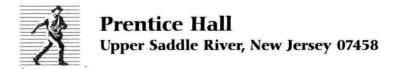


# STATISTICS Tools for Understanding Data

### Tools for Understanding Data in the Behavioral Sciences

Eva D. Vaughan

**University of Pittsburgh** 



#### Library of Congress Cataloging-in-Publication Data

Vaughan, Eva D.

Statistics: tools for understanding data in the behavioral sciences / Eva D. Vaughan.

p. cm

Includes bibliographical references and index. ISBN 0-02-422733-1

1. Social sciences—Statistical methods.

I. Title.

HA29.V33 1998

97-23655

300'.1'5195—dc21

CIP

Editor-in-Chief: Nancy Roberts Acquisitions Editor: Jennifer Gilliland Editorial Assistant: Tamsen Adams

Director of Production and Manufacturing: Barbara Kittle

Managing Editor: Bonnie Biller Production Liaison: Fran Russello Project Manager: Linda B. Pawelchak Manufacturing Manager: Nick Sklitsis

Prepress and Manufacturing Buyer: Tricia Kenny

Creative Design Director: Leslie Osher Interior and Cover Designs: Levavi & Levavi

Cover Art: Shadows/© Peter B. Kaplan, 1982 NYC.

Electronic Art Creation: Levavi & Levavi Marketing Manager: Mike Alread Copy Editing: Mary Louise Byrd

Proofreading: Maine Proofreading Services

This book was set in 10/12 Times Roman by Pub-Set, Inc., and was printed and bound by Courier Companies, Inc. The cover was printed by The Lehigh Press, Inc.



© 1998 by Prentice-Hall, Inc. Simon & Schuster/A Viacom Company Upper Saddle River, New Jersey 07458

All rights reserved. No part of this book may be reproduced, in any form or by any means, without permission in writing from the publisher.

Printed in the United States of America 10 9 8 7 6 5 4 3 2 1

ISBN 0-02-422733-1

Prentice-Hall International (UK), London
Prentice-Hall of Australia Pty. Limited, Sydney
Prentice-Hall Canada Inc., Toronto
Prentice-Hall Hispanoamericana, S. A., Mexico
Prentice-Hall of India Private Limited, New Delhi
Prentice-Hall of Japan, Inc., Tokyo
Simon & Schuster Asia Pte. Ltd., Singapore
Editora Prentice-Hall do Brasil, Ltda., Rio de Janeiro

## Dedicated to my granddaughter, Yuriko May she always be as eager to learn new things as she is now

### **Preface**

Some years ago, I was asked to teach an introductory statistics class for a distance-education program. Most students in the class would have no face-to-face contact with me or other students. They would work with the course materials at their own pace, mail required exercises or homework assignments to me, and take exams, when ready to do so, at designated "testing centers." Obviously, the students would need to rely entirely on their textbook and adjunct printed materials. As I examined possible textbooks, I realized that few, if any, could be used as stand-alone learning materials. This is understandable since statistics courses typically include lectures and other class activities to augment and reinforce the text. I had two alternatives: Choose a published textbook and prepare an extensive set of supplementary learning aids or write a stand-alone book. I chose the latter course.

Earlier versions of the material in this book have been used not only in distance-education settings but also in traditional courses that meet with an instructor for 3 to 4 hours a week. The responses in both settings have been highly favorable, and both students and instructors have asked me, "Why don't you publish this as a textbook?" I finally took their advice, and the book you have in front of you is the result.

Features of this book that support student learning, whether alone or in a class, include the following:

- Objectives at the start of each chapter so that students know what they will be learning and why it is important.
- A conversational writing style to make students feel as though I am speaking to them (many of my students have commented positively on this feature).
- Repeated explanations, stated in several different ways whenever possible, of difficult concepts.
- Many examples illustrating new ideas and procedures.
- Within-chapter exercises, usually seven or more per chapter, that allow students to check their comprehension of relatively small chunks of new information before going on to the next section.
- An appendix containing worked-out answers to all within-chapter exercises. Students are able to determine whether their answers are correct, and, for incorrect answers, what they did wrong.
- End-of-chapter summaries.

