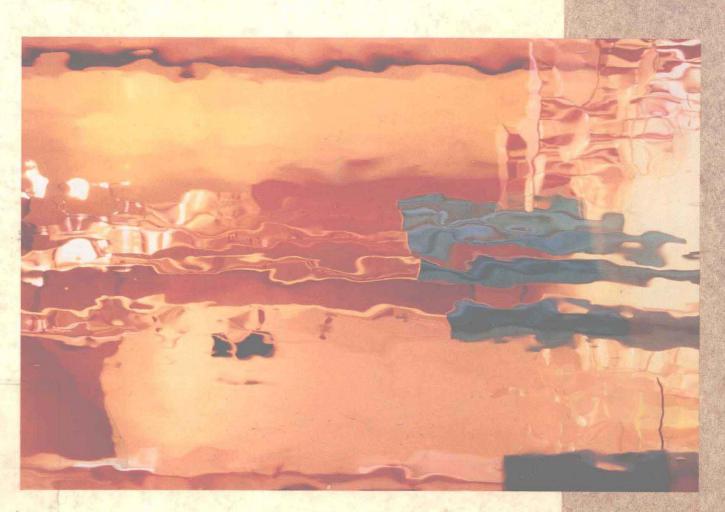
# INTERMEDIATE ALGEBRA WITH EARLY FUNCTIONS

S E C O N D E D I T I O N

James W. Hall



# INTERMEDIATE ALGEBRA WITH EARLY FUNCTIONS SECOND EDITION

James W. Hall Parkland College



### PWS PUBLISHING COMPANY

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Thomas Nelson Australia 102 Dodds Street South Melbourne, 3205 Victoria, Australia

Nelson Canada 1120 Birchmount Road Scarborough, Ontario Canada MIK 5G4

International Thomson Editores Campos Eliseos 385, Piso 7 Col. Polanco 11560 Mexico D.F., Mexico

International Thomson Publishing GmbH Königswinterer Strasse 418 53227 Bonn, Germany

International Thomson Publishing Asia 221 Henderson Road #05-10 Henderson Building Singapore 0315

International Thomson Publishing Japan Hirakawacho Kyowa Building, 31 2-2-1 Hirakawacho Chiyoda-ku, Tokyo 102 Japan

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Sponsoring Editor: David Dietz Editorial Assistant: Julia Chen

Developmental Editors: Maureen Brooks/Barbara Lovenvirth Production Coordinators: Susan Caffey/Patricia Adams

Production: Lifland et al., Bookmakers Interior/Cover Designer: Julie Gecha

Interior Illustrators: Scientific Illustrators/Tech-Graphics

Cover Photo/Art: © 1994 Ken Morigami/Panoramic Images, Chicago

Marketing Manager: Marianne C. P. Rutter Manufacturing Coordinator: Lisa Flanagan Compositor: Clarinda Company

Cover Printer: John P. Pow Company, Inc. Text Printer and Binder: Quebecor/Hawkins

Printed and bound in the United States of America.

Library of Congress Cataloging-in-Publication Data

Hall, James W.

Intermediate algebra with early functions /

James W. Hall. - 2nd ed. cm.

p. Includes index.

ISBN 0-534-94026-9

1. Algebra. I. Title.

QA152.2.H364 1995 512.9-dc20

94-31430 CIP

95 96 97 98 99 — 10 9 8 7 6 5 4 3 2

# INTERMEDIATE ALGEBRA WITH EARLY FUNCTIONS

# Preface

Intermediate Algebra with Early Functions, Second Edition, is intended to prepare students for a course in college algebra, finite mathematics, or statistics or for other further study in mathematics. It will also equip students for employment in a world where the importance of quantitative reasoning skills is continually increasing. The text features the introduction of graphs and linear functions in Chapter 2; this early introduction of linear functions ensures that fresh material is presented to the student. Coverage of functions and graphing continues throughout the text. See the Table of Contents for an overview of how the coverage is thoroughly integrated.

The text's organization allows for the appropriate use of graphics calculators throughout. The main emphasis is on making mathematical concepts the message, with the graphics calculator used as the messenger wherever it is relevant. This early and graduated use of graphics calculators will provide important background for other courses. This book is designed to work both in classes that fully incorporate the graphics calculator and in those where the instructor uses it occasionally (if only for demonstration purposes). Where appropriate in examples that utilize the graphics calculator, the text illustrates keystrokes for the TI-82 graphics calculator as a model for the student. However, any graphics calculator can be substituted.

Presentation of new ideas in early chapters, appropriate use of modern technology, and inclusion of more real-life applications are all features of this edition designed to produce improvement both in student attitudes and in student performance.

