

B. I. Bleaney and B. Bleaney

Electricity and Magnetism

Volume 1

B. I. BLEANEY

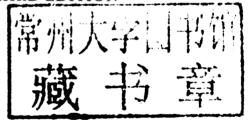
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Note on the Oxford Classic Text edition

For many years, Bleaney and Bleaney (B&B) provided an excellent foundation text in the teaching of electricity, magnetism, introductory electronics, and condensed-matter physics. In preparation for the current reissuing, I have reread the entire book from cover to cover and found nothing to change this opinion; B&B remains the most complete book of its kind. And the erudition of its authors remains very obvious; analogies with, and connections to, chemistry, engineering, molecular spectroscopy, atomic physics, geology, telecommunications, and so on are sprinkled throughout the book.

B&B is in many ways a classic, and in preparing the current edition, the intention has been to change as little as possible; anything else would have been akin to sprinkling words like 'dude' and 'dissed' through *Pride and Prejudice*. However, the present reissuing did afford the opportunity to correct a small number of misprints and to offer clarifications in a few places that students have found confusing or difficult to follow. Archaic words such as 'condenser' have (perhaps regrettably) been relegated to the index and replaced in the text by their more modern equivalents.

The earlier editions of B&B were remarkably contemporary books. Many 'cutting-edge' topics, such as the BCS theory of superconductivity, were introduced shortly after their discovery. Though such chapters still (in late 2011) constitute good introductory summaries of these subjects, the only references provided by B&B tended to be lists of early research papers. This is entirely understandable; at the time of writing, there were no textbooks on these topics! In such cases, I have introduced a few references to books that give a more recent overview of the subject. The only part of the book that has dated in a really obvious fashion is the chapter on 'Alternating current measurements'. Here, many of the techniques described have been rendered obsolete by modern digital instruments. This has been pointed out in a footnote, with the rest of the chapter left unaltered for historical interest.

The most persistent comments on the earlier editions of B&B mainly concern the index. In an age of instant informational gratification through the likes of Wikipedia and Google, the rather spare indexing of earlier editions seems to have become somewhat offputting. In response to these requests, the index has been expanded, and the complete index (to Volumes 1 and 2) is given in both volumes.

vi Note on the Oxford Classic Text edition

In making the above changes, I have been aided greatly by my former colleague Geoff Brooker. On most points we agreed. In the more obscure alterations it was good to have Geoff's support and extensive background knowledge. Guy Peskett and David Andrews have also made very useful suggestions, and numerous others have passed on comments from students, misprints etc.. I am very grateful for all of this assistance. Nevertheless, remaining mistakes and inaccuracies are my responsibility, and, in the hope of further reprints, I would be glad to be informed of them (j.singleton1 @physics.ox.ac.uk).

John Singleton November 2011 National High Magnetic Field Laboratory Los Alamos

Preface to the third edition

De manera que acordé, aunque contra mi voluntad, meter segunda vez la pluma en tan estraña lavor é tan agena de mi facultad, hurtando algunos ratos á mi principal estudio, con otras horas destinadas para recreacion, puesto que no han de faltar nuevos detractores á la nueva edicion.

1499

Fernando de Rojas

So I agreed, albeit unwillingly (since there cannot fail to be fresh critics of a new edition), again to exercise my pen in so strange a labour, and one so foreign to my ability, stealing some moments from my principal study, together with other hours destined for recreation.

For the third edition of this textbook the material has been completely revised and in many parts substantially rewritten. S.I. units are used throughout; references to c.g.s. units have been almost wholly eliminated, but a short conversion table is given in Appendix D. The dominance of solid-state devices in the practical world of electronics is reflected in a major change in the subject order.