In many ways, the sequence of topics in this book is like that of most introductory statistics textbooks. Perhaps the most marked departure is that the theory and practice of hypothesis testing are introduced earlier than usual (in Chapter 5), using the chi square test rather than the z test for a population mean. The reasons for this choice are that (1) frequencies in categories are more familiar to students than means and standard deviations; (2) the rationale of the test is relatively easy to understand; (3) chi square tests always use one tail of the distribution (the rather difficult concept of one-tailed versus two-tailed tests can be deferred until later, after students have mastered the logic of hypothesis testing); and (4) in practice, chi square tests are used far more often than z tests.

I have found this sequence to be very successful. However, instructors who prefer a more traditional sequence can proceed directly from Chapter 4 to Chapter 6. The z test is introduced near the end of Chapter 6. Students can be asked to read the first part of Chapter 5 just before reading about the z test. The rest of Chapter 5 can be left for later in the course.

Another feature that is, I believe, unique in this book is the inclusion of a final chapter, Chapter 15, Connections, which attempts to integrate material taught throughout the previous 14 chapters and to relate that material to other topics in statistics (e.g., meta-analysis) and beyond statistics (e.g., steps in the research process). I hope that instructors will have time to assign Chapter 15 and will find it useful. I would be especially interested in feedback from both instructors and students regarding this chapter.

Throughout the book, I have attempted to follow a piece of advice attributed to Albert Einstein: "Everything should be made as simple as possible, but not simpler." Yes, material should be presented in ways that make learning as easy as possible. But difficult concepts—and there are many of them in statistics—should not be "dumbed down." I believe that most students *can* learn statistics, even the hard stuff, if they put forth the necessary effort and if that effort is supported by a user-friendly textbook. And that is what this book is intended to be.

Many people have contributed to the writing of this textbook. I am especially grateful to the many students who have used these materials, most of them in a distance-learning setting. They have provided me not only with useful suggestions but also the motivation to persist in the task of reworking the materials into a publishable textbook. I owe a great debt, too, to my family for their patience and support. I am sure there were days when my husband wondered whether I still lived in the same house as he did. My friends, too, must have gotten tired of hearing me say, "Sorry, I can't do so-and-so. I have to work on the book." Many thanks to them for understanding.

Thanks, also, to the reviewers who carefully scrutinized early drafts: Barney Beins, Ithaca College; James Chumbley, University of Massachusetts; Susan Donaldson, University of Southern Indiana; Jack Kirshenbaum, Fullerton Community College; Linda Noble, Kennesaw State College; Carol Pandey, L.A. Pierce College; Toni Wegner, University of Virgina; and Patrick Williams, University of Houston. Their comments and criticisms have made this a better book. Any errors that remain are my own.

Lynn Cooper of the University External Studies Program at the University of Pittsburgh has done a great job preparing the manuscript to send to the publisher. Without her skills the job would have been impossible. Finally, let me acknowledge the assistance of Bill Webber, Jennifer Gilliland, and Linda Pawelchak of Prentice Hall. It has been a pleasure working with all of them.

### Contents

List of Figures		xvi
List of Tables		XX
Preface		xxiii
1 Basic Concepts: Variables, Measurement, and Resear	ch	1
INTRODUCTION	1	
OBJECTIVES	1	
WHAT IS STATISTICS?	2	
THE USE OF CALCULATORS AND COMPUTERS		
IN STATISTICAL ANALYSIS	3	
Exercise 1–1	4	
SOME BASIC CONCEPTS	4	
Variability	5	
Descriptive and Inferential Statistics	5	
Types of Variables	6 7	
The Measurement of Variables  Exercise 1–2	10	
MORE ABOUT RESEARCH QUESTIONS AND HOW THEY ARE ANSWERED		
Questions About One Variable in One Population	10	
Questions About the Relations Between Two or More Variables	10	
in One Population	11	
Questions About Differences Between Two or More Populations	11	
Exercise 1–3	13	
SUMMARY	13	
QUESTIONS	14	
2 Displaying Distributions in Tables and Graphs		17
INTRODUCTION	17	
OBJECTIVES	17	
TABULATING AND GRAPHING CATEGORICAL DATA	18	
One Variable Measured in One Group	18	
Exercise 2–1	20	
Comparing Two or More Distributions: Contingency Tables	21	
Exercise 2–2	23	
FREQUENCY DISTRIBUTIONS FOR QUANTITATIVE DATA	23	
Grouped Frequency Distributions	24	
Exercise 2–3	26	

