# Air Dispersion Modeling

Foundations and Applications

Alex De Visscher



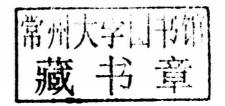
WILEY

# AIR DISPERSION MODELING

# Foundations and Applications

### **ALEX DE VISSCHER**

University of Calgary





Copyright © 2014 by John Wiley & Sons, Inc. All rights reserved.

Published by John Wiley & Sons, Inc., Hoboken, New Jersey. Published simultaneously in Canada.

No part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanical, photocopying, recording, scanning, or otherwise, except as permitted under Section 107 or 108 of the 1976 United States Copyright Act, without either the prior written permission of the Publisher, or authorization through payment of the appropriate per-copy fee to the Copyright Clearance Center, Inc., 222 Rosewood Drive, Danvers, MA 01923, (978) 750–8400, fax (978) 750–4470, or on the web at www.copyright.com. Requests to the Publisher for permission should be addressed to the Permissions Department, John Wiley & Sons, Inc., 111 River Street, Hoboken, NJ 07030, (201) 748–6011, fax (201) 748–6008, or online at http://www.wiley.com/go/permission.

Limit of Liability/Disclaimer of Warranty: While the publisher and author have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. No warranty may be created or extended by sales representatives or written sales materials. The advice and strategies contained herein may not be suitable for your situation. You should consult with a professional where appropriate. Neither the publisher nor author shall be liable for any loss of profit or any other commercial damages, including but not limited to special, incidental, consequential, or other damages.

For general information on our other products and services or for technical support, please contact our Customer Care Department within the United States at (800) 762–2974, outside the United States at (317) 572–3993 or fax (317) 572–4002.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic formats. For more information about Wiley products, visit our web site at www.wiley.com.

Library of Congress Cataloging-in-Publication Data

De Visscher, Alex, 1970-

Air dispersion modeling: foundations and applications / Alex De Visscher, Canada Research Chair in Air Quality and Pollution Control Engineering, Department of Chemical and Petroleum Engineering, and Centre for Environmental Engineering Research and Education (CEERE), Schulich School of Engineering, University of Calgary.

pages cm

Includes bibliographical references and index.

ISBN 978-1-118-07859-4 (hardback)