The fundamental organization of this edition builds on the successful presentation of the first edition. New material is introduced clearly and concisely. Examples give the student both a clear mathematical model of the given problem and detailed side-bar explanations of this model. Student aids are abundant and are integrated with the concepts being taught. The exercises contain adequate drill on the basics, as well as material to help students grow mathematically and construct their own bridges between skills and concepts.

Careful pedagogy is employed to ensure that the sections flow and are appropriate for a single lecture. For instance, the general case for the distance formula is developed side by side with a special case. Throughout the text, concepts are related to ideas the students have seen before; then these concepts are developed to a level that will enable students to apply them easily.

### **FEATURES**

### New

- Early Introduction to Functions and Graphs Early introduction of functions and graphing allows the appropriate use of graphics calculators throughout the book. It also serves to present fresh material to the student who has already completed a Beginning Algebra course. Early in the text many graphs are approximated by broken-line graphs. Thus students can approximate the graphs of a variety of functions without doing anything more complicated than connecting two points with a line segment. This introductory approach opens the door to graphing functions without confronting students with a difficult discussion.
- Appropriate Use of Technology Use of scientific and graphics calculators is illustrated wherever appropriate. The emphasis is on the mathematical concepts, with the technology included when it serves a purpose.
- Emphasis on Estimation Skills Skills in estimating and checking for the
  reasonableness of answers are emphasized through exercises designed specifically for this purpose. The appropriate use of technology should be accompanied by a corresponding concern for what is reasonable. The number
  of exercises on estimation skills has been increased in this edition.
- Focus on Problem Solving Consistent with NCTM recommendations, the
  text focuses on problem solving. There is an early introduction to translating word statements into algebraic statements, and this approach is reinforced throughout the book. Word problems are worked by first forming a
  word equation, which is then translated into an algebraic equation. The
  use of general principles and tables is emphasized to help the student see
  the connections that exist between different problems.

### New

Chapter-Opening Applications Each chapter opens with an application
carefully developed to present the chapter topics in interesting and motivational situations using real-life data provided by industry experts. Students
generally work harder when they perceive the material as relevant and important. These chapter openers illustrate the relevance of the mathematics
in the chapter and also show possible career opportunities in mathematics.

### New

 Active Applications These collaborative learning projects, which follow up on selected chapter-opening applications, provide opportunities for students to practice working cooperatively.

### New

Mathematical Notes Students should understand that the mathematics they
are studying was developed by many civilizations over a long period of time.
The Mathematical Notes show where much of the notation we use today
came from. They also place mathematics in a more interesting context.

Preface xiii

### New

- Geometric Viewpoints It is appropriate for students who are first viewing new concepts to meet these concepts geometrically, since many of the algebraic methods that we use today were first discovered and used in geometric form.
- Multiple Representations Students really understand mathematical principles when they have internalized them and can interpret them from multiple representations. Thus many exercises in the text ask about the same concept from a variety of perspectives. Students will experience the rule-of-three approach, as they see examples and exercises that present real-life functions in numerical, graphical, and algebraic forms.

### New

Discussion Questions Students should be able to organize their mathematical ideas and to express them clearly to others. The practice they will receive when responding to the Discussion Questions will not only improve their understanding of mathematics but also contribute to their total education.

### New

- Challenge Questions These exercises are designed to increase the interest of some students and to foster a variety of problem-solving skills.
- Self-Check Exercises Self-check exercises are interspersed throughout for students to check their progress.

### New

Section Skill Reinforcers Each section after Section 1-1 contains five exercises that review key skills from earlier in the text.

### New

Chapter Reviews, Mastery Tests, and Cumulative Reviews Each chapter
has a set of Review Exercises reviewing the entire chapter and a Mastery
Test keyed to the chapter objectives. A new Cumulative Review is located
after every third chapter.

### New

Titling of Examples and Exercises
 The examples and application exercises have been titled to facilitate the referencing of material by both students and instructors.

### New

• Full Color The use of full color enlivens the book for the student and facilitates the emphasis of key features. The palette of colors was carefully selected to enhance the pedagogical features of the text.

### AN APPLICATION

### Time Out for Calculating?

Many professional athletes and coaches now use sophisticated mathematics, implemented on computers, to gain a competitive edge over their opponents. Baseball managers use computers with statistics programs to determine which pitches batters are poorest at hitting. Marathon runners use computer-based motion analysis to fine tune their strides for maximum efficiency. And in mid-race yacht captains use laptop computers to compute optimal sail configurations, based on changing weather conditions.

