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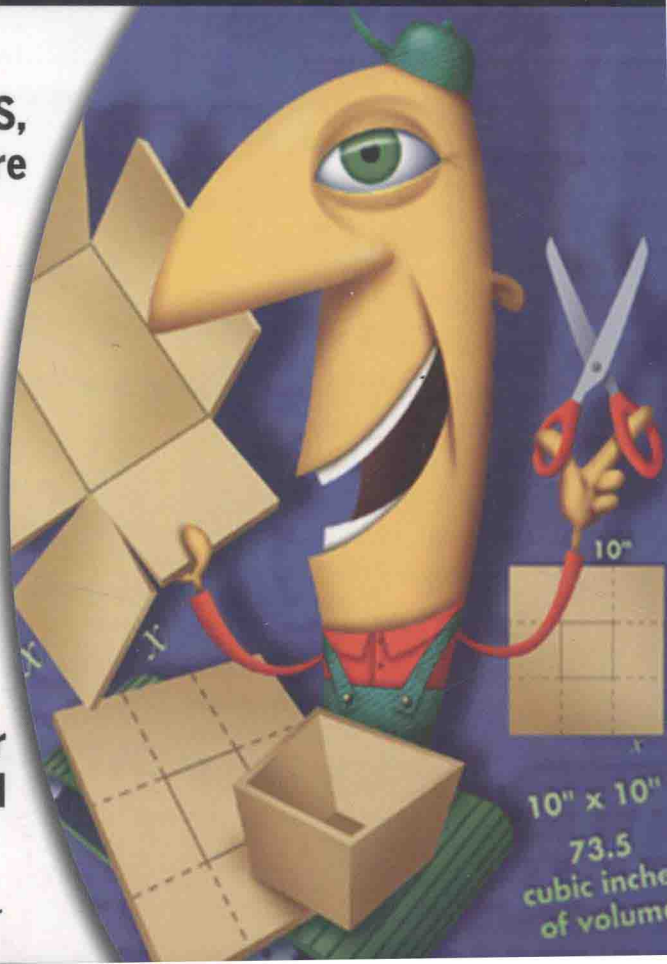
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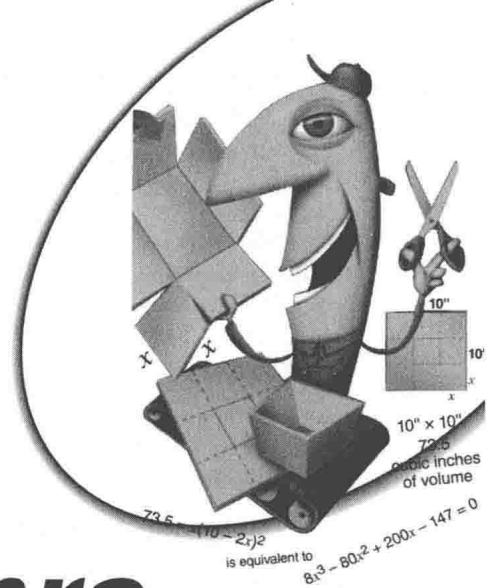
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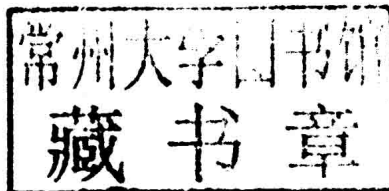




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Rhonda Huettenmueller



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*To my friends
from the Pohl Rec Center:*

*Jessica Carmona, Whitney Cook, Melissa Jenkins, Christin Ledford, Angela McGuire,
Angela Plata, Kristen Resendez, Samantha Rota, Mary Ann Teel, and Kia Williams.*

About the Author

Rhonda Huettenmueller has been teaching at the college level since 1990 and earned a PhD in mathematics in 2001. She is the author of several books in the *Demystified* series: *Algebra Demystified*, *College Algebra Demystified*, *Precalculus Demystified*, and *Business Calculus Demystified*.

Introduction

This book is meant to help you *understand* college algebra. While we will cover most of what a typical college algebra student must learn, we will cover it more carefully than an instructor can do so in class. I have found that most college algebra students struggle with the course because the material progresses too quickly.