1. Air–Pollution–Simulation methods. 2. Atmospheric diffusion–Simulation methods. I. Title.

TD883.1.D45 2013

628.5'3011-dc23

2013009404

Printed in the United States of America



## LIST OF SYMBOLS

```
acceleration (m s-2)
a
            activity (-)
            droplet surface area per unit air volume (m^2 m^{-3} = m^{-1})
A
            frequency factor [s<sup>-1</sup> (first order); cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup> (second order)]
            absorbance (-)
            frontal area (m2)
A_{\epsilon}
            plan area (m<sup>2</sup>)
            total area (m<sup>2</sup>)
A_{\scriptscriptstyle \mathrm{T}}
            stack cross-sectional area (m2)
A
             Bowen ratio (-)
B
            empirical constant (m2 µg-1)
b
            speed of light in vacuum (m s<sup>-1</sup>)
             amount concentration or mass concentration (mol m<sup>-3</sup> or g m<sup>-3</sup>)
             Cunningham slip correction factor (-)
C
             number concentration (molecules cm<sup>-3</sup>)
             gas-phase concentration in equilibrium with the surface (µg m<sup>-3</sup>)
C_0
             Lagrangian structure function constant (-)
             air-phase pollutant concentration (µg m<sup>-3</sup>)
C_{air}
             drag coefficient (-)
C_{\rm D}
C_{G}
             net radiation fraction going into the ground (-)
             air-phase concentration of pollutant at interface (µg m<sup>-3</sup>)
C_{i \text{ air}}
             water-phase concentration of pollutant at interface (\mu g \ m^{-3})
C<sub>i water</sub>
             mass concentration (g m<sup>-3</sup>)
C_{\rm m}
             odor concentration (ou m<sup>-3</sup>)
C_{
m odor}
             specific heat (J kg<sup>-1</sup> K<sup>-1</sup>)
             specific heat of air (J kg<sup>-1</sup> K<sup>-1</sup>)
C_{p, air}
             visual contrast (-)
             visual contrast at zero distance (–)
             droplet-phase pollutant concentration (µg m<sup>-3</sup>)
             water-phase pollutant concentration (µg m<sup>-3</sup>)
Cwater
C_{x}
             yz plane integrated plume concentration (g m<sup>-1</sup>)
cov()
             covariance (product of units of correlating functions)
d
             displacement height (m)
             day of the year (d)
d_{p}
             particle diameter (m)
\dot{D}
             molecular diffusivity (gas phase) (m<sup>2</sup> s<sup>-1</sup>)
D
             binary diffusion coefficient of compound i in compound j (m² s-1)
             molecular diffusivity (water phase) (m<sup>2</sup> s<sup>-1</sup>)
D_{\cdot \cdot}
             turbulent kinetic energy (m<sup>2</sup> s<sup>-2</sup>)
 \overline{e}
E
             activation energy (J mol-1)
             irradiance (W m-2 or W cm-2)
             photon energy (J photon<sup>-1</sup> or simply J)
e_{p}
```

```
E_{p}
             photon irradiance (photons cm<sup>-2</sup> s<sup>-1</sup> or simply cm<sup>-2</sup> s<sup>-1</sup>)
E_{\mathrm{p},\lambda}^{\mathrm{P}}
             spectral photon irradiance (photons cm<sup>-2</sup> s<sup>-1</sup> nm<sup>-1</sup> or simply cm<sup>-2</sup> s<sup>-1</sup> nm<sup>-1</sup>)
             spectral irradiance (W m<sup>-2</sup> nm<sup>-1</sup> or W cm<sup>-2</sup> nm<sup>-1</sup>)
E_{\lambda}
f
             Coriolis parameter (s<sup>-1</sup>)
F
             deposition flux (µg m<sup>-2</sup> s<sup>-1</sup>)
             broadening factor in falloff kinetics (-)
             reactivity factor (-)
f_0
F_{\rm b}
             buoyancy flux parameter (m<sup>4</sup> s<sup>-3</sup>)
             "complementary" (stochastic) force (N)
             falloff parameter (-)
F_{\rm d}
             pollutant flux at droplet surface (µg m<sup>-2</sup> s<sup>-1</sup>)
            drag force (N)
             momentum flux parameter (m<sup>4</sup> s<sup>-2</sup>)
            dispersion factor in the y direction (–)
f_{y}
            dispersion factor in the z direction (-)
Fr,
             Froude number for hill height (-)
Fr_w
             Froude number for hill width (-)
             acceleration of gravity (m s-2)
8
h
             Planck constant (J s)
            effective source height (m)
            hour angle (rad or °)
             vertical thickness scale (m)
            denser-than-air plume height (m)
H
            enthalpy (J)
            height of a hill (m)
            height of a building (m)
            dimensionless Henry constant (-)
h
            average plume height (m)
H_{c}
            height of the cavity (depends on location) (m)
H_{cn}
            Henry constant on a concentration/pressure basis (mol m<sup>-3</sup> Pa<sup>-1</sup>)
h_{d}
            dividing streamline height (m)
            horizontal flame extent (m)
h_{\rm fh}
             vertical flame height (m)
h_{\rm fv}
            mixing layer height (m)
H
            height of obstacles defining roughness (m)
H_{R}
            height of the cavity at its maximum (m)
h_{\zeta}
            source height (m)
h.
            altitude of terrain (m)
H_{w}
            height of the far wake (m)
h_*
             vertical height scale (m)
            actinic flux (photons cm<sup>-2</sup> s<sup>-1</sup> nm<sup>-1</sup> or simply cm<sup>-2</sup> s<sup>-1</sup> nm<sup>-1</sup>)
I
            ionic strength (mol kg-1)
            light intensity of background
i background
            intake fraction (-)
            light intensity of object
i_{
m object}
            turbulent intensity in the x direction (m)
            turbulent intensity in the y direction (m)
            turbulent intensity in the z direction (m)
            mass flux (moving frame of reference) (g m<sup>-2</sup> s<sup>-1</sup>)
```

```
photochemical rate constant of reaction i (s<sup>-1</sup>)
j_i
            von Kármán constant (-)
            Boltzmann constant (J molecule<sup>-1</sup> K<sup>-1</sup> or J K<sup>-1</sup>)
K
            equilibrium constant (-)
            apparent second-order rate constant in low-pressure limit (cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup>)
k_{0}
            air-phase mass transfer coefficient (m s<sup>-1</sup>)
k_{c}
            turbulent heat diffusivity (m<sup>2</sup> s<sup>-1</sup>)
K_{\rm h}
k_{\cdot}
            rate constant of reaction i [(s<sup>-1</sup> (first order); cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup> (second order)]
k_1
            water-phase mass transfer coefficient (m s<sup>-1</sup>)
K_{\rm m}
            turbulent momentum diffusivity (m<sup>2</sup> s<sup>-1</sup>)
K_{\zeta}
            solubility constant (-)
K
            turbulent mass diffusivity in the x direction (m^2 s^{-1})
K
            turbulent mass diffusivity in the y direction (m<sup>2</sup> s<sup>-1</sup>)
K,
            turbulent mass diffusivity in the z direction (m<sup>2</sup> s<sup>-1</sup>)
k_{\infty}
            rate constant at high pressure limit (cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup>)
L
            Obukhov length (m)
            length of a building, projected along the wind direction (m)
1
            path length (m or cm)
            flame length (m)
L_{\epsilon}
L
            integral length scale (m)
L_{\rm R}
            length of the cavity (m)
LAI
            leaf area index (-)
            mass (kg)
m