vi CONTENTS	
-------------	--

Score Limits and Exact Limits	27	
The Midpoint of a Class Interval	27	
Exercise 2–4	28	
Cumulative Frequencies and Cumulative Percentages	28	
Exercise 2–5	29	
GRAPHS OF QUANTITATIVE DATA	30	
Bar Graphs for Discrete Variables	30	
The Histogram	31	
Exercise 2–6	32	
The Frequency Polygon	32	
Exercise 2–7	33	
Stem-and-Leaf Plots	34	
Exercise 2–8	35	
Displaying Two or More Distributions in One Graph	35	
Exercise 2–9	37	
Cumulative Graphs	37	
Exercise 2–10	38	
DIFFERENT KINDS AND SHAPES OF DISTRIBUTIONS	38	
Theoretical and Obtained Distributions	39	
Areas Under a Curve	39	
Exercise 2–11	40	
LOCATING SCORES WITHIN A DISTRIBUTION: PERCENTILES		
AND PERCENTILE RANKS	41	
Calculating and Interpreting Percentile Ranks	41	
Exercise 2–12	43	
Calculating Percentiles	43	
Percentiles, Quartiles, and Skew	44	
Exercise 2–13	46	
Box-and-Whisker Plots	47	
Exercise 2–14	48	
DATA FILES AND COMPUTER GRAPHS	49	
SUMMARY	51	
QUESTIONS	51	
QUESTIONS	31	
3 Measures of Central Tendency and Variability		54
INTRODUCTION	54	
OBJECTIVES	54	
WHY DO WE NEED MEASURES OF CENTRAL TENDENCY		
AND VARIABILITY?	55	
Exercise 3–1	58	
MEASURES OF CENTRAL TENDENCY	58	
The Mode	58	
The Median	59	
Exercise 3–2	61	
The Mean	62	
Exercise 3–3	64	
Comparison of the Mean, Median, and Mode as Measures of Central Tendency	64	
Exercise 3–4	67	
	· .	

	CONTENTS	vii
MEASURES OF VARIABILITY	68	
The Range	68	
The Interquartile and Semi-Interquartile Range	68	
Exercise 3–5	71	
The Variance and the Standard Deviation	72	
Exercise 3–6	75	
Exercise 3–7	77	
LINEAR TRANSFORMATIONS AND STANDARD SCORES	78	
The Effect of Linear Transformations on the Mean, Variance,		
and Standard Deviation	78	
Exercise 3–8	80	
The Standard Deviation as a Measure of Distance: Standard Scores	80	
Exercise 3–9	84	
USING A COMPUTER TO DESCRIBE A DATA SET	84	
SUMMARY	85	
QUESTIONS	86	
4 Sampling and Probability		88
INTRODUCTION	88	
OBJECTIVES	88	
SAMPLING AND SAMPLING DISTRIBUTIONS	89	
Populations and Samples	89	
Statistics and Parameters	91	
Exercise 4–1	91	
Sampling Variability and Sampling Distributions	92	
Exercise 4–2	102	
PROBABILITY	102	
Two Definitions of Probability	102	
Exercise 4–3	104	
The Addition and Multiplication Laws of Probability	104	
Exercise 4–4	106	
Sampling With and Without Replacement	106	
Exercise 4–5	108	
Probability Distributions	108	
Exercise 4–6	112	
The Binomial Distribution	112	
Exercise 4–7	116	
An Introduction to Continuous Probability Distributions	116	
Exercise 4–8	118	
Sampling Distributions and Probability Distributions	118	
SUMMARY	119	
QUESTIONS	119	
5 An Introduction to Hypothesis Testing: The Chi Square Test		122
INTRODUCTION	122	
OBJECTIVES	123	

