



3D Game Engine Design

A Practical Approach to Real-Time Computer Graphics Second Edition

3D游戏引擎设计

实时计算机图形学的应用方法

(英文版・第2版)

[美] David H. Eberly 著





2009.

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、民邮电出版社 北

图书在版编目(CIP)数据

3D游戏引擎设计:实时计算机图形学的应用方法=3D Game Engine Design: A Practical Approach to Real-Time Computer Graphics, Second Edition:第2版:英文/(美)埃伯利(Eberly, D. H.)著.—北京:人民邮电出版社, 2009.2

(图灵原版计算机科学系列) ISBN 978-7-115-19553-1

I. 3… II. 埃… III. ①三维 - 动画 - 计算机图形学 - 教材 - 英文 ②游戏 - 软件设计 - 教材 - 英文 IV. TP391.41 TP311.5

中国版本图书馆CIP数据核字(2008)第204792号

内容提要

本书深入剖析了3D游戏引擎的设计,书中许多内容对于更好地理解3D计算机图形学也极有帮助。本书首先介绍了几何转换和坐标系统等较基础的内容,然后介绍曲线、渲染、效果等高级知识。本书基于作者自身在游戏产业中的工作、研究经验,提供了算法、编程技术、代码等大量实用信息,对于游戏设计者及相应的编程人员来说,是一本非常有价值的参考书。

本书适合高等院校相关专业的师生、接受游戏软件开发培训的学生、相关技术人员及游戏开发人员阅读。

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责任编辑 杨海玲

♦ 人民邮电出版社出版发行 北京市崇文区夕照寺街14号

邮编 100061 电子函件 315@ptpress.com.cn

网址 http://www.ptpress.com.cn

三河市海波印务有限公司印刷

◆ 开本: 800×1000 1/16

印张: 64.75 彩插: 8

字数: 1243千字 2009年2月第1版

印数: 1-2000 册 2009年2月河北第1次印刷

著作权合同登记号 图字: 01-2008-5826号

ISBN 978-7-115-19553-1/TP

定价: 138.00元

读者服务热线: (010) 88593802 印装质量热线: (010) 67129223 反盗版热线: (010) 67171154

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3D Game Engine Design: A Practical Approach to Real-Time Computer Graphics, Second Edition by David H. Eberly, ISBN: 978-0-12-447751-3.

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Authorized English language reprint edition published by the Proprietor.

ISBN: 978-981-272-315-4

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Elsevier (Singapore) Pte Ltd.

3 Killiney Road #08-01 Winsland House I Singapore 239519

> Tel: (65)6349-0200 Fax: (65)6733-1817

First Published 2009 2009年初版

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PREFACE

The first edition of 3D Game Engine Design appeared in print over six years ago (September 2000). At that time, shader programming did not exist on consumer graphics hardware. All rendering was performed using the fixed-function pipeline, which consisted of setting render states in order to control how the geometric data was affected by the drawing pass.

The first edition contained a CDROM with the source code for Wild Magic Version 0.1, which included 1,015 source files and 17 sample applications, for a total of 101,293 lines of code. The distribution contained support only for computers running the Microsoft Windows operating system; the renderer was built on top of OpenGL; and project files were provided for Microsoft Visual C++ 6. Over the years, the source code evolved to Wild Magic Version 3.9, which contained additional support for Linux and Macintosh platforms, had OpenGL and Direct3D renderers, and included some support for shader programming. However, the design of the engine was still based on a fixed-function pipeline. The distribution also included support for multiple versions of Microsoft's compilers, support for other compilers on the various platforms, and contained some tools such as importers and exporters for processing of art assets.

This is the second edition of 3D Game Engine Design. It is much enhanced, describing the foundations for shader programming and how an engine can support it. The second edition is about twice the size of the first. The majority of the increase is due to a more detailed description of all aspects of the graphics system, particularly about how shaders fit into the geometric pipeline. The material on scene graphs and their management is also greatly expanded. The second edition has more figures and less emphasis on the mathematical aspects of an engine.

The second edition contains a CDROM with the source code for Wild Magic Version 4.0, which includes 1,587 source files and 105 sample applications, for a total of 249,860 lines of code. The Windows, Linux, and Macintosh platforms are still supported, using OpenGL renderers. The Windows platform also has a Direct3D renderer whose performance is comparable to that of the OpenGL renderer. Multiple versions of Microsoft's C++ compilers are supported—versions 6, 7.0, 7.1, and 8.0 (Professional and Express Editions). The MINGW compiler and MSYS environment are also supported on the Windows platform. The Linux platform uses the g++ compiler, and the Macintosh platform uses Apple's Xcode tools.

① 凡是编号后标有"*"的图都配有对应的彩色插图。——编者注

② 本书出版并未随书附带光盘,凡书中提到CDROM中的Wild Magic Version 4.0的源代码可从Geometric Tools公司网站(www.geometrictools.com)下载。——编者注

The graphics system of Wild Magic Version 4.0 is fully based on shader programming and relies on NVIDIA's Cg programming language. The precompiled shader programs were created using the arbvp1 and arbfp1 profiles for OpenGL and using the vs_2_0 and ps_2_0 profiles for Direct3D, so your graphics hardware must support these in order to run the sample applications. If your graphics hardware supports only lesser profiles such as vs_1_1 and ps_1_1, you must recompile the shader programs with these profiles and use the outputs instead of what is shipped on the CDROM. The distribution also contains a fully featured, shader-based software renderer to illustrate all aspects of the geometric pipeline, not just the vertex and pixel shader components.

The replacement of the fixed-function approach by a shader-based approach has made Wild Magic Version 4 a much more powerful graphics engine for use in all graphics applications, not just in games. Much effort went into making the engine easier to use and to extend, and into improving the performance of the renderers. I hope you enjoy this new manifestation of Wild Magic!

A book is never just the product of the author alone. Many people were involved in making this book as good as it possibly can be. Thanks to the reviewers for providing valuable and insightful feedback about the first edition regarding how to improve it for a second edition. A special thanks goes to Marc Olano (University of Maryland, Baltimore County) for taking the time to provide me with detailed comments based on his experience using the first edition as a textbook. Thanks to Elisabeth Beller, the production editor and project manager for all of my Morgan Kaufmann Publisher books, for assembling yet another fine group of people who have the superb ability to take my unattractive book drafts and make them look really good. And, as always, thanks to my editor Tim Cox for his patience and help in producing yet another book for Morgan Kaufmann Publishers.

GEOMETRIC TOOLS, INC. LICENSE AGREEMENTS

Wild Magic has two license agreements, one for the Foundation library source code and one for the remaining source code. These agreements are located in the directory GeometricTools/WildMagic4 of the CD-ROM. The Foundation library agreement is Wm4FoundationLicense.pdf and the other agreement is Wm4RestrictedLicense.pdf.

INSTALLATION OF THE SOFTWARE

The installation manual and release notes are located in the directory Geometric Tools/WildMagic4 of the CD-ROM. The document name is Wm4Installation Release.pdf. Please read this document before installing the software.

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