Chapters 1–9 set out the macroscopic theory of electricity and magnetism, with only minor references to the atomic background, which is discussed in Chapters 10–17. A simple treatment of lattice vibrations is introduced in Chapter 10 in considering the dielectric properties of ionic solids. The discussion of conduction electrons and metals has been expanded into two chapters, and superconductivity, a topic previously excluded, is the subject of Chapter 13. Minor changes have been made in the three chapters (14–16) on magnetism. The discussion of semiconductor theory precedes new chapters on solid-state devices, but we have endeavoured to present such devices in a manner which does not presuppose a knowledge in depth of the theory. The remaining chapters, on amplifiers and oscillators, vacuum tubes, a.c. measurements, noise, and magnetic resonance, bring together the discussion of electronics and its applications.

The authors are grateful to many colleagues in Oxford and readers elsewhere for helpful comments on previous editions which have been incorporated in the present volume. In particular we are indebted to Dr. G. A. Brooker for numerous and detailed comments and suggestions; to Drs F. V. Price and J. W. Hodby, whose reading of new material on electronics in draft form resulted in substantial improvement of the presentation; to Drs F. N. H. Robinson and R. A. Stradling for several helpful suggestions; and to Messrs

viii

C. A. Carpenter and J. Ward for the considerable trouble taken in producing Fig. 23.3. We are indebted to Professors M. Tinkham and O. V. Lounasmaa for generously sending us material in advance of publication; and to Professor L. F. Bates, F.R.S., Drs R. Dupree, and R. A. Stradling for their kindness in providing the basic diagrams for Figs 15.6, 6.15, and 17.9. We wish to thank Miss C. H. Bleaney for suggesting the quotation which appears above.

Clarendon Laboratory, Oxford February 1975 B. I. B.

B. B.

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Note added in 1989

The opportunity has been taken of dividing this textbook into two volumes.

Volume 1: Chapters 1 to 9 inclusive, covering the basic theory of electricity and magnetism.

Volume 2: Chapters 10 to 24 inclusive, covering electrical and magnetic properties of matter, including semiconductors and their applications in electronics, alternating current measurements, fluctuations and noise, magnetic resonance.

A number of minor errors have been corrected, and a section (20.8) has been added on Operational Amplifiers. We wish to thank Dr. F. N. H. Robinson for suggesting this, and Dr. J. F. Gregg, I. D. Morris, and J. C. Ward for help in its preparation. We are indebted to Dr. L. V. Morrison of the Royal Greenwich Observatory, Cambridge (Stellar Reference Frame Group), for the up-to-date plot of the variations in the length of the day, measured by the caesium clock, that now appears as Fig. 24.12. It is based on data published by the Bureau de l'Heure, Paris.

B. I. B. B. B.

xii Contents

CONTENTS OF VOLUME 2

- 10. DIELECTRICS
- 11. FREE ELECTRONS IN METALS
- 12. THE BAND THEORY OF METALS
- 13. SUPERCONDUCTIVITY
- 14. PARAMAGNETISM
- 15. FERROMAGNETISM
- 16. ANTIFERROMAGNETISM AND FERRIMAGNETISM
- 17. SEMICONDUCTORS
- 18. SOLID-STATE DIODES
- 19. SOLID-STATE TRIODES
- 20. AMPLIFIERS AND OSCILLATORS
- 21. THERMIONIC VACUUM TUBES
- 22. ALTERNATING CURRENT MEASUREMENTS
- 23. FLUCTUATIONS AND NOISE
- 24. MAGNETIC RESONANCE