But not all mathematical applications in sports require the use of computers. The motion of a ball in flight, such as a basketball shot toward a hoop or a football kicked toward a goalpost, can be described fairly well using a quadratic equation. The same sort of equation can describe the motion of a javelin or shot put. Analyzing such an equation can yield useful information. Suppose, for example, that you are a track-and-field coach looking at films of one of your shot-putters at practice; you are watching for the angle at which the shot put leaves the thrower's hand. Using techniques from calculus, it is possible to derive the angle that gives maximum distance. Intuitively, what do you think that angle would be?

The actual path of a thrown or kicked object can be illustrated by the graph of its quadratic function. The graph provides a means of analyzing certain aspects of the flight of the object, including the hang time of a punted football, given its initial upward velocity. **Applications** present chapter topics in interesting situations.

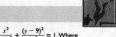
Active Application

493

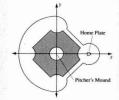
### ACTIVE APPLICATION

We will now analyze the motion of a baseball pitch the familiar curve bail. Place the pitcher's mound at the origin of a coordinate system, and center the front edge of home plate 60 feet away on the positive x-axis. A curve ball thrown by a right-handed pitcher will have a counterclockwise spin, as viewed by the batter, and the pitch will curve toward the first quadrant. A curve ball's motion is actually quite complicated, but the curving path has several reasonable approximations.

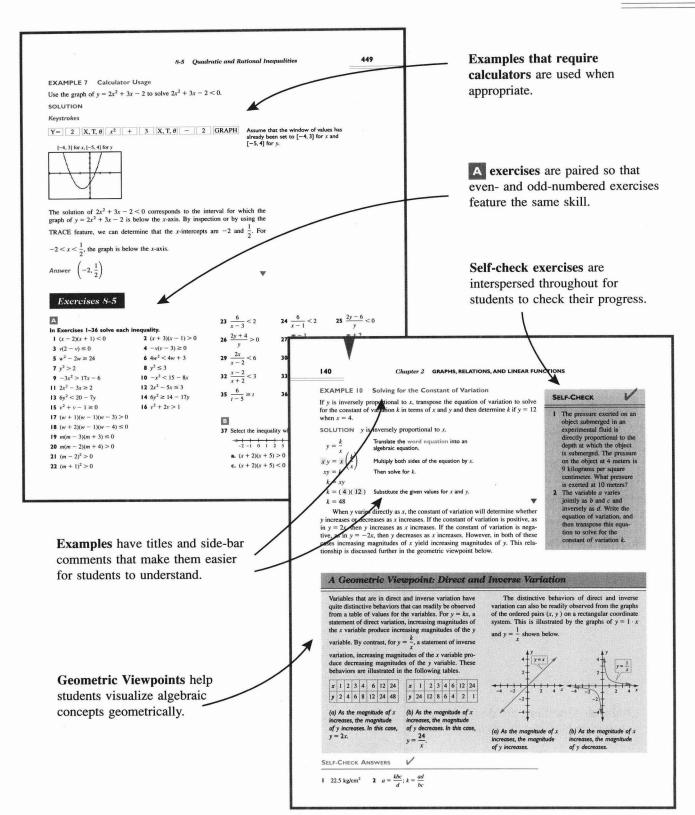
- I We can treat the ball's path as a part of a parabola. Suppose the ball leaves the pitcher's hand at (0, -1), initially traveling parallel to the x-axis and reaching home plate over the exact center of its front edge. If the ball's departure point is the vertex of the parabola, what is an equation for the ball's path.
- 2 If, as many baseball people say, a curve ball hooks more sharply toward the end of its flight than at the beginning, then an ellipse with major axis parallel to the x-axis may be a still better way to describe a curve ball's flight. Suppose the ball travels along

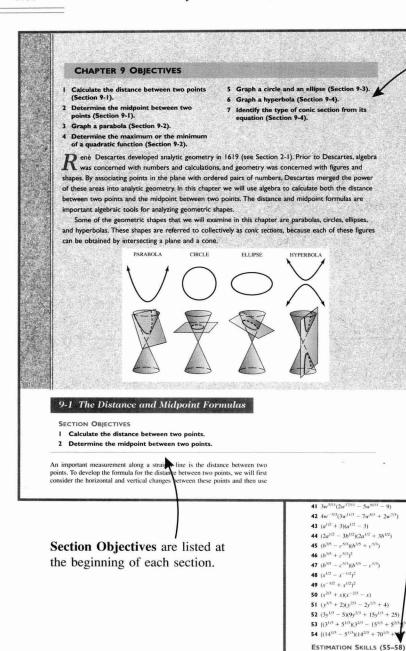


will it be when it passes the front edge of home plate? If the ball has to pass the front edge of home plate within  $\frac{3}{4}$  ft of its center for a strike, will the pitch be a strike or a ball?