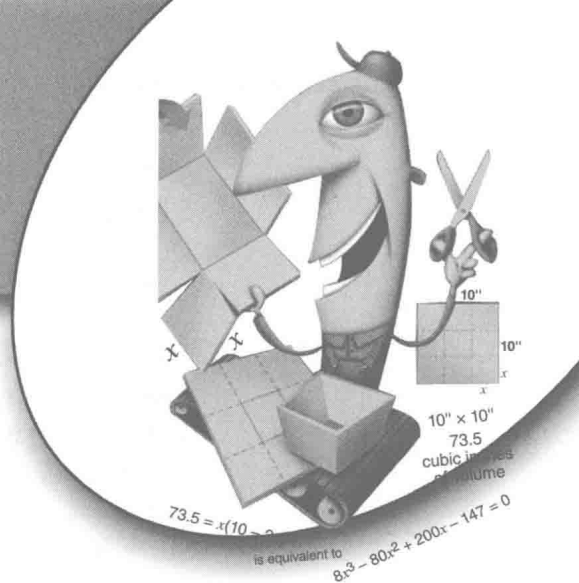
So that you do not have to absorb too much at once, each subsection contains exactly one new idea. You will not be distracted by missing algebra steps because I have included many of the algebra steps that most authors and instructors skip. The explanations are brief but clear and the examples are worked out in detail. I have used my more than 20 years of teaching experience to anticipate the questions you might have.

You'll get the most from this book if you work at it a little at a time. Because the topics build on each other, make sure that you understand the material from the previous sections before beginning a new section. If you have trouble working the Practice problems, solutions are worked out in detail so that you can self-correct. At the end of each chapter is a summary and a quiz. You should take each quiz as if you were in a classroom, that is, without notes and with a time limit. This will help you decide how well you understand the chapter. Try to prepare for the final exam at the end of the book as if it really were a comprehensive exam. Study the reviews at the end of each chapter before attempting the final. In fact, instead of answering all 90 questions at once, you might treat the final exam as three separate 30-question exams, trying to improve your score each time.

With steady work and patience, I think you will surprise yourself with success. Good luck.

Rhonda Huettenmueller

Contents



	<i>Introduction</i>	<i>xiii</i>
CHAPTER 1	Fundamentals	1
	The Distributive Property	2
	Rational Expressions	7
	Simplifying Rational Expressions	8
	Multiplying Rational Expressions	8
	Adding Rational Expressions	9
	Exponents and Roots	13
	Summary	17
	Quiz	18
CHAPTER 2	Linear Equations and Inequalities	21
	Basic Linear Equations	22
	Equations Leading to Linear Equations	25
	Absolute Value Equations	30
	Linear Inequalities	35
	Compound Inequalities	36
	Absolute Value Inequalities	39
	Summary	47
	Quiz	49
CHAPTER 3	Quadratic Equations	51
	Solving Quadratic Equations by Factoring	52
	The Quadratic Formula	53

	Completing the Square	56
	Summary	63
	Quiz	64
<hr/>		
CHAPTER 4	The xy-Coordinate Plane	65
	Plotting Points	66
	The Distance Between Two Points	67
	The Midpoint Formula	76
	Circles	77
	Summary	88
	Quiz	89
<hr/>		
CHAPTER 5	Lines and Parabolas	91
	Introduction to Lines	92
	Intercepts	95
	The Slope of a Line	102
	Horizontal and Vertical Lines	105
	Finding an Equation for a Line	107
	The Slope-Intercept Form of a Line	112
	Graphing the Line Using the Slope and y -Intercept	113
	Parallel and Perpendicular Lines	116
	Linear Applications	123
	Parabolas	134
	Sketching the Graph of a Parabola	135
	Locating the Vertex by Completing the Square	141
	Summary	147
	Quiz	149
<hr/>		
CHAPTER 6	Nonlinear Inequalities	153
	Solving Nonlinear Inequalities Graphically	154
	Solving Nonlinear Inequalities	157
	Sign Graphs	159
	Rational Inequalities	165
	Summary	173
	Quiz	174

CHAPTER 7	Functions	175
	Introduction to Functions	176
	Evaluating Functions	178
	Evaluating Piecewise Functions	180
	Domain and Range	182
	Functions and Their Graphs	188
	Finding the Domain and Range Graphically	193
	Increasing Intervals and Decreasing Intervals	197
	The Graph of a Piecewise Function	200
	More on Evaluating Functions	209
	The Difference Quotient	212
	Summary	217
	Quiz	220

CHAPTER 8	Quadratic Functions	223
	A Review of a Parabola's Vertex	224
	The Range of a Quadratic Function	226
	The Maximum/Minimum of a Quadratic Function	228
	Applied Maximum/Minimum Problems	230
	Revenue-Maximizing Price	239
	Maximizing/Minimizing Other Functions	242
	Summary	243
	Quiz	244

CHAPTER 9	Transformations and Combinations	247
	Transformations	248
	Reflections, and Vertical Stretching and Compressing	253
	Sketching the Graph of a Transformation	259
	Special Functions	264
	Even/Odd Functions	281
	Combining Functions	286
	Function Composition	287
	Function Composition for a Single Value	290
	The Domain for the Composition of Functions	295
	Summary	298
	Quiz	300