            mass of ambient air (kg)
m
            mass of water vapor (kg)
m
            molar mass (g mol-1 or kg mol-1)
M
M
            variance-covariance matrix of velocity fluctuation matrix (m<sup>2</sup> s<sup>-2</sup>)
            material balance matrix (s-1)
M
            molar mass of air (g mol-1 or kg mol-1)
M
            pollutant molar mass (kg mol-1)
            mass exchange rate constant between layers (s-1)
M_{..}
            amount of substance (i.e., number of moles) (mol)
n
            fractional cloud cover (-)
            integrated stochastic perturbation function (m s<sup>-1</sup>)
N
            mass flux (fixed frame of reference) (g m<sup>-2</sup> s<sup>-1</sup>)
N_{\Lambda}
            Avogadro constant (molecules mol<sup>-1</sup> or mol<sup>-1</sup>)
            Brunt-Väisälä frequency (s<sup>-1</sup>)
N_{i}
            flux of i in a fixed frame of reference (mol m^{-2} s<sup>-1</sup>)
            order of reaction i with respect to compound A (-)
n_{iA}
OU
            odor unit
            pressure (Pa = kg m^{-1} s<sup>-2</sup>)
p
            probability density function of location and velocity (s m<sup>-2</sup>)
P
            probability density function (inverse of units of the distributed variable)
            pressure at the surface (Pa)
p_0
            critical pressure (Pa)
p_{\rm c}
p^*
            nondimensionalized pressure (-)
PM_{2.5}
            mass concentration of particulate matter smaller than 2.5 µm diameter (µg m<sup>-3</sup>)
            heat (J = kg m^2 s^{-2})
9
            sensible heat flux (J m-2 s-1)
```

```
water/air mass ratio (-)
            pollutant mass fraction (-)
0
            emission rate (g s<sup>-1</sup>)
            anthropogenic heat flux (J m-2 s-1)
9,
Q
            heating value (kW)
            heat flux into the ground (J m<sup>-2</sup> s<sup>-1</sup>)
q_{\rm c}
            mass fraction of compound i(-)
4.
            latent heat flux (J m 2 s 1)
4,
Q_{\mathrm{md}i}
            downward mass flux between two layers (kg m 2 s 1)
            exchanged mass flux between two layers (kg m<sup>-3</sup> s<sup>-1</sup>)
Q_{mui}
             upward mass flux between two layers (kg m<sup>-2</sup> s<sup>-1</sup>)
 Q
             sensible heat emission (kW)
 r
              albedo (-)
              aerodynamic resistance (s m<sup>-1</sup>)
              surface canopy resistance (s m-1)
 r_{\rm b}
             quasi-laminar resistance (s m<sup>-1</sup>)
              surface resistance (s m<sup>-1</sup>)
              foliar resistance (s m<sup>-1</sup>)
             ground resistance (s m<sup>-1</sup>)
 r_{\rm cl}
             resistance of leaves, twigs, bark, ... (s m<sup>-1</sup>)
             cuticle resistance (s m<sup>-1</sup>)
             dry cuticle resistance (s m<sup>-1</sup>)
r_{\rm cut.d}
r cut.w
             wet cuticle resistance (s m-1)
r_{\rm cw}
             water resistance (s m<sup>-1</sup>)
r_{\rm dc}
             canopy resistance
             correlation coefficient between f and g(-)
r_{fe}
             dry ground resistance (s m<sup>-1</sup>)
r_{\rm gd}
             wet ground resistance (s m-1)
F_{\rm gw}
             ground resistance below surface canopy (s m-1)
             resistance parameter (s m<sup>-1</sup>)
\Gamma
             cuticle resistance parameter (s m<sup>-1</sup>)
F_{\text{lo}}
             mesophyll resistance (s m-1)
r_{\rm m}
             stomatal resistance (s m<sup>-1</sup>)
 R
             ideal gas constant (J mol-1 K-1)
             solar radiation energy flux (J m<sup>-2</sup> s<sup>-1</sup>)
             spread parameter in bi-Gaussian convective cycling model (-)
             building length scale (m)
             precipitation rate (mm h<sup>-1</sup>)
             atmospheric resistance (s m<sup>-1</sup>)
             reflection probability (-)
 R_{\Lambda}
             reaction rate of compound A (molecules cm<sup>-3</sup> s<sup>-1</sup>)
 R.
             reaction rate of reaction i (molecules cm^{-3} s^{-1})
 R_{i}
             Lagrangian autocorrelation coefficient (-)
 R_N
             net radiation energy flux (J m<sup>-2</sup> s<sup>-1</sup>)
             stack radius (m)
 r_{\varsigma}
             total resistance to deposition (s m<sup>-1</sup>)
 R_{...}
             autocorrelation coefficient (-)
 R'_{n}
             autocorrelation function (m<sup>2</sup> s<sup>-2</sup>)
 Re
             Reynolds number (=du\rho/\mu = du/\nu) (-)
```

```
Reynolds number based on friction velocity (=z_0u_*\rho/\mu = z_0u_*/\nu) (–)
Re*
RH
            relative humidity (%)
            stability parameter (s<sup>-2</sup>)
S
            distance traveled by plume center (m)
S
            skewness of vertical wind speed distribution (m<sup>3</sup> s<sup>-3</sup>)
So
            standard entropy (J mol<sup>-1</sup> K<sup>-1</sup>)
S
            spacing of obstacles defining roughness (m)
S'_{uu}
            spectrum function of wind speed variance (m<sup>2</sup> s<sup>-1</sup> if function of v)
S_{uu}
            normalized spectrum function of wind speed variance (s if function of v or \omega; m if
            function of \kappa)
S
            saturation (-)
Sc
            Schmidt number (=v/D)
t
            time (s or h)
            time of the solar noon (h)
t_0
            half life (s)
t_{1/2}
T
            temperature (K)
T_a
            apparent time (s)
            ambient temperature (K)
T_{i}
            critical temperature (K)
            integral time scale (s)
            Lagrangian integral time scale (s)
            stack gas temperature (K)
            surface air temperature (K)
T_{\cdot \cdot}
            virtual temperature (K)
            wind speed in the x direction (m s^{-1})
11
U
            wind speed in the X direction, Lagrangian frame of reference (m s<sup>-1</sup>)
            internal energy (J)
\overline{u}
            average wind speed (m s-1)
u'
            wind speed fluctuation (m s<sup>-1</sup>)
            wind speed variable in nocturnal atmosphere stability calculations (m s<sup>-1</sup>)
u_0
            wind speed in the x_1 (i.e., x) direction (m s<sup>-1</sup>)
и,
            wind speed in the x_2 (i.e., y) direction (m s<sup>-1</sup>)
u_{\gamma}
            wind speed in the x_3 (i.e., z) direction (m s<sup>-1</sup>)
u_{3}
            ambient wind speed (m s-1)
U
U_{\mathrm{atm}}
            wind speed (m s<sup>-1</sup>)
            characteristic velocity (m s<sup>-1</sup>)
u,
             wind speed in a cavity (m s-1)
 U_{c}
             wind speed at height H_{\rm s} (m s<sup>-1</sup>)
 \mathcal{U}_{H}
 U_{sc}
             velocity of plume centerline (m s<sup>-1</sup>)
U_{\rm w}
             wind speed in a far wake (m s<sup>-1</sup>)
             friction velocity (m s-1)
 u_*
             water-side friction velocity (m s<sup>-1</sup>)
 u_*
             local friction velocity (between obstacles) (m s<sup>-1</sup>)
 \mathcal{U}_{\tau}
             wind speed in the y direction (m s<sup>-1</sup>)
 \nu
 V
             wind speed in the Y direction, Lagrangian frame of reference (m s<sup>-1</sup>)
 V
             velocity fluctuation matrix (m s<sup>-1</sup>)
 \bar{V}
             total wind speed (m s-1)
             deposition velocity (m s-1)
             settling velocity (m s<sup>-1</sup>)
```

