6	<i>Reliability, Systematic Errors and Standardization</i>	180
7.3	Angle-dispersive Diffraction	184
7.3.1	<i>Experimental Set-up, Detectors, and Data Analysis</i>	184
7.3.2	<i>Exemplar: Mapping Stresses Around Foreign Object Damage</i>	186
7.3.3	<i>Exemplar: Fast Strain Measurements</i>	187
7.4	Energy-dispersive Diffraction	188
7.4.1	<i>Experimental Set-up, Detectors, and Data Analysis</i>	189
7.4.2	<i>Exemplar: Crack Tip Strain Mapping at High Spatial Resolution</i>	189
7.4.3	<i>Exemplar: Mapping Stresses in Thin Coatings and Surface Layers</i>	190
7.5	New Directions	191
7.6	Concluding Remarks	192
	References	193
<b>8</b>	<b>Neutron Diffraction</b>	<b>195</b>
	<i>Thomas M. Holden</i>	
8.1	Introduction	195
8.1.1	<i>Measurement Concept</i>	195
8.1.2	<i>Neutron Technique</i>	196
8.1.3	<i>Neutron Diffraction</i>	196
8.1.4	<i>3-Dimensional Stresses</i>	198
8.1.5	<i>Neutron Path Length</i>	198
8.2	Formulation	199
8.2.1	<i>Determination of the Elastic Strains from the Lattice Spacings</i>	199
8.2.2	<i>Relationship between the Measured Macroscopic Strain in a given Direction and the Elements of the Strain Tensor</i>	199
8.2.3	<i>Relationship between the Stress <math>\sigma_{i,j}</math> and Strain <math>\epsilon_{i,j}</math> Tensors</i>	200
8.3	Neutron Diffraction	201
8.3.1	<i>Properties of the Neutron</i>	201
8.3.2	<i>The Strength of the Diffracted Intensity</i>	202
8.3.3	<i>Cross Sections for the Elements</i>	203
8.3.4	<i>Alloys</i>	204
8.3.5	<i>Differences with Respect to X-rays</i>	205
8.3.6	<i>Calculation of Transmission</i>	205

8.4	Neutron Diffractometers	206
8.4.1	<i>Elements of an Engineering Diffractometer</i>	206
8.4.2	<i>Monochromatic Beam Diffraction</i>	206
8.4.3	<i>Time-of-flight Diffractometers</i>	209
8.5	Setting up an Experiment	210
8.5.1	<i>Choosing the Beam-defining Slits or Radial Collimators</i>	210
8.5.2	<i>Calibration of the Wavelength and Effective Zero of the Angle Scale, <math>2\theta_0</math></i>	210
8.5.3	<i>Calibration of a Time-of-flight Diffractometer</i>	210
8.5.4	<i>Positioning the Sample on the Table</i>	211
8.5.5	<i>Measuring Reference Samples</i>	211
8.6	Analysis of Data	211
8.6.1	<i>Monochromatic Beam Diffraction</i>	211
8.6.2	<i>Analysis of Time-of-flight Diffraction</i>	212
8.6.3	<i>Precision of the Measurements</i>	213
8.7	Systematic Errors in Strain Measurements	213
8.7.1	<i>Partly Filled Gage Volumes</i>	213
8.7.2	<i>Large Grain Effects</i>	214
8.7.3	<i>Incorrect Use of Slits</i>	214
8.7.4	<i>Intergranular Effects</i>	215
8.8	Test Cases	215
8.8.1	<i>Stresses in Indented Discs; Neutrons, Contour Method and Finite Element Modeling</i>	215
8.8.2	<i>Residual Stress in a Three-pass Bead-in-slot Weld</i>	218
	Acknowledgments	221
	References	221
<b>9</b>	<b>Magnetic Methods</b>	<b>225</b>
	<i>David J. Buttle</i>	
9.1	Principles	225
9.1.1	<i>Introduction</i>	225
9.1.2	<i>Ferromagnetism</i>	226
9.1.3	<i>Magnetostriction</i>	226
9.1.4	<i>Magnetostatic and Magneto-elastic Energy</i>	227
9.1.5	<i>The Hysteresis Loop</i>	228
9.1.6	<i>An Introduction to Magnetic Measurement Methods</i>	228
9.2	Magnetic Barkhausen Noise (MBN) and Acoustic Barkhausen Emission (ABE)	229
9.2.1	<i>Introduction</i>	229
9.2.2	<i>Measurement Depth and Spatial Resolution</i>	230
9.2.3	<i>Measurement</i>	232
9.2.4	<i>Measurement Probes and Positioning</i>	233
9.2.5	<i>Calibration</i>	233
9.3	The MAPS Technique	235
9.3.1	<i>Introduction</i>	235
9.3.2	<i>Measurement Depth and Spatial Resolution</i>	237