### viii CONTENTS

WHAT IS HYPOTHESIS TESTING ALL ABOUT?	123	
Why Do We Need to Test Hypotheses?	123	
General Procedure for Hypothesis Testing	124	
Exercise 5–1	125	
Differences Between Statistical and Real-Life Hypothesis Testing	125	
Recapitulation: General Procedure in Statistical Hypothesis Testing	126	
Exercise 5–2	127	
INTRODUCTION TO THE CHI SQUARE TEST	127	
Rationale: Comparing Observed and Expected Frequencies	127	
Exercise 5–3	129	
The Chi Square Distribution	130	
Exercise 5–4	133	
THE CHI SQUARE TEST OF GOODNESS OF FIT	133	
Part 1: Testing Hypotheses About Theoretical Distributions	133	
Exercise 5–5	135	
Part 2: Testing the Null Hypothesis	135	
Exercise 5–6	137	
THE CHI SQUARE TEST OF INDEPENDENCE	137	
Contingency Tables	138	
Exercise 5–7	139	
Procedures in the Chi Square Test of Independence	139	
Recapitulation: Chi Square Test of Independence	141	
Exercise 5–8	142	
SCOPE AND LIMITATIONS OF THE CHI SQUARE TEST	142	
Independence of Observations	143	
Small Expected Frequencies	143	
Random Sampling	145	
Exercise 5–9	145	
AN INTRODUCTION TO ERRORS OF INFERENCE	146	
Exercise 5–10	147	
USING STATISTICAL SOFTWARE TO CONDUCT TESTS	148	
Exercise 5–11	148	
SUMMARY	148	
QUESTIONS	150	
( Dalations Detruces Counts and Denulation		
6 Relations Between Sample and Population Means and Variances		150
Means and variances		152
INTRODUCTION	152	
OBJECTIVES	152	
PARAMETERS AND STATISTICS	153	
Exercise 6–1	154	
THE RELATION BETWEEN POPULATION AND SAMPLE MEANS	154	
A Theoretical Sampling Distribution of the Mean	155	
Symbols and Terms for the Sampling Distribution of the Mean	158	
Exercise 6–2	158	
The Central Limit Theorem	159	
Exercise 6–3	162	
LALICIDE U-J	102	

	CONTENTS	ix
ESTIMATING THE VARIANCE OF A POPULATION	163	
Exercise 6–4	166	
AN INTRODUCTION TO COMPONENTS OF VARIANCE	166	
Exercise 6–5	168	
SUMMARY	168	
QUESTIONS	169	
7 The Normal Curve		171
INTRODUCTION	171	
OBJECTIVES	171	
INTRODUCTION TO THE NORMAL CURVE	172	
Properties of the Normal Curve	172	
The Standard Normal Curve	173	
Exercise 7–1	177	
SOME APPLICATIONS OF THE NORMAL CURVE	177	
Using the Normal Curve Table to Answer Questions About Normal Populations	178	
Exercise 7–2	180	
The Normal Approximation to the Binomial Distribution	181	
Exercise 7–3	183	
Using the Normal Curve to Answer Sampling and Probability Questions		
About Sample Means	183	
Exercise 7–4	185	
A RETURN TO HYPOTHESIS TESTING: THE NORMAL CURVE TEST	185	
Review of Steps in Hypothesis Testing	185	
Rationale and Assumptions of the Normal Curve Test	187	
One-Tailed and Two-Tailed Tests	189	
Exercise 7–5	193	
Exercise 7–6	198	
Some Final Comments About Normal Curve Tests	198	
SUMMARY	199	
QUESTIONS	200	
8 Using the t Distribution to Make Inferences About a Population Mean		202
About a ropulation Mean		202
INTRODUCTION	202	
OBJECTIVES	202	
INTRODUCTION TO THE t DISTRIBUTION	203	
Calculating the Estimated Standard Error of the Mean	203	
Exercise 8–1	204	
Comparison of the t Distribution and the Standard Normal Curve	205	
Exercise 8–2	207	
A Historical Note	207	
Addendum	207	
Using the Table of the t Distribution	208	
Exercise 8–3	209	