V

### XXIV LIST OF SYMBOLS

```
ν.
            transfer velocity (m s<sup>-1</sup>)
            wind speed in the z direction (m s<sup>-1</sup>)
  W
  W
            wind speed in the Z direction, Lagrangian frame of reference (m s<sup>-1</sup>)
            width of a hill (m)
            width of a building, projected across the wind flow (m)
            Wiener process
  W_*
            convective velocity (m s<sup>-1</sup>)
            average vertical wind speed of updrafts (m s-1)
  W,
            average vertical wind speed of downdrafts (m s-1)
  Wa
            emission velocity at the surface (m s-1)
 W_{b}
 W
            half-width of the cavity (m)
            wet fraction of the cuticle (-)
 W
           entrainment velocity (m s-1)
 W
           wet fraction of the ground (-)
 W
           stack gas velocity in the vertical direction (m s<sup>-1</sup>)
 W_{\rm st}
           wet fraction of the stomata (-)
           water weight fraction of air (-)
 W
 W_{\rm w}
           width of the far wake (m)
 w'w
           water-air weight ratio (-)
           downwind distance from the source (m)
X
           coordinate in the west-east direction (Eulerian models) (m)
           distance from the upwind side of a building (m)
X
          downwind distance coordinate, Lagrangian frame of reference (m)
           coordinate in the west-east direction (Eulerian models) (m)
X_1
          coordinate in the south-north direction (m)
X_{\gamma}
          vertical distance (m)
X_{3}
          downwind distance to the source of final plume rise (m)
X_{\rm f}
          distance to virtual source (m)
X_{v}
X_{\rm vis}
          visibility (m)
          crosswind distance from the plume axis (m)
          coordinate in the south-north direction (m)
Y
          crosswind distance coordinate, Lagrangian frame of reference (m)
          mole fraction of i in the gas phase (-)
y.
          vertical distance from the surface (terrain following coordiates) (m)
          vertical distance from the surface at the source (Cartesian coordinates) (m)
Z
          vertical distance coordinate, Lagrangian frame of reference (m)
          vertical distance coordinate, terrain following coordinates (m)
          roughness length (m)
Z_0
          junction height (m)
```