**Active Applications,** keyed to chapter-opening applications, follow selected chapters.

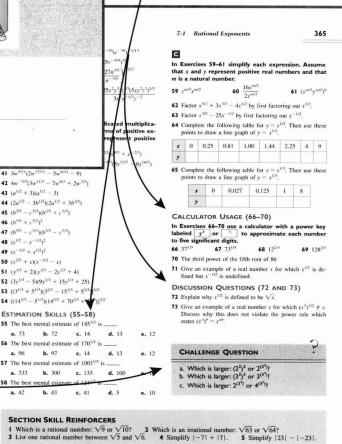




Challenge Questions are designed to foster problem-solving skills.

Section Skill Reinforcers review key skills from previous sections. Chapter Objectives, keyed to sections, begin each chapter.

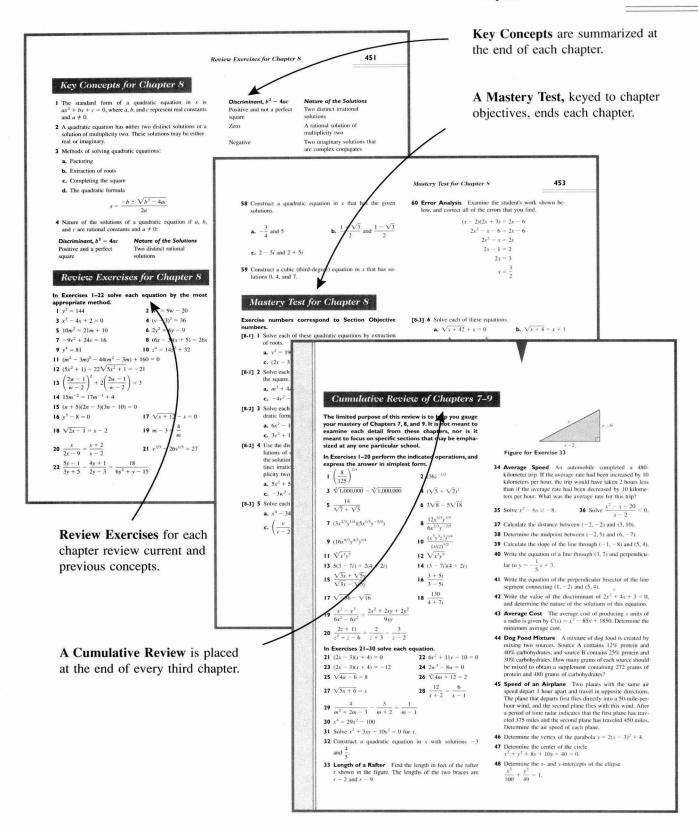
**Exercises in Calculator Usage** and Estimation Skills are featured in most sections, as are Discussion Questions.



a. 73 b. 72 c. 14

**b.** 43

58 The best mental estimat a. 42



### SUPPLEMENTS TO ACCOMPANY THE TEXT

### For Instructors:

- Instructor's Edition contains answers to all exercises in a section at the end
  of the book.
- *Instructor's Manual* has answers to all exercises and suggested procedures, where appropriate, for Challenge Questions.
- Test Bank with Transparency Masters contains all questions and answers from the computerized test bank, three ready-to-use tests (two open-ended and one multiple choice) for each chapter, two final examinations, and a set of transparency masters.
- Computer Testing Software is available both for the IBM and compatibles
  and for the Macintosh. These computerized test banks contain multiplechoice and open-ended questions and allow the user to edit, rearrange, and
  add to the question bank. EXPTest runs on Windows or DOS, and ExamBuilder runs on the Macintosh.

### For Students:

- Student Solutions Manual contains a complete worked-out solution for every other odd problem.
- MathQuest Tutorial Software is an interactive, text-specific tutorial which
  runs on both Windows and Macintosh platforms. The program poses fill-in
  and multiple-choice questions. If a student answers a question incorrectly,
  the program will first respond with hints; if the student answers incorrectly
  a second time, the program will supply a step-by-step solution. Scorekeeping capabilities enable students to monitor their progress. DOS Tutorial Software with similar capabilities is also available.
- Videotape Series features professional math instructors and reviews key topics in the text. These tutorial tapes, produced by Educational Video Resources, are free to adopters for use in math labs.
- Video Guidebook provides exercises that link the content of the text to the
  videos. For each video that accompanies the text, a three-part lesson ("Pretest," "While You Watch," and "Posttest") engages the student in active
  learning. All answers are provided, making this worktext especially helpful
  for independent learners.

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