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# Introduction to C++ for financial engineers

*An Object-Oriented Approach*

DANIEL J. DUFFY

# Introduction to C++ for Financial Engineers

An object-oriented approach

**Daniel J. Duffy**



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# Introduction to C++ for Financial Engineers

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# Goals of this Book and Global Overview

## 0.1 WHAT IS THIS BOOK?

The goal of this book is to introduce the reader to the C++ programming language and its applications to the field of Quantitative Finance. It is a self-contained introduction to the syntax of C++ in combination with its applications to current topics of interest. In particular, we develop libraries, frameworks and applications for a variety of derivatives models using numerical methods such as binomial and trinomial trees, finite difference methods (FDM) and the Monte Carlo (MC) method.

The book consists of three major parts. The first part concentrates on essential C++ syntax that must be learned before proceeding. The second part introduces generic programming and design pattern techniques and we show how to create libraries and data structures that we use in part three that deals with full applications. We also have written a number of chapters on topics related to the current book, for example a review of the C language, interfacing with Excel and an introduction to the Component Object Model (COM).

This book is a thorough introduction to C++ and how to use it to write non-trivial and robust applications in Quantitative Finance. Some special features of the book are:

- A full discussion of C++ syntax (as described in Stroustrup, 1997)
- Advanced topics in C++: memory management, exceptions, templates and RTTI
- An introduction to data structures and Complexity Analysis
- The Standard Template Library (STL) and its applications to Quantitative Finance
- Introduction to Design Patterns and integration into Quantitative Finance applications
- Creating real applications for derivative pricing
- **Working** source code for all chapters and applications
- Exercises for every chapter

After having read this book, studied the code and done the exercises you will be in a position to appreciate how to use C++ for Quantitative Finance.

## 0.2 WHY HAS THIS BOOK BEEN WRITTEN?

We have written this book for a number of reasons. First, in our opinion there are very few books on C++ that teach the language and apply it to interesting and non-trivial problems in Quantitative Finance. This book assumes no knowledge of C++ nor do we assume that the reader is conversant with the C programming language. The first ten chapters of the book introduce the major syntax elements that you will need in order to write C++ applications.

The second reason was to show how to apply C++ to writing flexible and robust applications using an appropriate combination of the object, generic and functional programming models. Furthermore, we apply design patterns and established frameworks to help create extendible applications.

Finally, seeing that C++ is an important language in the financial world we have included exercises, questions and projects at the end of each chapter. We advise the reader to answer these questions and implement the exercises and projects because the best way to learn C++ is by doing it. It is our feeling (and hope) that you will then be able to face job interviews with confidence.

### 0.3 FOR WHOM IS THIS BOOK INTENDED?

We have written this book for quantitative analysts, designers and other professionals who are involved in developing front office and trading systems. The book is structured in such a way that both novice and experienced developers can use it to write applications in Quantitative Finance.

The book is also suitable for university students in finance, mathematics and other disciplines where C++ is used as the language for computation.

### 0.4 WHY SHOULD I READ THIS BOOK?

This is the first book (in our opinion) that attempts to give a complete overview of C++ and some of its applications to Quantitative Finance. We employ modern design and programming techniques to create flexible and robust software. Finally, we provide the reader with working source code in this book.

### 0.5 THE STRUCTURE OF THIS BOOK

The book is divided into four major sections with each section devoted to one major focus of attention. The sections are:

Part I: C++ Essential Skills

Part II: Data Structures, Templates and Patterns

Part III: Quantitative Finance Applications

Part IV: Background Information

Each part represents a level of C++ expertise. If you learn Part I you will receive a green belt, completing Part II entitles you to brown belt grade and if you learn the contents of Part III you may then call yourself a black belt.

An overview of the contents of this book is given in Chapter 21.

I would like to thank **Dr Joerg Kienitz** for his willingness to write a chapter in this book on the Monte Carlo method.

### 0.6 WHAT THIS BOOK DOES NOT COVER

This book is about C++ syntax and its applications to Quantitative Finance. It uses a number of concepts and techniques that are discussed elsewhere in more detail. Thus, this book is not:

- an introduction to Quantitative Finance (see Hull, 2006)
- an introduction to numerical methods (see Duffy, 2006)
- advanced C++ programming and Excel AddIn interfacing (see Duffy, 2004)



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## **0.7 MORE INFORMATION AND SUPPORT**

We will continue to support this book (as well as my other books) on the web sites [www.datasim.nl](http://www.datasim.nl) and [www.datasim-component.com](http://www.datasim-component.com). We also give both in-company and courses in this area.

The author can be contacted at [dduffy@datasim.nl](mailto:dduffy@datasim.nl). I welcome your feedback and suggestions for improvement.

Good luck with C++ and Finance.