APPENDIX: NUMERICAL VALUES OF THE FUNDAMENTAL CONSTANTS

APPENDIX: SOME USEFUL UNIT CONVERSIONS

INDEX

Volume 1

Contents

1.	. ELECTROSTATICS I				
	1.1.	The electrical nature of matter	1		
	1.2.	Coulomb's law and fundamental definitions	2		
		Gauss's theorem	6		
	1.4.	Electric dipoles The theory of isotropic dielectrics	11		
	1.5.	The theory of isotropic dielectrics	14		
	1.6.	Capacitors and systems of conductors	20		
	1.7.	Stress in the electrostatic field	26		
		ences	29		
	Prob	lems	29		
2.	ELECTROSTATICS II				
4.			32		
	2.2.	The equations of Poisson and Laplace Solutions of Laplace's equation in spherical coordinates	34		
	2.3.	The multipole expansion	38		
	2.4.	Some electrostatic problems	43		
	2.5.	Some electrostatic problems Electrical images	48		
	2.6.	Line charges	51		
	2.7.	Images in dielectrics	55		
		ences	56		
	Prob		56		
2	CUD	RENT AND VOLTAGE			
٥.		Introduction	60		
		Flow of current in conductors	60 62		
	3.2.	The voltaic circuit	67		
	3.3	The voltaic circuit Resistance networks	70		
	3.4.	The potential divider and resistance bridge	73		
	3.5.	Electron optics	74		
	3.0.	Space charge and Child's law	79		
	3.8.		81		
	3.9.		90		
	3.10	Voltaic cells	92		
		Metallic conduction: classical theory	94		
		ences	95		
	Problems		96		
4.	. THE MAGNETIC EFFECTS OF CURRENTS AND				
	MOVING CHARGES, AND MAGNETOSTATICS				
	4.1.		98		
	4.2.	Magnetic dipole moment and magnetic shell	101		
	4.3.	Magnetostatics and magnetic media	107		
	4.4.	Solution of magnetostatic problems	111		
	4.5.	Steady currents in uniform magnetic media	114		
	4.6.	Calculation of the magnetic field strengths of simple circuits	122		

**	Contonto
X	Contents

	4.7. Refer Probl		125 129 129		
	1100	ons.	12)		
5.	ELECTROMAGNETIC INDUCTION AND VARYING				
	CURRENTS				
	5.1.	Faraday's laws of electromagnetic induction	132		
	5.2.	Self-inductance and mutual inductance	135		
	5.3.	Transient currents in circuits containing inductance, resistance,			
		and capacitance	140		
	5.4.	Magnetic energy and mechanical forces in inductive circuits	145		
	5.5.	Magnetic energy in magnetic media	149		
	5.6	Galvanometers and galvanometer damping	150		
	5.7.	The ballistic galvanometer and fluxmeter	153		
	5.8.	Absolute measurements	157		
	Refer	ence	160		
	Prob	ems	160		
6	MAG	NETIC MATERIALS AND MAGNETIC			
٠.		SUREMENTS			
	6.1.	Origins of magnetism	163		
		Diamagnetism	166		
	6.3.		169		
		Ferromagnetism	171		
	6.5.	Production of magnetic fields	174		
	6.6.	Measurement of magnetic fields	183		
	6.7.	Measurement of magnetic moment and susceptibility	184		
	6.8.	Experimental investigation of the hysteresis curve	188		
	6.9.	Terrestrial magnetism	190		
	Refer	ences	190		
	Prob	ems	191		
7.	ALTERNATING CURRENT THEORY				
	7.1.	Forced oscillations	193		
	7.2.	Use of vectors and complex numbers	196		
	7.3.	Tuned circuits	201		
	7.4.	Coupled resonant circuits	207		
	7.5	Low-frequency transformers	212		
	7.6.	Linear circuit analysis	215		
	Prob		222		
_					
8.		TROMAGNETIC WAVES	225		
	8.1.	Maxwell's equations of the electromagnetic field	225		
	8.2.	Plane waves in isotropic dielectrics	229		
	8.3.	The Poynting vector of energy flow	232		
	8.4.	Plane waves in conducting media	234		
	8.5.	The skin effect	236		
	8.6.	Reflections and refraction of plane waves at the boundary of two	000		
	0.7	dielectrics	239		
	8.7.	Reflection from the surface of a metal	246		
	8.8.	The pressure due to radiation	247		