•	CONTENT	TC

CONDUCTING THE t TEST	209	
Exercise 8–4	211	
ESTIMATING THE POPULATION MEAN: CONFIDENCE INTERVALS	211	
Rationale and Computation of Confidence Intervals	212	
Interpretation of Confidence Intervals	214	
Exercise 8–5	215	
Factors Affecting the Width of Confidence Intervals	215	
Relation Between Interval Estimation and Hypothesis Testing	217	
Exercise 8–6	218	
CONFIDENCE INTERVALS FOR POPULATION PERCENTAGES	218	
Exercise 8–7	220	
ERRORS OF INFERENCE	220	
Type I and Type II Errors	220	
Factors Affecting the Probability of Type I and Type II Errors	222	
Choosing a Level of Alpha	223	
Exercise 8–8	224	
THE POWER OF A TEST	225	
Factors Affecting the Power of a Test	225	
Exercise 8–9	227	
POSTSCRIPTS	228	
Postscript 1: Some Common Errors in Interpretation	228	
Postscript 2: Parametric and Nonparametric Statistical Tests	228	
HIGHER A COMPUMED TO COMPUTE TERMS AND CALCULATE		
USING A COMPUTER TO CONDUCT t TESTS AND CALCULATE		
CONFIDENCE INTERVALS	229	
CONFIDENCE INTERVALS	229 230	
CONFIDENCE INTERVALS SUMMARY QUESTIONS		
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships	230	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables	230 231	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables INTRODUCTION	230 231	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES	230 231 233 233	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS	230 231 233 233 234	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation	230 231 233 233 234 234	naki pierwita wi
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1	230 231 233 233 234 234 239	nakelenojeni
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations	230 231 233 233 234 234 239 239	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2	230 231 233 233 234 234 239 239 242	nakeamoigna
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION	230 231 233 233 234 234 239 239 242 242	nadpote revision i
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance	230 231 233 233 234 234 239 239 242 242 242	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient	230 231 233 233 234 234 239 239 242 242 242 242	and other company
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9–3	230 231 233 233 234 234 239 239 242 242 242 244 247	ina kata manjana
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9–3 EXERCISE 9–4	230 231 233 233 234 234 239 239 242 242 242 244 247 249	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9–3 EXERCISE 9–4 INTERPRETING CORRELATION COEFFICIENTS	230 231 233 233 234 234 239 239 242 242 242 242 244 247 249 250	inak de Assiens
SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9–3 EXERCISE 9–4 INTERPRETING CORRELATION COEFFICIENTS What Is a "High" Correlation?	230 231 233 233 234 234 239 239 242 242 242 242 244 247 249 250 250	najest stillen
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9–1 The Strength of Correlations EXERCISE 9–2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9–3 EXERCISE 9–4 INTERPRETING CORRELATION COEFFICIENTS What Is a "High" Correlation? Factors Affecting the Correlation Coefficient	230 231 233 233 234 239 239 242 242 242 242 244 247 249 250 250 250	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9-1 The Strength of Correlations EXERCISE 9-2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9-3 EXERCISE 9-4 INTERPRETING CORRELATION COEFFICIENTS What Is a "High" Correlation? Factors Affecting the Correlation Coefficient EXERCISE 9-5	230 231 233 233 234 239 239 242 242 242 244 247 249 250 250 250 255	interference of
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9-1 The Strength of Correlations EXERCISE 9-2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9-3 EXERCISE 9-4 INTERPRETING CORRELATION COEFFICIENTS What Is a "High" Correlation? Factors Affecting the Correlation Coefficient EXERCISE 9-5 Correlation and Causal Relationship	230 231 233 233 234 239 239 242 242 242 244 247 249 250 250 250 255 255	
CONFIDENCE INTERVALS SUMMARY QUESTIONS  9 Correlation: Measuring Relationships Between Variables  INTRODUCTION OBJECTIVES BASIC CONCEPTS The Meaning of Correlation EXERCISE 9-1 The Strength of Correlations EXERCISE 9-2 MEASURING COVARIATION The Covariance The Pearson Correlation Coefficient EXERCISE 9-3 EXERCISE 9-4 INTERPRETING CORRELATION COEFFICIENTS What Is a "High" Correlation? Factors Affecting the Correlation Coefficient EXERCISE 9-5	230 231 233 233 234 239 239 242 242 242 244 247 249 250 250 250 255	