### Greek letters

```
\begin{array}{ll} \alpha & & \text{along-plume entrainment rate parameter (-)} \\ & & \text{quasi-laminar layer thickness parameter (-)} \\ & & \text{mass transfer enhancement factor (-)} \\ & \alpha_a & & \text{absorption coefficient } (m^{-1}) \\ & \alpha_c & & \text{sea roughness parameter (-)} \\ & \alpha_{out} & & \text{extinction coefficient } (m^{-1}) \end{array}
```

```
\alpha_{\nu}
            Kolmogorov constant (–)
 \alpha
            scattering coefficient (m-1)
 \alpha_{\rm sair}
            scattering coefficient for air molecules (m-1)
            scattering coefficient for PM (m-1)
 \boldsymbol{\alpha}_{s,PM}
            ratio of Lagrangian to Eulerian integral time scales (-)
            across-plume entrainment rate parameter (-)
            parameter describing height dependence of density in denser-than-air plumes (-)
            vertical slope of potential temperature above the planetary boundary layer (K m-1)
 Y
            wavelength (m)
            activity coefficient
 Γ
            dry adiabatic lapse rate (K m-1)
 Γ
            moist adiabatic lapse rate (K m<sup>-1</sup>)
 δ
            solar declination (rad or °)
 \Delta H^{\circ}
            standard enthalpy of formation (kJ mol-1)
 \Delta h
            plume rise (final) (m)
 \Delta h_{\rm sd}
            stack downwash (m)
 \Delta G^{\circ}
            standard Gibbs free energy of reaction (kJ mol<sup>-1</sup>)
 \Delta H^{\circ}
            standard enthalpy of reaction (kJ mol-1)
\Delta S^{\circ}
            standard entropy of reaction (J mol-1 K-1)
\Delta U
            velocity deficit (m s-1)
\Delta_{\rm van}H
            enthalpy of vaporization (J kg-1)
\Delta z
            plume rise (transitional) (m)
\Delta\theta
            temperature jump at capping inversion (K)
3
            height of obstacles defining surface roughness (m)
            energy dissipation rate (m<sup>2</sup> s<sup>-3</sup>)
            emissivity (-)
            molar decadic absorption coefficient (cm<sup>2</sup> molecule<sup>-1</sup> or simply cm<sup>-2</sup>)
5
            dimensionless height variable in Monin-Obukhov theory (-)
η
            Kolmogorov length microscale (m)
\theta
           potential temperature (K)
           dimensionless temperature variable (-)
           terrain slope (rad)
\theta_{c}
           temperature (°C)
\theta_{\rm c}
           temperature (°F)
\theta_{m}
           vertical average potential temperature in mixing layer (K)
\theta
           virtual potential temperature (K)
\theta_*
           friction temperature (K)
K
           thermal diffusivity (m<sup>2</sup> s<sup>-1</sup>)
           wave number (rad m<sup>-1</sup> or simply m<sup>-1</sup>)
λ
           height scale for Coriolis effects (m)
           thermal conductivity (J m<sup>-1</sup> K<sup>-1</sup>)
           latitude (rad or °)
           molecule mean free path (m)
           scavenging coefficient (s<sup>-1</sup>)
           wavelength (m or nm)
λ,
           area fraction of updraft (-)
           area fraction of downdraft (-)
\lambda_{r}
           frontal area parameter (-)
           spatial Taylor microscale (m)
```

### XXVI LIST OF SYMBOLS

```
A_{\rm L}
            Lagrangian integral length scale (m)
            plan area parameter (-)
Λ
            temperature lapse rate (K m<sup>-1</sup>)
            scavenging ratio (s<sup>-1</sup>)
            dynamic viscosity (Pa s)
μ
ν
            kinematic viscosity (m<sup>2</sup> s<sup>-1</sup>)
            frequency (s-1)
P
            density (kg m<sup>-3</sup>)
\rho_{a}
            ambient air density (kg m<sup>-3</sup>)
            particle density (kg m<sup>-3</sup>)
\rho_{\rm p}
            stack gas density (kg m<sup>-3</sup>)
P
            Stefan-Boltzmann constant (s<sup>-1</sup> m<sup>-2</sup> K<sup>-4</sup>)
            absorption cross-section (cm<sup>2</sup> molecule<sup>-1</sup> or simply cm<sup>2</sup>)
            standard deviation of perturbation function (m s<sup>-1</sup>)
\sigma_{n}
            turbulent velocity in the x direction (m s^{-1})
\sigma_{..}
            turbulent velocity in the y direction (m s<sup>-1</sup>)
\sigma
            turbulent velocity in the z direction (m s<sup>-1</sup>)
\sigma
            turbulent velocity in the z direction of updraft (m s^{-1})
\sigma_{\rm wl}
            turbulent velocity in the z direction of downdraft (m s^{-1})
\sigma_{w2}
            dispersion parameter along the horizontal wind direction (m)
\sigma
            dispersion parameter across the horizontal wind direction (m)
\sigma
            dispersion parameter in the vertical direction (m)
\sigma
            shear stress (Pa)
τ
            time constant (s)
            shear stress at the surface (Pa)
\tau_{0}
            Taylor microscale (s)
τ
            solar elevation (rad)
\varphi
            latitude (rad)
φ
            angle between plume path and the horizontal (rad)
            quantum yield (-)
            Monin-Obukhov similarity function for heat transfer (-)
\phi_{\rm h}
            Monin-Obukhov similarity function for momentum transfer (-)
            dilution factor due to lateral dispersion (m<sup>-1</sup>)
\varphi_{v}
            dilution factor due to vertical dispersion (m<sup>-1</sup>)
\varphi_{z}
            angular frequency (rad s<sup>-1</sup> or simply s<sup>-1</sup>)
\omega
Ω
            angular velocity of Earth (s<sup>-1</sup>)
```