	Contents	xi
8.9. Radiation from an oscillating dipo	ole	248
References		255
Problems		255
9. FILTERS, TRANSMISSION LINE	SAND	
WAVEGUIDES	3, AND	
9.1. Elements of filter theory		258
9.2. Some simple types of filter		263
9.3. Travelling waves on loss-free tran-	smission lines	267
9.4. Terminated loss-free lines		271
9.5. Lossy lines and resonant lines		277
9.6. Guided waves—propagation betw	een two parallel conducting	
planes		281
9.7. Waveguides		287
References		291
Problems		292
APPENDIX A. VECTORS		
A.1. Definition of scalar and vector qu	antities	A1
A.2. Vector addition and subtraction		A1
A.3. Multiplication of vectors		A1
A.4. Differentiation and integration of	vectors	A4
A.5. The divergence of a vector		A5
A.6. The curl of a vector		A6
A.6. The curl of a vector A.7. The divergence theorem		A8
A.8. Stokes's theorem		A8
A.9. Some useful vector relations		A9
A.10. Transformation from a rotating co	oordinate system	A10
A.11. Larmor's theorem		A11
APPENDIX B. DEPOLARIZING ANI	DEMAGNETIZING	
FACTORS	DEMINGREFIZING	A13
APPENDIX C. NUMERICAL VALUE	S OF THE	
FUNDAMENTAL CON	NSTANTS	A15
APPENDIX D. SOME USEFUL UNIT	CONVERSIONS	A16
INDEX		A17

1. Electrostatics I

1.1. The electrical nature of matter

THE fundamental laws of electricity and magnetism were discovered by experimenters who had little or no knowledge of the modern theory of the atomic nature of matter. It should therefore be possible to present these laws in a textbook by dealing at first purely in macroscopic phenomena and then introducing gradually the details of atomic theory as required, developing the subject almost in the historical order of discovery. Instead, in this book a basic knowledge of atomic theory is assumed from the beginning, and the macroscopic phenomena are related to atomic properties throughout.

Conductors and insulators

For the purpose of electrostatic theory all substances can be divided into two fairly distinct classes: conductors, in which electrical charge can flow easily from one place to another; and insulators, in which it cannot. In the case of solids, all metals and a number of substances such as carbon are conductors, and their electrical properties can be explained by assuming that a number of electrons (roughly one per atom) are free to wander about the whole volume of the solid instead of being rigidly attached to one atom. Atoms which have lost one or more electrons in this way have a positive charge, and are called ions. They remain fixed in position in the solid lattice. In solid substances of the second class, insulators, each electron is firmly bound to the lattice of positive ions, and cannot move from point to point. Typical solid insulators are sulphur, polystyrene, and alumina.

When a substance has no net electrical charge, the total numbers of positive and negative charges within it must just be equal. Charge may be given to or removed from a substance, and a positively charged substance has an excess of positive ions, while a negatively charged substance has an excess of electrons. Since the electrons can move so much more easily in a conductor than the positive ions, a net positive charge is usually produced by the removal of electrons. In a charged conductor the electrons will move to positions of equilibrium under the influence of the forces of mutual repulsion between them, while in an insulator they are fixed in position and any initial distribution of charge will remain almost indefinitely. In a good conductor the movement of charge is almost instantaneous, while in a good insulator it is extremely slow. While there is no such

2 Electrostatics I [1.2

thing as a perfect conductor or perfect insulator, such concepts are useful in developing electrostatic theory; metals form a good approximation to the former, and substances such as sulphur to the latter.

1.2. Coulomb's law and fundamental definitions

The force of attraction between charges of opposite sign, and of repulsion between charges of like sign, is found to be inversely proportional to the square of the distance between the charges (assuming them to be located at points), and proportional to the product of the magnitudes of the two charges. This law was discovered experimentally by Coulomb in 1785. In his apparatus the charges were carried on pith balls, and the force between them was measured with a torsion balance. The experiment was not very accurate, and a modern method of verifying the inverse square law with high precision will be given later (§ 1.3). From here on we shall assume it to be exact.

