□ 应用统计学丛书

Extremes in Random Fields

A Theory and Its Applications

随机域中的极值统计学

理论及应用（英文版）

Benjamin Yakir 著

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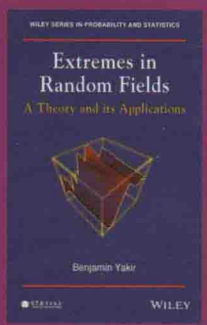

本书以通俗易懂的方式介绍了随机域中研究极值分布的某些新颖而有效的方法。全书分成两部分。第一部分总结随机域中极值的尾概率的渐近估计的一般方法。结合一些简单或者基本的例子，本书给读者展示一些经典的方法，同时也介绍了作者本人发展的一些方法，并对一些定理给出了数学证明。第二部分则介绍处理实际问题相对复杂且用传统的方法难以分析的技术，主要涉及5种应用，分别为基因组序列数据拷贝数变异探测、信号发生图像的连续监测、输入过程长时间交互缓冲溢出分析、Pickands常数模拟以及基于传感器网络基础的连续改变点检测，而上述应用的例子用经典的方法是难以分析的。

本书可作为概率和统计专业的高级课程或讨论班的教材，也可供相关专家参考。

Benjamin Yakir，耶路撒冷希伯来大学统计系教授，研究方向为极值统计学，发表了60余篇高质量文章，其中有10余篇发表在国际顶尖期刊。

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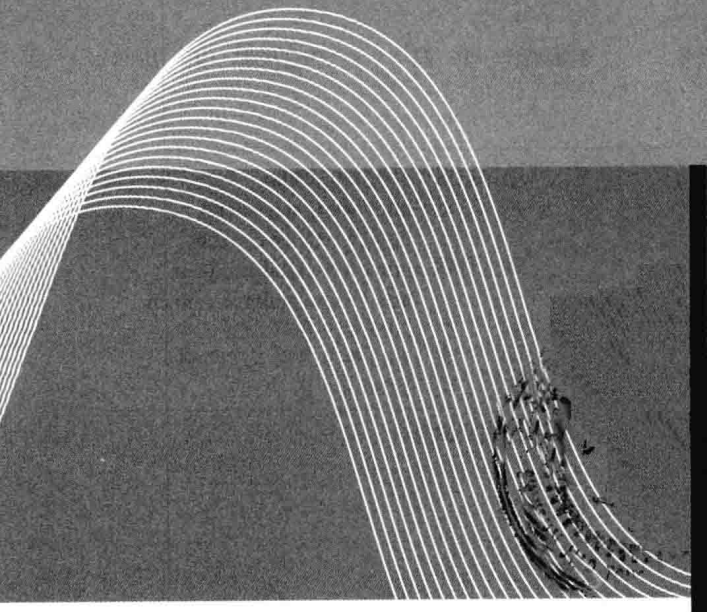

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To David

Preface

This text started as class notes for a course that I gave in the Mathematical Sciences Center (MSC) in Tsinghua University, Beijing, that got overblown and became a book. I was enjoying a sabbatical leave in the Department of Statistics and Applied Probability (DSAP) of the National University of Singapore when I was given an offer to teach a summer course in China. Of course I accepted. How could I resist the opportunity to fulfil a childhood dream of visiting China?

After accepting the proposal I had to decide what to teach. I decided to fulfil yet another dream, the dream of summarizing and unifying a subject I was writing about all my career, even before I knew what the subject was. The subject is the distribution of extremes in random fields and the analysis of statistical problems that can be formulated in relation to such extremes. Immediately after obtaining my PhD, and as a continuation of my PhD thesis, I was interested in the investigation of the average run length of the Shiryaev–Roberts change-point detection rule. Therefore, I found it natural to try to address a challenge that was presented to me by David Siegmund during a barbecue meal that he prepared for me in his yard. The challenge was to develop a simpler method for analyzing this average run length. In an attempt to attack this problem I began experimenting with the likelihood ratio identity, one of David's favorite techniques, and followed the road that eventually led me to writing this book.

The original problem was the investigation of average run length in a sequential change-point detection problem.[1] However, the basic technique that was developed turned out to be useful for the investigation of a relatively wide array of different statistical problems that involve the distribution of maxima.[2] Among other things, David and I used the method in order to investigate the significance level of sequence alignment, for the computation of the false detection rate in

[1] Yakir B., Pollak M. A new representation for the renewal-theoretic constant appearing in asymptotic approximations of large deviations. Ann. Appl. Probab. **8**, 749-774 (1998).

[2] Grossman S., Yakir B. Large deviations for global maxima of independent superadditive processes with negative drift and an application to optimal sequence alignment. Bernoulli **5**, 829–845 (2004).

Seigmund D.O., Yakir B. Approximate p-values for local sequence alignments. Ann. Statist. **28**, 657–680 (2000).

