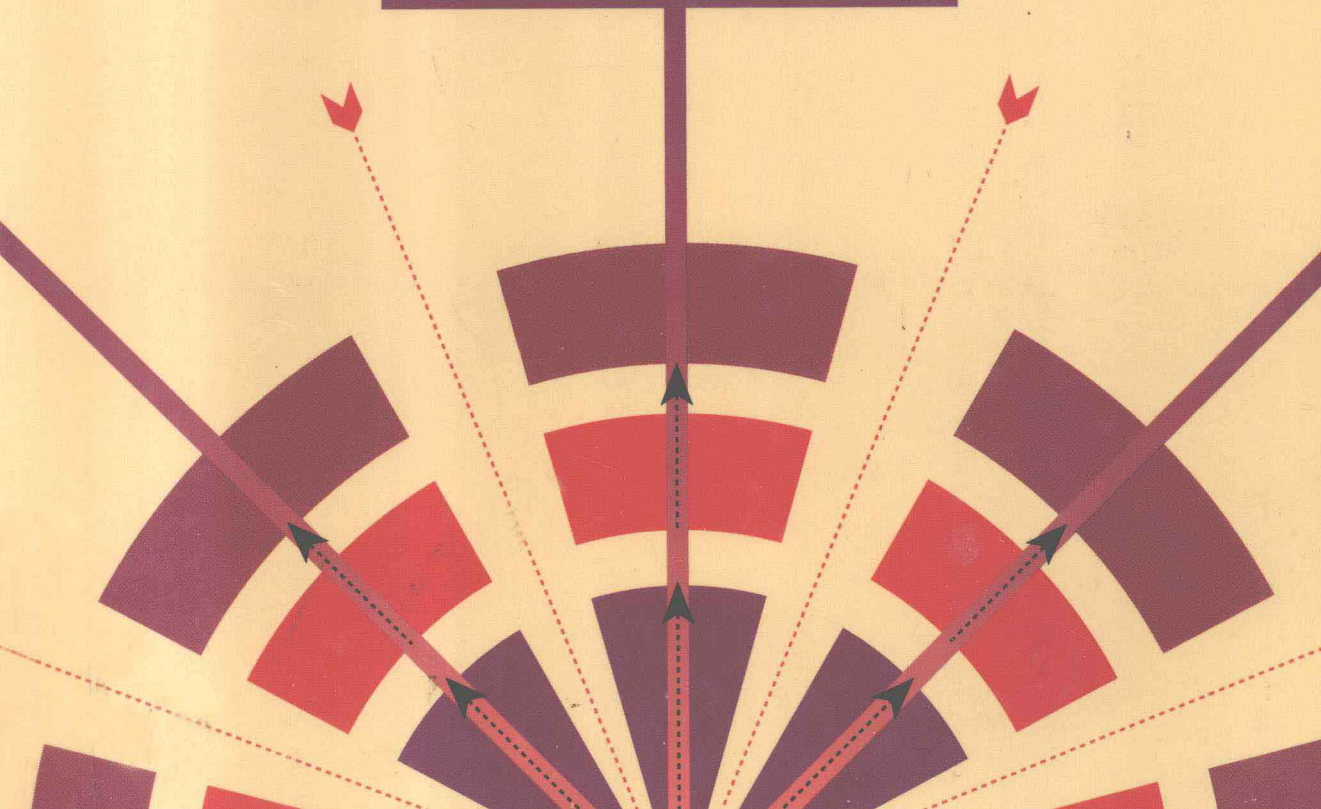


FOUNDATIONS
for
GATHERING
and
INTERPRETING
BEHAVIORAL
DATA

Robert Thomas Maleske



FOUNDATIONS FOR GATHERING AND INTERPRETING BEHAVIORAL DATA

An Introduction to Statistics

Robert Thomas Maleske

Carthage College



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I dedicate this work to Marianne, my wife, whose love, support, and patience are between the lines;

to Melissa, my daughter, whose love for reading inspires me to write;

to my sister, Carol Anne Maleske Restis, and brother-in-law, Robert Restis, who supported me in high school and college after the untimely deaths of my parents;

to Marianne's parents, Frank Adamczyk and Theresa Giacchino Adamczyk, who helped us in countless ways during our graduate school years;

in loving memory of my own parents, Thomas Joseph Maleske and Dorothy Kruder Maleske, whose lives and values continue in my writing;

and to my beloved grandmother, Ruth Anderson Kruder, who, at the age of 98, continues to inspire my growth.