If the charges are q_1 and q_2 , and r is the distance between them, then the force F on q_2 is along r. If the charges are of the same sign, the force is one of repulsion, whose magnitude is

$$F = C \frac{q_1 q_2}{r^2}.$$

The vector equation for the force is

$$\mathbf{F} = C \frac{q_1 q_2}{r^3} \mathbf{r}. \tag{1.1}$$

Here \mathbf{F} , \mathbf{r} are counted as positive when directed from q_1 to q_2 . Eqn (1.1) is the mathematical expression of Coulomb's law.

The units of F and r are those already familiar from mechanics; it remains to determine the units of C and q. Here there are two alternatives: either C is arbitrarily given some fixed numerical value, when eqn (1.1) may be used to determine the unit of charge, or the unit of charge may be taken as some arbitrary value, when the constant C is to be determined by experiment. The Système International (S.I.), which will be used throughout this book, makes use of the second method. The force F is in newtons, the distance r in metres, and an arbitrary unit, the coulomb, is used to measure the charges q_1 and q_2 . The coulomb is directly related to the unit of current, the ampere, which is one coulomb per second; the ampere is defined by the forces acting between current-carrying conductors (see § 4.1). Eqn (1.1) for Coulomb's law is then analogous to that for gravitational attraction, except that it deals with electrical charges instead of masses; the constant of proportionality C must be determined by experiment. In the S.I., the constant C is written as $1/4\pi\epsilon_0$, the factor 4π being introduced here so that it occurs in formulae involving spherical rather than plane geometry. Eqn (1.1) therefore becomes

$$\mathbf{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^3} \mathbf{r},\tag{1.2}$$

where **F** is in newtons (N), **r** in metres (m), and q in coulombs (C). The quantity ϵ_0 is known as the 'permittivity of a vacuum' (see § 1.5); its experimental value (see § 5.8) is 8.85×10^{-12} coulomb² newton⁻¹ metre⁻² (C² N⁻² m⁻²)—a more convenient name for this unit (see § 1.6) is farad metre⁻¹ (F m⁻¹).

Electric field and electric potential

The force which a charge q_2 experiences when in the neighbourhood of another charge q_1 may be ascribed to the presence of an 'electric field' of strength \mathbf{E} produced by the charge q_1 . Since the force on a charge q_2 is proportional to the magnitude of q_2 , we define the field strength \mathbf{E} by the equation

$$\mathbf{F} = \mathbf{E}q_2. \tag{1.3}$$

From this definition and Coulomb's law it follows that E does not depend on q_2 , and is a vector quantity, like F. From eqn (1.2) we find that

$$\mathbf{E} = \frac{q_1}{4\pi\epsilon_0 r^3} \mathbf{r} \tag{1.4}$$

is the electric field due to the charge q_1 .

If a unit positive charge is moved an infinitesimal distance ds in a field of strength E, then the work done by the field is E.ds, and the work done against the field is -E.ds. This follows from the fact that the force on unit charge is equal to the electric field strength E. The work done against the field in moving a unit positive charge from a point A to a point B will therefore be

$$V = -\int_{A}^{B} \mathbf{E} \cdot d\mathbf{s}.$$

This is a scalar quantity known as the electric potential. If the field strength \mathbf{E} is due to a single charge q at O, as in Fig. 1.1, then the force on unit charge at an arbitrary point P is along OP, and ds is the vector element P_1P_2 . Now $\mathbf{E} \cdot d\mathbf{s} = E \cos \theta \, ds = E \, dr$, and hence

$$V_{\rm B} - V_{\rm A} = -\int_{\rm A}^{\rm B} E \, dr = -\frac{q}{4\pi\epsilon_0} \int_{r_1}^{r_2} \frac{dr}{r^2} = \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_2} - \frac{1}{r_1}\right).$$

Thus the difference of potential between A and B depends only on the positions of A and B, and is independent of the path taken between them.

4 Electrostatics I [1.2

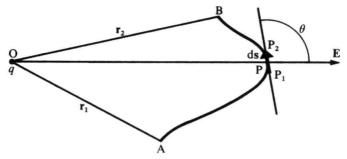


FIG. 1.1. Calculation of the potential difference between points A and B due to the field of a point charge q at O.