# **CONTENTS**

| Prefa | Preface                   |  | xv  |
|-------|---------------------------|--|-----|
| List  | of Sym                    | bols   | xix |
| CHA   | PTER 1                    | INTRODUCTION   | 1   |
| 1.1   | Introd                    | uction   | 1   |
| 1.2   | Types                     | of Air Dispersion Models                                     | 4   |
|       | 1.2.1                     | Gaussian Plume Models  | 4   |
|       | 1.2.2                     | Gaussian Puff Models   | 5   |
|       | 1.2.3                     | Stochastic Lagrangian Particle Models                        | 5   |
|       | 1.2.4                     | Eulerian Advection and Dispersion Models                     | 5   |
|       | 1.2.5                     | Computational Fluid Dynamics                                 | 6   |
| 1.3   | Standa                    | ard Conditions for Temperature and Pressure                  | 6   |
| 1.4   | Conce                     | ntration Units in the Gas Phase                              | 7   |
| 1.5   | Units                     |  | 9   |
| 1.6   | Consta                    | ants and Approximately Constant Variables                    | 11  |
| 1.7   | Freque                    | ently Used Greek Symbols                                     | 12  |
|       | Proble                    | ms   | 12  |
|       | Refere                    | ences  | 12  |
| СНА   | PTER 2                    | AN AIR DISPERSION MODELING PRIMER                            | 14  |
| 2.1   | Introd                    | uction   | 14  |
| 2.2   | Basic                     | Concepts of Air Dispersion                                   | 15  |
| 2.3   | Gaussian Dispersion Model |  | 17  |
|       | 2.3.1                     | Assumptions Underlying the Gaussian Plume Concept            | 17  |
|       | 2.3.2                     | Quantitative Description                                     | 18  |
|       | 2.3.3                     | Refinements  | 26  |
| 2.4   | Plume Rise                |  | 30  |
|       | 2.4.1                     | Plume Rise Correlations                                      | 30  |
|       | 2.4.2                     | Critical Wind Speed  | 32  |
|       | 2.4.3                     | Rules of Thumb   | 33  |
| 2.5   | Need                      | for Refinements to the Basic Gaussian Plume Dispersion Model | 34  |
|       | Proble                    | ems  | 34  |
|       | Mater                     | ials Online  | 36  |
|       | Refere                    | ences  | 36  |
| СНА   | PTER 3                    | AIR POLLUTANTS: AN OVERVIEW                                  | 37  |
| 3.1   | Introd                    | uction   | 3   |
| 3.2   | Types                     | of Air Pollution   | 3   |
|       |                           | Sulfur Compounds   | 38  |
|       | 3.2.2                     | Nitrogen Compounds   | 39  |
|       | 3.2.3                     |  | 40  |
|       | 3.2.4                     | Inorganic Carbon   | 4   |
|       | 3.2.5                     | Ozone  | 4:  |
|       |                           |  |     |

### viii contents

|      | 3.2.6                 | Particulate Matter                                 | 44  |
|------|-----------------------|--|-----|
|      | 3.2.7                 | Metals   | 45  |
|      | 3.2.8                 | Air Pollution and Health                           | 45  |
|      | 3.2.9                 | Global Warming                                     | 46  |
|      | 3.2.10                | Air Pollution and Visibility                       | 49  |
|      | 3.2.11                | Odor Nuisance                                      | 50  |
|      | Proble                | ms   | 51  |
|      | Refere                | nces   | 52  |
| CHAP | PTER 4                | REGULATION OF AIR QUALITY AND AIR QUALITY MODELING | 54  |
| 4.1  | Introdu               |  | 54  |
| 4.2  | Air Qu                | ality Regulation                                   | 54  |
| 4.3  | Air Di                | spersion Modeling Guidelines                       | 59  |
|      | Refere                | nces   | 59  |
| CHAP | PTER 5                | METEOROLOGY FOR AIR DISPERSION MODELERS            | 60  |
| 5.1  | Introdu               |  | 60  |
| 5.2  |                       | are of the Atmosphere                              | 61  |
| 5.3  |                       | le Dependence of Barometric Pressure               | 62  |
| 5.4  |                       | Dependence of Temperature—Adiabatic Case           | 65  |
|      |                       | Adiabatic Lapse Rate                               | 65  |
|      | 5.4.2                 | Potential Temperature                              | 68  |
| 5.5  | Stabili               | *  | 70  |
|      | 5.5.1                 | General Description of Stability                   | 70  |
|      | 5.5.2                 | 2  | 72  |
|      | 5.5.3                 | Diurnal Cycle of Stability                         | 75  |
| 5.6  | Heat Balance          |  | 76  |
| 5.7  |                       | Speed Profile                                      | 81  |
|      | 5.7.1                 |  | 81  |
|      |                       | Case 2: Rough Surface, Adiabatic Conditions        | 83  |
|      | 5.7.3                 | Case 3: Rough Surface, Nonneutral Conditions       | 86  |
| 5.8  |                       | rature Profile Revisited: Nonneutral Conditions    | 93  |
| 5.9  |                       | alance Revisited: Stable Conditions                | 97  |
| 5.10 |                       | g Layer Height                                     | 99  |
| 5.11 | Concept of Turbulence |  | 103 |
|      | 5.11.1                | Basic Properties of Turbulence                     | 103 |
|      | 5.11.2                | Measures of Turbulence                             | 105 |
|      | 5.11.3                | Similarity Theory and Turbulence                   | 107 |
|      | 5.11.4                | Covariance and Turbulence                          | 110 |
|      | 5.11.5                | 5  | 113 |
| 5.12 |                       | l Topics in Meteorology                            | 119 |
|      | 5.12.1                | Convective Cycles: Qualitative Description         | 119 |
|      | 5.12.2                | Internal Boundary Layer: Qualitative Description   | 120 |
|      | 5.12.3                | Plume Shapes                                       | 121 |
|      | 5.12.4                | Virtual Temperature                                | 122 |
| 5.13 | 5                     |  | 122 |
|      | 5.13.1                | Convective Cycles: Quantitative Description        | 123 |
|      | 5.13.2                | Simple Convective Boundary Layer Model             | 126 |
|      | 5.13.3                | Internal Boundary Layer: Quantitative Description  | 129 |
|      | 5.13.4                | Effect of Complex Terrain in Meteorology           | 130 |

