
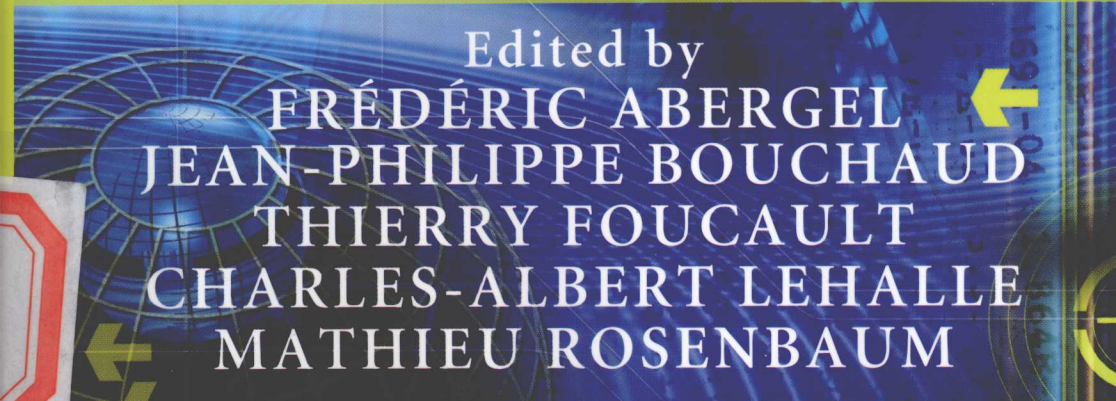


WILEY FINANCE



Market microstructure

Confronting Many Viewpoints



Edited by
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Introduction

The accumulation of high frequency market data in recent years has revealed many surprising results. These results are interesting both from theoretical and practical standpoints. The mechanism of price formation is at the very heart of economics; it is also of paramount importance to understand the origin of the well-known anomalous ‘stylized facts’ in financial price series (heavy tails, volatility clustering, etc.). These issues are of obvious importance for practical purposes (organisation of markets, execution costs, price impact, etc.). This activity is also crucial to help the regulators, concerned with the organisation of liquidity in electronic markets and the issues raised by ‘high frequency trading’.

Correspondingly, this problem has been vigorously investigated by at least five different communities (economics, financial mathematics, econometrics, computer science and econo-physics), scattered in academic institutions, banks and hedge funds, with at present limited overlap and sometimes lack of visibility. On the other hand, due to the gigantic amount of available data, precise quantitative theories can now be accurately tested.

At the time where this conference series started in 2010, the interest for market microstructure had finally reached a stage where the interest for the theoretical breakthroughs of the pioneers in the field had become comparable to its practical importance for market practitioners. Thanks to the development of high frequency trading, market microstructure is now, not only a subject of theoretical modelling and simulation but, more interestingly maybe, a real practical field where a better model can make a big difference.

The organisers of the conference thought that it would be extremely fruitful to confront the ideas that have blossomed in those different

communities in the past decade. In order to foster this confrontation and ease communication, we have gathered researchers from these different communities, including professionals, and ask them to give introductory tutorials, reviewing both their recent activity and the problems that, in their eyes, are most relevant to address in the near future.

Our aim in setting up this friendly, knowledge-oriented confrontation has been to examine and compare possibly very different views on the nature of the mechanisms relevant to describe and understand what one can actually observe when scrutinising the tick-by-tick behaviour of markets. Such important questions as the interplay between liquidity taking and providing, the existence and characterisation of various types of market impact, the statistical tools designed to handle well the ‘tick’ effect, the ‘best-execution’ and other algorithmic trading strategies, or the question of market design and organisation . . . have been studied in-depth by the speakers at the conference, and their contributions to this present volume will help shed a new light, or, rather, new lights, on the market microstructure viewed as an object for scientific study as well as a wealth of information for price discovery and trading.

Frédéric Abergel
Jean-Philippe Bouchaud
Thierry Foucault
Charles-Albert Lehalle and
Mathieu Rosenbaum

About the Editors

Frédéric Abergel

After graduating from École Normale Supérieure in 1985 and completing a PhD in Mathematics in 1986, Frédéric Abergel started an academic career as a researcher with the CNRS. He spent ten years in the Mathematics Department of the University of Orsay Paris XI, where he obtained his habilitation degree in 1992. He then switched to the capital markets industry and became a 'quant' (quantitative analyst). During the second part of his career, Frédéric Abergel has worked for trading floors in various financial institutions, mainly in the derivatives sector, developing pricing and hedging models. In July 2007, he decided to return to Academia, where he now holds the BNP Paribas Chair of Quantitative Finance at École Centrale Paris. His research focuses on the study of empirical properties and mathematical model of market microstructure, high frequency data and algorithmic trading.

Jean-Philippe Bouchaud

Jean-Philippe Bouchaud graduated from the École Normale Supérieure in Paris, where he also obtained his PhD in physics. He was then appointed by the CNRS until 1992. After a year spent in the Cavendish Laboratory (Cambridge), he joined the Service de Physique de l'État Condensé (CEA-Saclay), where he worked on the dynamics of glassy systems and on granular media. He became interested in economics and theoretical finance in 1991. His work in finance includes extreme risk models, agent based simulations, market microstructure and price formation. He has been very critical about the standard concepts and models used in economics and in the financial industry (market efficiency, Black-Scholes models, etc.) He founded the company Science &

Finance in 1994 that merged with Capital Fund Management (CFM) in 2000. He is now the President and Head of Research at CFM and professor at Ecole Polytechnique since 2008. He was awarded the IBM young scientist prize in 1990 and the C.N.R.S. Silver Medal in 1996. He has published over 250 scientific papers and several books in physics and in finance.