	CONTENTS	хi
DRAWING CONCLUSIONS ABOUT POPULATION CORRELATION		
COEFFICIENTS FROM SAMPLE DATA	258	
The Sampling Distribution of the Correlation Coefficient	258	
Testing Hypotheses About Population Correlation Coefficients	259	
Exercise 9–7	261	
Exercise 9–8	263	
OTHER TYPES OF CORRELATION COEFFICIENTS	264	
The Spearman Rank-Order Correlation Coefficient	264	
The Point Biserial Correlation Coefficient	265	
The Phi Coefficient	267	
Tests of Significance	268	
Exercise 9–9	269	
SUMMARY	270	
QUESTIONS	271	
QUESTIONS	2/1	
10 Analyzing Correlational Data: Linear Regression		274
INTRODUCTION	274	
OBJECTIVES	274	
THE REGRESSION EQUATION AND ITS PROPERTIES	275	
General Form of the Regression Equation	275	
Exercise 10–1	276	
A Graphic Approach to Regression: The Regression Line	277	
Calculating the Slope and the Y-Intercept of the Regression Equation	280	
Exercise 10–2	283	
Some Facts About Regression	284	
Exercise 10–3	289	
MEASURING VARIABILITY AROUND THE REGRESSION LINE	289	
The Residual Variance and the Standard Error of Estimate	291	
Exercise 10–4	293	
A Return to Components of Variance	293	
Alternative Formulas for the Residual Variance and the Standard		
Error of Estimate	295	
Exercise 10-5	296	
GOING BEYOND SAMPLE REGRESSION: MAKING PREDICTIONS		
IN THE POPULATION	296	
The Relation Between Sample and Population Regression Analyses	296	
Calculating Prediction Intervals for Criterion Scores	299	
Exercise 10–6	300	
Another Example of Regression	301	
A Comparison of Predictions With and Without the Use of Regression	302	
A Few Cautionary Notes: When Not to Use Regression Analyses	303	
A NONTECHNICAL INTRODUCTION TO MULTIPLE REGRESSION	304	
Factors That Influence the Multiple Regression Equation	305	
The Multiple Correlation Coefficient	306	
Measuring Errors of Prediction in Multiple Regression	307	
Exercise 10–7	307	
USING A COMPUTER TO CONDUCT A REGRESSION ANALYSIS	307	

xii	CONTENTS
-----	----------

SUMMARY QUESTIONS	309 310	
11 Making Inferences About Differences Between Population Means		312
INTRODUCTION	312	
OBJECTIVES	312	
THE RESEARCH CONTEXT	313	
Independent Sample Designs	314	
Correlated Sample Designs	315	
Exercise 11–1	319	
THE t TEST FOR THE DIFFERENCE BETWEEN MEANS	319	
The Sampling Distribution of the Difference Between Means	320	
Exercise 11–2	324	
Rationale of the t Test	325	
Exercise 11–3	328	
The t Test for the Difference Between Means of Independent Samples	328	
Exercise 11–4	332	
Exercise 11–5	335	
The t Test for the Difference Between Means of Correlated Samples	335	
Exercise 11–6	340	
Postscript: Drawing Conclusions From t Tests in Experimental		
and Nonexperimental Research	340	
ESTIMATING THE DIFFERENCE BETWEEN TWO POPULATION		
MEANS-CONFIDENCE INTERVALS	341	
Exercise 11–7	343	
POWER, ROBUSTNESS, AND THE STRENGTH OF RELATIONSHIPS	343	
The Power of the t Test	343	
Measuring the Strength of the Relation Between the Independent		
and Dependent Variables	345	
Exercise 11–8	346	
The Assumptions Underlying the t Test and the Robustness of the Test	347	
SUMMARY	347	
QUESTIONS	348	
12 Simple or One-Way Analysis of Variance		352
INTRODUCTION	352	
OBJECTIVES	352	
RATIONALE OF THE ANALYSIS OF VARIANCE	353	
The Case Against Multiple t Tests	353	
The Rationale of ANOVA	354	
Exercise 12–1	356	
RATIONALE AND STEPS OF THE ANOVA	356	
Partitioning the Total Variation of a Data Set	356	
Exercise 12–2	360	
Mean Squares and Degrees of Freedom	360	
Exercise 12–3	363	