| CONTENTS | ix |
|----------|----|
|----------|----|

| 5.14 |                                     | nary of Main Equations   | 134 |
|------|-------------------------------------|--|-----|
|      | Proble                              |  | 137 |
|      |                                     | ials Online  | 138 |
|      | Refere                              | ences  | 139 |
| СНАР | TER 6                               | GAUSSIAN DISPERSION MODELING: AN IN-DEPTH STUDY                  | 141 |
| 6.1  |                                     | uction   | 141 |
| 6.2  |                                     | ian Plume Models   | 142 |
| 6.3  |                                     | neterizations Based on Stability Classes                         | 145 |
| 6.4  | Gaussian Plume Dispersion Short Cut |  |     |
| 6.5  | Plume Dispersion Modifiers          |  | 150 |
| 6.6  |                                     | nuous Parameterization for Gaussian Dispersion Models            | 153 |
|      | 6.6.1                               | Introduction: From Turbulence to Dispersion                      | 153 |
|      |                                     | Autocorrelation of Wind Speed                                    | 154 |
|      |                                     | Taylor's Hypothesis  | 155 |
|      |                                     | Lagrangian Frame of Reference                                    | 156 |
|      |                                     | Practical Schemes for Continuous Parameterizations               | 159 |
|      | 6.6.6                               | Dispersion Parameters Based on the Autocorrelation Function      | 164 |
|      | 6.6.7                               | More $T_{i,L}$ Relationships                                     | 168 |
| 6.7  | Gauss                               | ian Plume Models for Nonpoint Sources                            | 172 |
| 6.8  | Virtua                              | l Source Concept   | 174 |
| 6.9  | Specia                              | al Issues  | 175 |
|      | 6.9.1                               | Probability Density Functions for Plumes in Convective           |     |
|      |                                     | Boundary Layers  | 175 |
|      | 6.9.2                               | Emission from a Ground-Level Source                              | 176 |
| 6.10 | Gaussian Puff Modeling              |  | 180 |
|      | 6.10.1                              | Introduction   | 180 |
|      | 6.10.2                              | Puff Models  | 181 |
|      | 6.10.3                              | Stochastic Puff Models: Parameterization for Instantaneous Puffs | 185 |
| 6.11 | Advanced Topics in Meteorology      |  | 187 |
|      | 6.11.1                              | Spectral Properties of Turbulence                                | 187 |
|      | 6.11.2                              | Turbulent Energy Dissipation: Kolmogorov Theory                  | 188 |
| 6.12 | Sumn                                | nary of the Main Equations                                       | 193 |
|      | Proble                              | ems  | 195 |
|      | Mater                               | ials Online  | 197 |
|      | Refer                               | ences  | 197 |
| CHAP | TER 7                               | PLUME-ATMOSPHERE INTERACTIONS                                    | 201 |
| 7.1  | Introd                              | uction   | 201 |
| 7.2  | Plume                               | e Rise   | 201 |
|      | 7.2.1                               | Introduction   | 201 |
|      | 7.2.2                               | Plume Rise Theory  | 202 |
|      | 7.2.3                               | Flare Plume Rise   | 208 |
|      | 7.2.4                               | Numerical Plume Rise Calculations                                | 210 |
| 7.3  | Plume                               | e Downwash: PRIME (Plume RIse Model Enhancements)                | 215 |
|      | 7.3.1                               | Introduction   | 215 |
|      | 7.3.2                               | Wake Size Calculations   | 216 |
|      | 7.3.3                               | Streamline Deflection Calculation                                | 219 |
|      |                                     | Plume–Wake Interaction Calculation                               | 221 |
| 7.4  |                                     | vior of Denser-than-Air Plumes                                   | 225 |