Thierry Foucault

Thierry Foucault is Professor of Finance at HEC, Paris, where he received his PhD in Finance in 1994. He is a research fellow of the Centre for Economic Policy (CEPR). He has taught in various institutions such as Carnegie Mellon University, the École Polytechnique Fédérale de Lausanne, Oxford (Said Business School), Pompeu Fabra University (Spain), the Tinbergen Institute and the School of Banking and Finance at UNSW. His research focuses on the determinants of financial markets liquidity and the industrial organisation of the securities industry. His work has been published in top-tier scientific journals, including *The Journal of Finance*, *The Journal of Financial Economics* and *The Review of Financial Studies*. He serves on the scientific committees of the Autorité des Marchés Financiers, the Research Foundation of the Banque de France, the Group of Economic Advisors of the Committee of Economic and Markets Analysis of the European Securities and Markets Authority (ESMA) and on the executive committee of the European Finance Association (EFA). He acts as co-editor of the Review of Finance since 2009 and is an Associate Editor of *The Review of Asset Pricing Studies*. For his research, he received awards from the Europlace Institute of Finance in 2005 and 2009, the annual research prize of the HEC Foundation in 2006 and 2009, and the Analysis Group award for the best paper on Financial Markets and Institutions presented at the 2009 Western Finance Association meetings.

Charles-Albert Lehalle

Currently Head of Quantitative Research at CA Cheuvreux, Charles-Albert Lehalle is an international expert in optimal trading. He published papers in international journals about the use of stochastic control and stochastic algorithms to optimise a trading flow with respect to flexible constraints. He also authored papers on post-trade analysis, market impact estimates and modelling the dynamics of limit order books. Charles-Albert Lehalle lectures at 'Paris 6 (El Karoui) Master of Finance' (École Polytechnique, ESSEC, École Normale Supérieure) and

MASEF/ENSAE, and gives master classes in the Certificate in Quantitative Finance in London. With a PhD in applied mathematics, his core fields are stochastic processes, information theory and nonlinear control.

Mathieu Rosenbaum

Mathieu Rosenbaum obtained his PhD from Université Paris-Est in 2007. He is now Professor at Université Pierre et Marie Curie (Paris 6) and École Polytechnique and is a member of the CREST (Center of Research in Economics and Statistics). His research mainly focuses on statistical finance problems, such as market microstructure modeling or designing statistical procedures for high frequency data. Also, he has research collaborations with several financial institutions, in particular BNP-Paribas since 2004.

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Part I

Economic Microstructure

Theory

Algorithmic Trading: Issues and Preliminary Evidence

Thierry Foucault

1.1 INTRODUCTION

In 1971, while the organization of trading on the NYSE had not changed much since its creation in 1792, Fischer Black (1971) was asking whether trading could be automated and whether the specialist's judgment could be replaced by that of a computer (the specialist is a market-maker designated to post bid and ask quotes for stocks listed on the NYSE). Forty years later, market forces have given a positive response to these questions.

Computerization of trading in financial markets began in the early 1970s with the introduction of the NYSE's "designated order turnaround" (DOT) system that routed orders electronically to the floor of the NYSE. It was then followed with the development of program trading, the automation of index arbitrage in the 1980s, and the introduction of fully computerized matching engines (e.g., the CAC trading system in France in 1986 or the Electronic Communication Networks in the US in the 1990s). In recent years, this evolution accelerated with traders using computers to implement a wide variety of trading strategies, e.g., market-making, at a very fine time scale (the millisecond).

The growing importance of these "high frequency traders" (HFTs) has raised various questions about the effects of algorithmic trading on financial markets. These questions are hotly debated among practitioners, regulators, and in the media. There is no agreement on the

effects of HFTs.¹ As an example consider these rather opposite views of the HFTs' role by two Princeton economists, Paul Krugman and Burton Malkiel. Krugman has a rather dim view of HFTs:

High-frequency trading probably degrades the stock market's function, because it's a kind of tax on investors who lack access to those superfast computers – which means that the money Goldman spends on those computers has a negative effect on national wealth. As the great Stanford economist Kenneth Arrow put it in 1973, speculation based on private information imposes a “double social loss”: it uses up resources and undermines markets. (Paul Krugman, “Rewarding Bad Actors”, *New York Times*, 2 August 2009).

In contrast, for Malkiel, high frequency traders have a more positive function:

In their quest to find trading profits, competition among high-frequency traders also serves to tighten bid-offer spreads, reducing transactions costs for all market participants, both institutional and retail. Rather than harming long-term investors, high-frequency trading reduces spreads, provides price discovery, increases liquidity and makes the market a fairer place to do business. (Burton Malkiel, “High Frequency Trading is a Natural Part of Trading Evolution”, *Financial Times*, 14 December 2010).

Concerns have also been voiced that HFTs could manipulate markets to their advantage, exacerbate market volatility and that high frequency trading could be a new source of fragility and systemic risk for the financial system. In particular, some have suggested that HFTs may have been responsible for the flash crash of 6 May 2010.

Not surprisingly, given these concerns and lack of consensus on the exact role of algorithmic traders, debates are now raging about whether actions should be taken to regulate algorithmic trading. A (certainly incomplete) list of questions raised in these debates is as follows (see SEC, 2010, Section IV, or CESR, 2010a and 2010b):

1. *Liquidity*. What is the effect of algorithmic trading on market liquidity? Is liquidity more likely to evaporate in turbulent times when it is provided by HFTs?

¹ Although algorithmic trading is not a new phenomenon, algorithmic trading, especially high frequency trading, went to the forefront of policy debates in recent years. A search on articles from newspapers, magazines, academic journals, trade publications, etc., containing the words “algorithmic trading” on EBSCO yields 2502 hits over the period 2005–2011 and only 329 over the period 1999–2004.