P R E F A C E

Many textbooks are available to those who are studying statistical analyses; this is not one of them. This book is for those who want or are expected to gain a fundamental understanding of the *total process* of gathering and interpreting behavioral data, and who are willing to study the basic issues and concepts involved in this process, of which statistics is only a part.

At the heart of my motivation to write this book is a firm belief that we can understand new information more easily when we can connect it with our own experience. All of us have observed the behavior of people and things; asked questions based on our observations; made our interpretations; and tested the validity of our explanations with additional observations. This universal experience is the foundation—and the only prerequisite—for using this book.

As the title indicates, my overall objective is to help readers understand the *process* of gathering and interpreting behavioral data. You will notice in the table of contents that the headings almost always contain active verbs—for example, “Recognizing the difference between data and information.” This is because I emphasize actual skills rather than abstract concepts.

This book is in part my response to other texts on elementary statistics and research methods. Typically, these books focus on inferential statistical analyses *per se*, as if understanding them were an end in itself; often, the names of statistical tests—*t*-tests, for example—will be used as chapter titles. In contrast, the structure of this book emphasizes developing skills and understanding concepts that are prerequisites to knowing when and how to use statistical analyses. Specifics regarding inferential analyses are postponed until Part Four, after a larger and more coherent context is in place.

Few students find statistics intrinsically interesting. However, I have found that they are more willing to absorb the material if it emphasizes logical concepts rather than complex statistical formulas. In that case, they can recognize its relevance to everyday decision making.

Acknowledgments

I used to wonder why authors go on and on with acknowledgments; now I understand.

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No textbook can be completed without a reality check. I appreciate the efforts of Steve Prosavac and Yi-Chun Sun of the University of Utah, who tested all the calculations, and the contributions of my students and of all readers—past, present, and future—who respect my work enough to challenge it and make thoughtful suggestions for improvement.

I could not have kept my nose to the word processor day after day without the support of my colleagues: Larry Hamilton, whose wisdom and sensitivity helped me keep everything in perspective; Ingrid Tiegel, whose professional commitment provided me with a model of persistence; George Catlin, who helped me balance the statistical with the spiritual; and Donald Michie, whose encouragement and respect added to my confidence.

To all my friends and relatives, too numerous to mention, whose encouragement and support were like fresh breezes during the doldrums every writer confronts; and to our good friend Judy Krieger, who gave Melissa a wonderful place to be when I had deadlines and Marianne had professional commitments: Thank you!

In closing, I want to recognize the wisdom of Albert Erlebacher, whose good advice during my graduate years at Northwestern has stayed with me during twenty years of teaching, and which I continue to pass on to my students: Never collect research data until you know which statistics will be appropriate!

Robert Thomas Maleske

B R I E F C O N T E N T S

1 AN OVERVIEW 1

- 1 Understanding the Total Process of Gathering and Interpreting Data 3

2 UNDERSTANDING DESCRIPTIVE STATISTICS 16

- 2 Understanding Measurement 19
- 3 Organizing Your Measurements 39
- 4 Summarizing Your Measurements 57
- 5 Showing Your Summaries 83
- 6 Standardizing Scores 97

3 UNDERSTANDING INFERENTIAL STATISTICS 132

- 7 Understanding the Rationale for Inferential Statistics 135
- 8 Structuring Scientific Observations 145
- 9 Making Decisions about Scientific Theories 159
- 10 Applying the Rules of Probability to Hypothesis Testing 173

4 SELECTING AND INTERPRETING STATISTICAL ANALYSES 198

- 11 Selecting Statistical Analyses 201
- 12 Understanding Statistical Analysis Formulas 217
- 13 Interpreting the Results of Inferential Analyses 237

Appendix A Databases 255

Appendix B Tables 264

Appendix C Calculations and Analysis Scenarios 313

Appendix D Answers to Selected Exercises 445

C O N T E N T S

1 AN OVERVIEW 1

1 Understanding the Total Process of Gathering and Interpreting Data 3

- Observing, Questioning, Explaining, Predicting 4
- Data versus Information 7
- Interpretation versus Decision Making 9
- Formal versus Informal Processes 10
- The Total Process of Gathering and Interpreting Data 11
- Descriptive Statistics versus Inferential Statistics 11
- Populations and Samples 11
- Representativeness 12
- Random Selection 13
- Overview of This Book 13
- Summary 13
- Key Terms and Concepts 14
- Exercises 14