The potential at a point distance r from a charge q is the work done in bringing up unit charge to the point in question from a point at zero potential. By convention, the potential is taken as zero at an infinite distance from all charges, that is, V = 0 for $r = \infty$. Therefore the potential at a point distance r from a charge q is

$$V = q/4\pi\epsilon_0 r. \tag{1.5}$$

The difference in potential dV between P_1 and P_2 (Fig. 1.1) distance ds apart is

$$dV = -\mathbf{E} \cdot d\mathbf{s} = -(E_x dx + E_y dy + E_z dz).$$

Hence

$$\mathbf{E} = -\operatorname{grad} \mathbf{V} = -\nabla \mathbf{V},\tag{1.6}$$

where in Cartesian coordinates grad $V = i \partial V/\partial x + j \partial V/\partial y + k \partial V/\partial z$ and i, j, k are unit vectors parallel to the x-, y-, and z-axes. The components of E along the three axes are

$$E_{x} = -\frac{\partial V}{\partial x}, \qquad E_{y} = -\frac{\partial V}{\partial y}, \qquad E_{z} = -\frac{\partial V}{\partial z}.$$

The negative sign shows that of itself a positive charge will move from a higher to a lower potential, and work must be done to move it in the opposite direction. (For vector relations, see Appendix A.)

The work done in taking a charge q round a closed path in an electrostatic field is zero. This can be seen from Fig. 1.2. The work done in taking the charge q round the path ABCA is

$$W = -q \oint \mathbf{E} \cdot d\mathbf{s} = q(V_{B} - V_{A}) + q(V_{C} - V_{B}) + q(V_{A} - V_{C}) = 0,$$

and is independent of the path taken provided it begins and ends at the same point. Therefore the electric potential is a single-valued function of the space coordinates for any stationary distribution of electric charges; it has only one value at any point in the field.

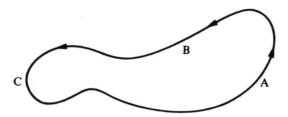


FIG. 1.2. The work done in taking an electric charge round a closed path in an electrostatic field is zero.

From the vector identity curl grad V = 0 or $\nabla \wedge (\nabla V) = 0$ (see Appendix § A.9, eqn (A.19)) it follows that curl $\mathbf{E} = 0$. Here curl \mathbf{E} is a vector whose components are

$$\bigg(\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} \,, \quad \frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x} \,, \quad \frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y}\bigg).$$

These components can be shown to be zero by the use of elementary circuits (cf. Appendix § A.6), and the fact that no work is done in taking a charge round a closed path. The relation curl $\mathbf{E} = 0$ holds because \mathbf{E} can be expressed as the gradient of a scalar potential: $\mathbf{E} = -\text{grad } V$. This is true in electrostatics, but does not hold when a changing magnetic flux threads the circuit (see § 5.1).

Since potential is a scalar quantity the potential at any point is simply the algebraic sum of the potentials due to each separate charge. On the other hand, \mathbf{E} is a vector quantity, and the resultant field is the vector sum of the individual fields. Hence it is nearly always simpler to work in terms of potential rather than field; once the potential distribution is found, the field at any point is found by using eqn (1.6).

Units

From eqn (1.3) we obtain the unit of electric field strength. An electric field of 1 unit exerts a force of 1 newton on a charge of 1 coulomb. Electric field strengths can therefore be expressed in newton coulomb⁻¹ (N C^{-1}).

The unit of potential is defined as follows: When 1 joule (J) of work is done in transferring a charge of 1 C from A to B, the potential difference between A and B is 1 volt (V). From eqn (1.6) E can be expressed in volt metre⁻¹ (V m⁻¹), and this is the unit which is customarily used. It is easily verified that the two alternative units for E are equivalent.

Lines of force

A line drawn in such a way that it is parallel to the direction of the field at any point is called a line of force. Fig. 1.3 shows the lines of force for