CHAPTER 10	Polynomial Functions	305
	Introduction to Polynomial Functions	306
	Sketching Graphs of Polynomials	314
	Polynomial Division	317
	Synthetic Division	324
	Synthetic Division and Factoring	331
	Rule of Signs and Upper and Lower Bounds Theorem	340
	Complex Numbers	346
	Complex Solutions to Quadratic Equations	354
	The Fundamental Theorem of Algebra	357
	Summary	370
	Quiz	372

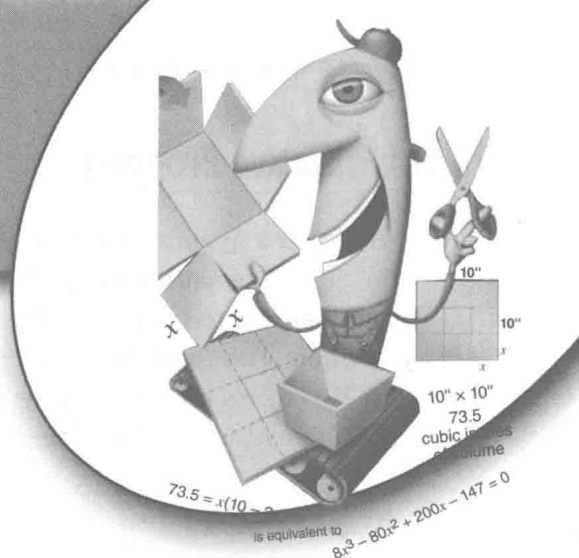
CHAPTER 11	Systems of Equations and Inequalities	375
	Systems of Linear Equations	376
	Elimination by Addition	380
	Applications for Systems of Equations	390
	Systems Containing Nonlinear Equations	396
	Inequalities and Systems of Inequalities	401
	Systems of Inequalities	408
	Summary	419
	Quiz	421

CHAPTER 12	Exponents and Logarithms	425
	Compound Growth	426
	The Number e	430
	Increasing Population	431
	Logarithms	434
	Properties of Logarithms	436
	Three More Important Logarithm Properties	439
	Using Multiple Logarithm Properties	441
	Equations Involving Exponents and Logarithms	445
	Exponent and Logarithm Functions	453
	The Domain of a Logarithm Function	459
	Summary	460
	Quiz	463

<i>Final Exam</i>	467
<i>Answers to Quizzes and Final Exam</i>	483
<i>Index</i>	487

chapter 1

Fundamentals



Success in any math class depends on a solid foundation in fundamentals. For college algebra, this means the ability to do the basics: arithmetic, factoring, solving equations, and working with rational expressions, exponents, and roots. The first two chapters are meant to dust off your algebra skills. If you find anything in this chapter (or the next) that is covered too fast, you might consider using my book *Algebra Demystified*, which covers these topics more carefully. If you are already comfortable with the basics, then you can safely skip this chapter.

CHAPTER OBJECTIVES

In this chapter, you will

- Use the Distributive Property to expand and factor expressions
- Use the FOIL method to expand expressions
- Simplify rational expressions (fractions containing a variable)
- Perform arithmetic on rational expressions
- Work with exponent and radical properties

The Distributive Property

A *term* is a quantity separated by a plus or minus sign. For example, the terms in the expression $3x^2y + 10xy + 4xy^2 + 9$ are $3x^2y$, $10xy$, $4xy^2$, and 9. The number in a term is called the *coefficient*. A term without a variable is called a *constant*. The constant in this example is 9, and the coefficients are 3, 10, 4, and 9. Two terms are *alike* if they have the same variables to the same powers. We combine *like* terms by adding/subtracting coefficients on terms that are alike.



EXAMPLE 1-1

Combine like terms.

$$14x^2y + 8y + 3x + 2x^2y - 5y + 7x$$

We begin by rewriting the expression so that like terms are next to each other. After that, we simply add their coefficients.

$$\begin{aligned} 14x^2y + 8y + 3x + 2x^2y - 5y + 7x &= (14x^2 + 2x^2y) + (8y - 5y) \\ &\quad + (3x + 7x) = 16x^2y + 3y + 10x \end{aligned}$$

We use the Distributive Property a lot in algebra. This property allows us to write expressions both in *expanded form* and in *factored form*.

$$\begin{array}{cc} \text{Factored form} & \text{Expanded form} \\ a(b \pm c) & = ab \pm ac \end{array}$$



EXAMPLE 1-2

Use the Distributive Property to expand the expression.

$$\bullet 3(2xy - 5xy^2)$$

3 is distributed here.

$$3(2xy - 5xy^2) = 3(2xy) - 3(5xy^2) = 6xy - 15xy^2$$

$$\bullet 10x(4y + 6xy - 7x)$$

$$\begin{aligned} 10x(4y + 6xy - 7x) &= 10x(4y) + 10x(6xy) - 10x(7x) \\ &= 40xy + 60x^2y - 70x^2 \end{aligned}$$