2 UNDERSTANDING DESCRIPTIVE STATISTICS 16

2 Understanding Measurement 19

- Observing and Experiencing 20
- What Is Behavior? 22
- Operational Definitions 24
- Measurement Validity 26

	Levels of Measurements	26
	Precision of Measurement	33
	Regarding Appendix A	34
	Summary	34
	Key Terms and Concepts	36
	Exercises	36
3	Organizing Your Measurements	39
	Sorting Measurements	40
	Grouping Measurements	41
	Counting Measurements	42
	Creating Frequency Distribution	42
	Cumulative Frequencies	46
	Apparent Class Intervals and Real Class Intervals	51
	Summary	55
	Key Terms and Concepts	55
	Exercises	56
4	Summarizing Your Measurements	57
	Introduction	59
	Computing Averages (Means)	59
	Computing Modes	63
	Choosing among Means, Medians, and Modes	64
	Central Tendency	67
	Statistics and Parameters Revisited	67
	Variability	68
	Computing Ranges	69
	Range as an Index of Variability	71
	Average Absolute Deviation as an Index of Variability	72
	Terminal Statistics	74
	Variance as an Index of Variability	74
	Standard Deviation as an Index of Variability	78
	Calculation Formulas for Standard Deviation and Variance	80
	Summary	81
	Key Symbols	81
	Key Terms and Concepts	81
	Exercises	82

5 Showing Your Summaries 83

Choosing between Tables and Graphs 84

Creating Tables 86

Creating Graphs 86

Types of Tables 88

Types of Graphs 89

Frequency Distributions 92

A Final Comment on Graphs 95

Summary 95

Key Terms and Concepts 95

Exercises 95

6 Standardizing Scores 97

Introduction 98

What Is a Standardized Score? 101

Understanding the Normal Curve 104

Hypothetical versus Empirical Distributions 106

Using the Normal Curve as a Model 108

Shape of the Normal Curve 114

Using the Normal Curve to Estimate Percentiles and
Percentile Ranks 118

From Descriptive to Inferential Statistics 122

Estimating (Inferring) Parameters from Sample Statistics 124

Sample Standard Deviation as an Estimate of the Population Standard
Deviation 126

Unbiased Estimates of the Population Standard Deviation 127

Standardized Scores Revisited 129

Summary 129

Key Symbols 130

Key Terms and Concepts 130

Exercises 130

3 UNDERSTANDING INFERENTIAL STATISTICS 132

7 Understanding the Rationale for Inferential Statistics 135

Introduction 136

Human Curiosity Revisited 136

	The Scientific Process	137
	What Is a Theory?	138
	What Is a Hypothesis?	140
	Inferential Statistics	141
	Summary	142
	Key Terms and Concepts	142
	Exercises	142
8	Structuring Scientific Observations	145
	The Primary Objective of Science	146
	Uncontrolled Observations versus Controlled Experiments	147
	The Relationship between Theory and Hypothesis	152
	Representativeness and Random Sampling	153
	Random Sampling versus Random Assignment	155
	Summary	155
	Key Terms and Concepts	156
	Exercises	156
9	Making Decisions about Scientific Theories	159
	Stating Null Hypotheses	160
	Stating Alternative Hypotheses	162
	Defining Hypotheses Operationally	164
	Comparing Test Results with Probabilistic Models	165
	Using the Additive Rule of Probability	166
	Using the Multiplicative Rule of Probability	166
	General Strategies for Solving Probability Problems	167
	Replacement or Nonreplacement?	169
	Summary	170
	Key Terms and Concepts	170
	Exercises	170
10	Applying the Rules of Probability to Hypothesis Testing	173
	Applying Probability to Hypothesis Testing	174
	Using the Binomial Distribution as a Model	178
	The Binomial Formula	178
	Statistical Significance and Statistical Power	183
	Using the Normal Distribution as a Model	184

Establishing Sampling Distributions	186
Sampling Distribution of Differences	191
The Logic of Sampling Distributions	193
Type-I versus Type-II Errors	193
Statistical Power Revisited	194
Summary	196
Key Symbols	196
Key Terms and Concepts	196
Exercises	197

