

The background of the entire cover is a repeating isometric pattern of cubes. Each cube is rendered with three visible faces: a top face, a front face, and a right side face. The top faces are a light gray color, while the front and side faces are a slightly darker gray. The cubes are arranged in a grid-like fashion, creating a three-dimensional effect across the entire surface.

# **STATISTICS FOR THE HELPING PROFESSIONS**

**FRANK P. BESAG  
AND  
PETER L. BESAG**

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**SAGE PUBLICATIONS** Beverly Hills London New Delhi

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*For information address:*

SAGE Publications, Inc.  
275 South Beverly Drive  
Beverly Hills, California 90212

SAGE Publications India Pvt. Ltd.  
C-236 Defence Colony  
New Delhi 110 024, India



SAGE Publications Ltd  
28 Banner Street  
London EC1Y 8QE, England

Printed in the United States of America

## **Library of Congress Cataloging in Publication Data**

Besag, Frank P.

Statistics for the helping professions.

Includes index.

I. Social sciences—Statistical methods. 2. Social service—Statistical methods. I. Besag, Peter.

II. Title.

HA29.B4525 1984 519.5 84-13399

ISBN 0-8039-2340-6

**SECOND PRINTING**

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To Charles Loewner, Stanford University, who brought the light of his spirit and his knowledge to those around him. —P.L.B.

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## PROLOGUE

Statistics for the helping professions are different than for other fields. Not that the calculations are different or that even different procedures are used. Rather, the questions asked are different. Helping professionals deal in concrete situations that directly affect the lives of people, and not just any people, but people with whom we have to work on a daily basis. Our questions deal not only with scientific truth but also with practical reality and personal concerns.

What we have needed is a book that explains not only which statistical procedures will be of help in our decision making but also which procedures should not be used and why. Helping professionals are always asking "Why?" and "Why not?" and that is the way this text is designed.

This book, then, is an attempt not only to show the "how to" of statistics, but more importantly, to show the "why" and the "why not." It is a philosophical book more than an arithmetic book. Less time is spent on computations, which computers can perform, while more time is spent on the nonmechanical aspects of statistics; for example, logical constraints, thoughtfulness, and human concern.

The book is divided into six sections:

- I. Philosophy, History, and Science, Chapters 1 and 2
- II. Definitions, Dialectics, and More Definitions, Chapters 3 and 4
- III. Descriptive Methods, Chapters 5 through 7
- IV. Probables, Improbables, Common and Rare, Chapters 2 through 11
- V. Parameter Estimation and Tests of Hypotheses, Chapters 12 through 14
- VI. Common Statistical Procedures, Statistical Significance, and Helping Professions' Alternatives, Chapters 15 through 18

Before leaving this prologue, the authors acknowledge that this book would not have been possible without the aid and assistance of David Farr, Professor of Educational Psychology, SUNY-Buffalo; H. Warren Button, Professor, Foundations of Education, SUNY-Buffalo; Leonard Abrams,



Lockheed Corporation; Robert Mercer, The Aerospace Corporation; William Feyerherm, Richard Cummings, Ronald Podeschi, Stephen Nolte, Barbara Lee, and Maureen Wahl, and again Maureen Wahl of the University of Wisconsin-Milwaukee. They gave generously of their time to read the manuscript and make the comments, which were so necessary. Much of the wealth of this book comes from them. Any errors in the book lie with the authors.

Perhaps the most tedious and irritating task was performed, and then performed again, and again, by Winifred Fairweather Flisram, Dana Gallas Hackenberg, and most especially Cathy Nelson. They had to cope with the seemingly never-ending rewrites, bad spelling, ridiculous formulas, and “You want it when?” In any event, our heartfelt thanks for an often thankless job.

Particular thanks to Dean Michael Stolee, a good and decent person, without whose aid and support so many things would not have been possible.