### X CONTENTS

| 7.5        | Depos  | sition   | 234        |
|------------|--|--|------------|
|            | 7.5.1  | Dry Deposition   | 234        |
|            |  | Wet Deposition   | 265        |
|            |  | Gaussian Dispersion Models with Deposition   | 277        |
| 7.6        |  | nary of the Main Equations   | 288        |
|            | Proble   |  | 291        |
|            |  | ials Online  | 292        |
|            | Refere   | ences  | 292        |
| СНА        | PTER 8   | GAUSSIAN MODEL APPROACHES IN URBAN   |            |
| OR         | INDUS  | TRIAL TERRAIN  | 296        |
| 8.1        | Introd   | uction   | 296        |
| 8.2        |  | Flow around Obstacles  | 297        |
| 8.3        | Surfac   | ee Roughness and Displacement Height in Urban and Industrial Terrain   | 298        |
|            | 8.3.1  | Introduction   | 298        |
|            | 8.3.2  | Determination of $z_0$ and $d$   | 300        |
| 8.4        |  | Speed Profiles near the Surface: Deviations from Similarity Theory   | 303        |
|            |  | Theoretical Background   | 303        |
|            |  | Simple Approach  | 305        |
|            |  | Exponential Wind Speed Profile   | 305        |
|            | 8.4.4  | Junction Methods   | 307        |
| 0.5        | 8.4.5  | Other Canopy Wind Speed Descriptions   | 309        |
| 8.5        |  | lence in Urban Terrain   | 314        |
| 8.6        | Dispersion Calculations in Urban Terrain near the Surface                              |  | 317        |
|            | 8.6.1  | Introduction   | 317        |
|            | 8.6.2  | Gaussian Model Formulation near the Surface  | 317        |
| 07         | 8.6.3  | Near Surface Dispersion Parameter Calculation Schemes  | 318        |
| 8.7<br>8.8 | An Ex  |  | 320        |
| 0.0        | Proble   | nary of the Main Equations   | 324        |
|            |  | ials Online  | 326        |
|            | Refere   |  | 327        |
|            | Refere   | ences  | 327        |
|            | PTER 9   | STOCHASTIC MODELING APPROACHES   | 329        |
| 9.1        | Introd   |  | 329        |
| 9.2        |  | mentals of Stochastic Air Dispersion Modeling  | 330        |
|            | 9.2.1  | Introduction: Properties of the Langevin Equation  | 330        |
|            | 9.2.2  | Modifying the Langevin Equation for Air Dispersion Modeling:   |            |
|            | 0.2.2  | Homogeneous Atmosphere   | 333        |
|            | 9.2.3  | Langevin Equation in Heterogeneous Atmosphere  | 338        |
|            | 9.2.4  | Turbulence Data for Stochastic Lagrangian Models  Stochastic Lagrangian Particle Medicine of the Communities | 343        |
|            | 9.2.5  | Stochastic Lagrangian Particle Modeling of the Convective<br>Boundary Layer                                  | 346        |
| 9.3        | Nume   | •  | 348        |
| 9.4        | Numerical Aspects of Stochastic Modeling<br>Stochastic Lagrangian Calculation Examples |  | 353        |
| 9.5        |  | ary of the Main Equations  | 358        |
| 9.3        | Problems   |  |            |
|            | Materials Online   |  | 359<br>360 |
|            | References   |  | 360        |
|            |  |  |            |

| CHAP         | TER 10 COMPUTATIONAL FLUID DYNAMICS   |            |
|--------------|---|------------|
| AND          | METEOROLOGICAL MODELING   | 363        |
| 10.1         | Introduction  | 363        |
| 10.2         | CFD Model Formulation: Fundamentals   | 364        |
|              | 10.2.1 The Navier–Stokes Equation   | 364        |
|              | 10.2.2 The Material and Energy Balance  | 371        |
| 10.3         | Reynolds-Averaged Navier-Stokes (RANS) Techniques   | 375        |
|              | 10.3.1 Averaging the Navier–Stokes Equations  | 375        |
|              | 10.3.2 Closing the Navier–Stokes Equations  | 379        |
|              | 10.3.3 Reynolds-Averaged Material and Energy Balances   | 392        |
| 10.4         | Large Eddy Simulation (LES)   | 394        |
|              | 10.4.1 Introduction   | 394        |
|              | 10.4.2 Turbulence Modeling in LES   | 394        |
| 10.5         | Numerical Methods in CFD  | 397        |
| 10.6         | Meteorological Modeling   | 399        |
| 10.7         | Summary of the Main Equations   | 400        |
|              | References  | 402        |
|              |   |            |
| СНАР         | TER 11 EULERIAN MODEL APPROACHES  | 404        |
| 11.1         | Introduction  |            |
| 11.1         |   | 404<br>405 |
| 11.2         | Governing Equations of Eulerian Dispersion Models Closing the Material Balance for Turbulent Motion | 403        |
| 11.5         | 11.3.1 Local Closure  | 412        |
|              | 11.3.2 Nonlocal Closure   | 412        |
| 11.4         |   | 413        |
| 11.4         | Atmospheric Chemistry 11.4.1 Introduction   | 422        |
|              | 11.4.2 Introduction to Chemical Kinetics  | 422        |
|              | 11.4.2 Introduction to Chemical Kinetics  |            |
|              |   | 428        |
|              | 11.4.4 Gas-Phase Reactions in Tropospheric Chemistry  | 431        |
| 115          | 11.4.5 Chemistry of Aerosol Formation in the Troposphere  | 440        |
| 11.5         | Numerical Aspects of Eulerian Dispersion Modeling   | 455        |
|              | 11.5.1 Advection  | 456        |
|              | 11.5.2 Diffusion/Dispersion   | 461        |
|              | 11.5.3 Chemical Reaction Kinetics   | 463        |
|              | 11.5.4 Boundary Conditions  | 466        |
| 11.6         | 11.5.5 Plume-in-Grid Modeling   | 467        |
| 11.6         | Summary of the Main Equations   | 467        |
|              | Problems  | 469        |
|              | References  | 470        |
| CHAD         | PTER 12 PRACTICAL ASPECTS OF AIR DISPERSION MODELING  | 474        |
|              | Introduction  | 1000       |
| 12.1         |   | 474        |
| 12.2         | Source Characterization and Source Modeling   | 474        |
|              | Coordinate Systems  | 476        |
| 12.4<br>12.5 | Data Handling<br>Model Validation   | 478        |
| 12.3         |   | 478        |
|              | References  | 479        |