



A Practical Logic of Cognitive Systems

VOLUME 2

The Reach of Abduction

Insight and Trial

**BY
DOV M. GABBAY AND JOHN WOODS**

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Volume 2

The Reach of Abduction
Insight and Trial

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In Memoriam

Raymond Reiter

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Preface

Although *A Practical Logic of Cognitive Systems* exhibits some common themes, we have written the individual volumes with a view to their being read either as stand-alone works or as linked and somewhat overlapping items in the series, depending on the interests of particular readers. Relevance was our main theme in volume one; abduction will occupy us in the present volume; and volume three will concern itself with fallacious reasoning. Here too, we intend to honour the pledge of independent readability. Even so, certain continuities will also be evident in all volumes, of which the first and foremost is what we suggest about the structure of practical reasoning. In some cases, it will be unavoidable that we repeat a point made in a predecessor volume. Sometimes we will elaborate upon a prior point. On occasion, we will correct what we now see as a mistake.

In writing our predecessor volume on relevance, we were mindful of two approaches to the subject that had attained dominant purchase. One is the output of a generation's research on relevant logic, ensuing from the work of Alan Ross Anderson and Nuel D. Belnap, Jr., beginning in the late 1950s. The other is the theory of the communication theorists, Dan Sperber and Deirdre Wilson, whose influential pragmatic account appeared in 1986. We did not want to write a derivative book; neither were we much attracted by the prospects of polemical attack. We desired to take an approach that at once recognized the significance of the dominant views, while attempting to advance beyond them in substantial measure.

Abduction faces us with a somewhat different challenge. No less central a factor in practical reasoning than relevance, we trust that we give no offence in observing that the abductive landscape is not yet presided over by dominant theoretical presences, in the manner of relevance. A possible exception to this are the scattered contributions by the modern founder of abductive logic, Charles Peirce. Peirce's sallies are indeed seminal, and dotted with some brilliantly original insights. But unlike the cumulative record of modern relevant logicians and the detailed theoretical articulation of Sperber's and Wilson's account, Peirce left the logic of abduction in a comparatively undeveloped state. It is true that there is by now a large literature on abduction, created by an impressive number of authors

from philosophy, cognitive psychology, computer science, artificial intelligence and, of course, logic. From philosophy alone it may be suggested that, contrary to our present suggestion, an important approach has indeed presented itself in the literature that has grown up around Gilbert Harman's significant paper from 1965 on inference to the best explanation. There can be no doubt that inference to the best explanation is an important idea which has been ably probed by a generally sophisticated literature. Even so, we are not quite ready to accede to a dominance that is more arguably to be found in the literature on relevance. There are three reasons for this reluctance. One is that various kinds of abductive practice have nothing to do with achieving explanations. Another is that even in those cases in which abduction has an explanationist character, the factor of explanation is but a part, albeit an important part, of the abductive pie. Thirdly, in some versions of it, inference to the best explanation is not abductive, surprising as that may strike us initially.

If we are correct in these observations, abduction is a more wide-open field than relevance. For the would-be theorist this is an advantage and a disadvantage. The advantage is that achieving a dominant position is, in principle, a target still to be aimed at. The disadvantage is that there are fewer stout shoulders on which the theorist might secure a purchase. Still, we don't wish to leave the impression that the abductive theorist's is a voice in a solitary wilderness. There is much good work that has already been published, of which three recent examples are [Aliseda, forthcoming; Magnani, 2001a] and [Meheus *et al.*, forthcoming].

The comparative openness of the logic of abduction makes a book such as this in like degree an enterprise of first words rather than last. Even in what we think we have already come to understand about abduction, there is ample discouragement of the idea that all of abduction can be gobbled up in a single try. Accordingly, the best we can hope for is new ground decisively broken in ways that portend favourably for the grand theory, whenever it appears.

Part I

A Practical Logic of Cognitive Systems

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Chapter 1

Introduction

It is sometimes said that the highest philosophical gift is to invent important new philosophical problems. If so, Peirce is a major star on the firmament of philosophy. By thrusting the notion of abduction to the forefront of philosophers' consciousness he created a problem which — I will argue — is the central one in contemporary epistemology.

Jaakko Hintikka,

The surprising fact C is observed. But if A were true, C would be a matter of course. Hence there is reason to suspect that A is true.

Charles S. Peirce

Abduction is our subject here. We meet it in a state of heightened theoretical activity. It is part of the contemporary research programmes of logic, cognitive science, AI, logic programming, and the philosophy of science. This is a welcome development. It gives us multiple places to look for instruction and guidance.

The approach that we take in this book is broadly logical. Any fears, even so, that this will be an over-narrow orientation may be allayed by our decision to define logic as the disciplined description of the behaviour of real-life logical agents. In this we command a theme that has played since antiquity: that logic is an account of how thinking agents reason and argue. Because we wish to give due attention to the process side of the process-product distinction, we propose a rapprochement between logic and psychology, with a special emphasis on developments in cognitive science. It would be foolish to suggest that the hugely profitable theoretical attainments of modern mathematical logic have no place in an agent-based, psychologically realistic account of abduction. The rich yield in