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MECHANICS OF TURBULENCE OF MULTICOMPONENT GASES

MIKHAIL YA. MAROV
ALEKSANDER V. KOLESNICHENKO



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MECHANICS OF TURBULENCE OF MULTICOMPONENT GASES

by

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