4 SELECTING AND INTERPRETING STATISTICAL ANALYSES 198

11 Selecting Statistical Analyses 201

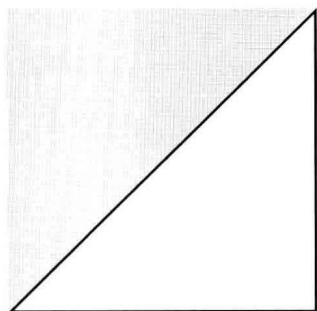
Relationship between Hypotheses and Data Collection Strategies	202
Relationship between Data Collection Strategies and the Choice of Statistical Analysis	203
Relationship between the Type of Data and the Choice of Statistical Analysis	205
Determining Which Statistical Analysis to Use by Means of the Decision Tree	207
Examples of the Decision-Making Process	212
Summary	214
Key Terms and Concepts	214
Exercises	214

12 Understanding Statistical Analysis Formulas 217

Review of Hypothesis Testing Logic	218
General Logic of Inferential Statistical Analysis	219
Pearson r Analysis	221
Spearman r Analysis	223
Relationship between the Z Analysis and t -test Analysis	224
Inflated Alpha	225
Analysis of Variance	225
Limitations of the Analysis of Variance	227
Scheffe Analysis	227

Interaction	228
Factorial Analysis of Variance	230
Complex Experimental Designs	231
Simple Chi Square Analysis	231
Nonparametric Analysis	232
Summary	233
Key Symbols	233
Key Terms and Concepts	234
Exercises	234
13 Interpreting the Results of Inferential Analyses	237
General Considerations	238
Information Required	239
Using the Tables of Critical Values	242
Stating Statistical Conclusions	245
Relating Statistical Conclusions to Research Hypotheses	247
Stating Plain English Conclusions	250
Interpreting Computer-Generated Outputs	250
Summary	251
Key Words and Concepts	252
Exercises	252
Appendix A Databases	255
Appendix B Tables	264
Appendix C Calculations and Analysis Scenarios	313
Appendix D Answers to Selected Exercises	445

AN OVERVIEW



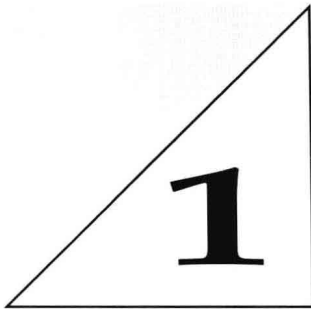
1

Understanding the Total Process of
Gathering and Interpreting Data

1

Although Part One consists of only one chapter, it is not merely a polite opening leading to the meat and potatoes of later chapters. The material in Chapter 1 lies at the core of everything that follows. Its message is that gathering data and interpreting data are not discrete processes; they are but steps in a total process. The individual chapters that follow provide the foundations for understanding that process and how the separate steps work together.

Understanding the Total Process of Gathering and Interpreting Data



Observing, Questioning, Explaining, Predicting
Data versus Information
Interpretation versus Decision Making
Formal versus Informal Processes
The Total Process of Gathering and Interpreting Data
Descriptive Statistics versus Inferential Statistics
Populations and Samples
Representativeness
Random Selection
Overview of this Book
Summary
Key Terms and Concepts
Exercises

OBJECTIVES

After reading and studying Chapter 1 you should understand the following.

- *making observations, formulating questions, explaining observations, and making predictions are fundamental to human existence.*
- *the difference between data and information.*
- *the difference between interpreting information and making a decision based on that information.*
- *the difference between formal and informal approaches to gathering and interpreting data.*
- *gathering and interpreting data are not separate processes but elements of a total process.*
- *the difference between descriptive and inferential statistics.*
- *the difference between populations and samples.*
- *representativeness.*
- *random selection.*
- *the overall structure of this textbook.*

OBSERVING, QUESTIONING, EXPLAINING, PREDICTING

For all organisms, including humans, survival depends on responding and adapting to conditions in the environment. To respond and adapt means to (a) observe what is going on, (b) ask questions about why things happen as they do, (c) seek explanations for our questions, and (d) make predictions about what might happen. The more successful we are at responding and adapting, the more likely we are to “live long and prosper,” in the words of Mr. Spock.