	CONTENTS	xiii
Comparing MS Between and MS Within: The F Test	363	
Summary of Reasoning and Procedure in the One-Way ANOVA	366	
Exercise 12–4	367	
Displaying the Results of an ANOVA: Summary Tables	367	
Exercise 12–5	369	
COMPUTATIONAL PROCEDURES	369	
Conducting One-Way ANOVA by Computer	369	
Computational Formulas for Manual Calculation	369	
Exercise 12–6	371	
Another Example of One-Way ANOVA	371	
Exercise 12–7	373	
THE RELATIONSHIP BETWEEN ANOVA AND THE $t$ TEST	374	
Exercise 12–8	376	
POWER, ROBUSTNESS, AND STRENGTH OF RELATIONS	377	
The Power of the ANOVA	377	
Exercise 12–9	377	
Measuring the Strength of the Relationship Between the Independent		
and Dependent Variables	378	
The Robustness of the ANOVA	379	
Exercise 12–10	379	
MULTIPLE COMPARISONS	380	
Introduction	380	
Subhypotheses and Weights Assigned to Sample Means	380	
Orthogonal and Nonorthogonal Comparisons	382	
Exercise 12–11	384	
Tests for Planned Comparisons	384	
Exercise 12–12	386	
Post Hoc Tests	386	
Exercise 12–13	388	
Exercise 12–14	392	
SUMMARY	392	
QUESTIONS	393	
13 Analyses of Variance for Factorial Designs		
and Repeated Measures		396
INTRODUCTION	396	
OBJECTIVES	396	
TWO-WAY ANALYSIS OF VARIANCE	397	
Constructing a Factorial Design	397	
Exercise 13–1	398	
Rationale of the Two-Way ANOVA	398	
Exercise 13–2	401	
Conducting the Analysis	402	
Exercise 13–3	407	
Exercise 13–4	411	
Exercise 13–5	413	
Assumptions, Power, and Strength of Relationships	414	
Exercise 13–6	415	

_	
viv	CONTENTS

Multiple Comparisons in Two-Way ANOVA		
Exercise 13–7		
ANALYSIS OF VARIANCE FOR REPEATED MEASURES		
Hypotheses and Assumptions		
Exercise 13–8	422	
Computational Procedures	423	
Exercise 13–9	425	
Relation Between the Repeated Measures ANOVA and the t Test		
for Correlated Samples	425	
Comparison of One-Way and Repeated Measures ANOVA	427	
Exercise 13–10	430	
Multiple Comparisons in the Repeated Measures Design	430	
Exercise 13–11	432	
OTHER ANALYSES OF VARIANCE—AN INTRODUCTION	432	
SUMMARY	433	
QUESTIONS	434	
14 Some Nonparametric/Distribution-Free Tests		437
INTRODUCTION	437	PRINTED AND THE PRINTED AND TH
OBJECTIVES	437	
INTRODUCTION TO NONPARAMETRIC TESTS	438	
FOUR REPRESENTATIVE TESTS FOR RANKS	439	
The Mann-Whitney U Test	439	
Exercise 14–1	442	
The Wilcoxon Matched-Pairs Signed-Ranks Test	442	
Exercise 14–2	444	
The Kruskal-Wallis H Test	444	
Exercise 14–3	446	
The Friedman Analysis of Variance by Ranks	446	
Exercise 14–4	448	
THE RELATIVE POWER OF PARAMETRIC AND NONPARAMETRIC TESTS	448	
Exercise 14–5	449	
SUMMARY	450	
QUESTIONS	451	
15 Connections		453
INTRODUCTION	453	
OBJECTIVES	454	
CHOOSING AN APPROPRIATE PROCEDURE OR TEST	454	
Questions About the Distribution of One Variable in One Group of Individuals	455	
Questions About Relations Between Two or More Variables Measured		
in One Group	457	
Questions About Differences Between Two or More Groups or Under Two	(KING), 1484	
or More Experimental Conditions	460	
Keywords	463	
Exercise 15–1	465	
COMMON THEMES	465	

	CONTENTS	XV	
The Logic of Hypothesis Testing (Again) and a New Look			
at the Test Statistic	464		
Exercise 15–2	466		
Components of Variance (Again)	467		
Exercise 15–3	468		
An Introduction to the General Linear Model	468 470		
THE ROLE OF STATISTICS IN THE RESEARCH PROCESS			
Steps in the Research Process	471		
The Role of Statistics	478		
Exercise 15–4	479		
ANALYZING ANALYSES: META-ANALYSIS	479		
Exercise 15–5	481		
SUMMARY	481		
QUESTIONS	482		
A FINAL WORD	484		
References		485	
Glossary			
Appendix A: Arithmetic and Algebra Self–Evaluation Quiz Appendix B: Review of Arithmetic and Algebra			
Appendix D: Tables		555	
Index		569	