Seigmund D.O., Yakir B. Statistical analysis of direct identity by descent mapping. Ann. Hum. Genet. **67**, 464–470 (2003).

Seigmund D.O., Yakir B. Correction note: Approximate p-values for local sequence alignments. Ann. Statist. **31**, 1027–1031 (2003).

scanning statistic, for producing more efficient ways of simulation, etc. Each application required this modification or that trick in order to apply the basic principle. However, after 20 years of repeating the same argument even I was able to identify the pattern. The thrust of this book is a description of the pattern and the demonstration of its usefulness in the analysis of nontrivial statistical problems.

The basic argument relies on a likelihood ratio identity that uses a sum of likelihood ratios. This identity translates the original problem that involves the approximation of a vanishingly small probability to a problem that calls for the summation of approximations of expectations. The expectations are with respect to alternative distributions in which the event in question is much more likely to occur. Moreover, by carefully selecting the alternative distributions one may separate the leading term in the probability from the expectations that form the sum, enabling the investigation to concentrate on finer effects.

The method is useful since it does not rely on the ordering of the parameter set and it does not require the normal distribution. In many applications, some of them are presented in the book, a natural formulation of the model calls for the use of collections of random variables that are parameterized not by subsets of the real line. Frequently, the normal assumption may fit the limit in a central limit formulation but may not fit as a description of the extreme tail. In all such cases an alternative to the methods that are usually advocated in the literature are required. The method we present is such an alternative which we felt others may benefit from by knowing about.

This is why we wrote the book. But who is the target audience? This is a tough call. Even if I may state otherwise, the book requires a relatively advanced knowledge in probability as background, perhaps at the level of Durrett's book.[3] Prior knowledge in statistics is an advantage. Indeed, there is an appendix that lists theorems and results and can be used as reference for the statements that are made in the book. Still, I guess that this book is not an easy read even for experts, and much less so for students.

With this warning in mind, I hope that the effort that is required in reading the book will be rewarding. Definitely, for an expert who wants to add yet another method to his toolbox but also for a student who wants to become an expert.

Seigmund D.O., Yakir B. Significance level in interval mapping. In Development of Modern Statistics and Related Topics, Series in Biostatistics, Volume 1. World Scientific Publishing, River Edge, NV, 10–19 (2003).

Shi J., Siegmund D.O., Yakir B. Importance sampling for estimating p-values in linkage analysis. JASA **102**, 929–937 (2007).

Yakir B. On the average run length to false alarm in surveillance problems which possess an invariance structure. Ann. Statist. **26**, 1198–1214 (1998).

Yakir B. Approximation of the p-value in a multipoint linkage analysis using grandparent grandchild pairs and partially informative markers. Nonlinear Anal. **47**, 1973–1984 (2001).

Yakir B. Discussion on "Is average run length to false alarm always an informative criterion?" by Yajun Mei. Sequential Analysis **27**, 406–410 (2008).

[3] Durrett R. Probability: Theory and Examples (2nd Edition). Duxbury Press, Belmont, CA (1995).

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For such students, the book can be used as a basis for an advanced seminar. Reading chapters of the book can be used as a primer for a student who is then required to analyze a new problem that was not digested for him/her in the book. This is how I intend to use this book with my students.

The teacher can start such a course by discussing Chapters 1–4 that give the basic background and demonstrate the technique. Chapter 5 is more technical and can be skipped, unless the main interest is in the mathematical details. From the second part of the book it is probably recommended to go over Chapter 6, which is of an intermediate level of difficulty, and then read some or all of Chapters 7–10 depending on the interests of the teacher and the students and on the time constraints.

Acknowledgments

My first acknowledgments are to environments, and especially the people who enabled these environments. The first half of the book was written mainly in DSAP. I know of no better place to do this type of scientific work. I will always be grateful. The second place is MSC. Without them I do not know when, if at all, this book would have been written. Next, I would like to recognize the financial support that I got from the Israel Science Foundation (Grant No. 325/09) and from the US–Israel Binational Science Foundation (Grant No. 2006101). This support was instrumental for the development of the original work that led to the applications that are presented in the second part of the book.

Some of the people that gave me a helping hand I would like to mention by name. Unfortunately, I cannot give the names of the anonymous reviewers who made very useful suggestions on the first draft of the book and helped me improve it. But I can give the name of the editor from Higher Education Press, Liping Wang. Thanks to her this is a book and not just class notes. Also I would like to thank Yuval Nardi, Moshe Pollak, Ton Dieker and Nancy Zhang who coauthored with David Siegmund and myself some of the works that are related directly to the content of the book.

And finally there is David Siegmund. The work presented in this book is basically our joint work. The only reason that we do not share authorship is the fact that I wanted to dedicate this book to him as my modest contribution to the celebration of his career and his accomplishments and as an appreciation for what he gave me. It is not appropriate for a book to be dedicated to one of its authors. So here it is: this is for you, David.

February 2013 Benjamin Yakir, Jerusalem, Israel

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