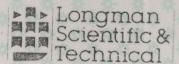
Nuclear Magnetic Resonance Spectroscopy

A Physicochemical View

Robin K Harris

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Preface to the revised reprint

Reprinting this book provides an opportunity to correct typographical errors, to carry out some small cosmetic improvements to the presentation and to make a few additional changes. I have attempted, for instance, to clarify the difference between the frequency of the electromagnetic radiation and its strength as indicated by the precession it induces in the magnetization. The symbol ω_1 is retained for the former and Ω_1 (= γB_1) introduced for the latter. New sections have been added to Chapters 6 and 7 in recognition of the growing importance of NMR work on solids and of 2-D NMR techniques. Furthermore, an increased emphasis has been placed on the tensor nature of NMR interactions by minor changes in the text and, more importantly, by the addition of a new Appendix.

It is hoped that these changes are welcomed and that publication in paperback form enables the book to reach a wider readership, particularly among graduate students.

Since the original book was published, I have moved to a different University. I take this opportunity to thank my former colleagues at the University of East Anglia for assisting greatly in my continued chemical education over the past 20 years. I also wish to thank G. A. Morris for helpful discussion of Chapter 7.

University of Durham, January 1986

Robin Harris

Preface

Nuclear magnetic resonance spectroscopy has occupied an important place in the armoury of physical techniques available to the chemist for over 25 years. Indeed, it is arguable that it is the single most important tool for obtaining detailed information on chemical systems at the molecular level. In spite of the high cost of NMR spectrometers no moderately-sized chemical laboratory, whether industrial or academic, can be considered to be properly-equipped without at least one such instrument. No university undergraduate chemistry course is complete without a discussion of the basic principles of NMR. The subject has proved to be remarkable for the number of innovations that have appeared and become established as valuable additions. Thus, in the early 1970s the use of high-resolution techniques based on the Fourier transform (FT) principle profoundly modified the practice of NMR and provided a quantum jump in the amount of information accessible by NMR. The FT mode also ushered in an era in which an increasing number of spectrometer operations are computer-controlled, leading also to the ability both to perform new experiments and to enhance the quality of the results. The past five or six years have seen several additional 'quantum jumps' in NMR, for instance (a) multinuclear studies, (b) very-high-field operation, (c) high-resolution work on solids, (d) 'two-dimensional' operation, and (e) spin imaging. These advances owe much to the ever-increasing variety of pulse sequences which can be implemented.

It is clear that many of these advances must be incorporated into undergraduate and graduate teaching. In 1969 Dr Ruth Lynden-Bell and I wrote a book entitled *Nuclear Magnetic Resonance Spectroscopy* (published by Thomas Nelson & Sons Ltd, but now out of print) which took a physicochemical approach to such teaching. Although very little in that book has become outmoded, the material is now wholly inadequate for a proper view of NMR—the FT technique, for instance, was not mentioned. The aim of the present work is to provide an updated text based on the same philosophy of a physicochemical approach. Material from the earlier book has been incorporated (with modifications), particularly in Chapters 1, 2 and 8, but the total amount of text has roughly doubled, since much has been added. The

new book is intended to cover NMR adequately for students taking Bachelor's and Master's degrees in chemistry, and should also be valuable in Ph.D. work and for people involved in NMR to a greater or lesser extent in industrial and Government laboratories.

It is, perhaps, obvious that considerable difficulty was encountered in deciding which topics to include and which to exclude. The choice is, to some extent, personal, but the policy has been to avoid mention of topics at a trivial level, such as would have been necessary to keep the size of the book within reasonable bounds if all the conceivably relevant areas were to be mentioned. Therefore several topics have been totally omitted. The principal among these are (a) NMR in liquid crystals and liquid crystal solutions. (b) spin imaging and related topics. and (c) chemically-induced dynamic nuclear polarization. These areas are self-contained and may be considered somewhat away from mainstream chemical usage of NMR. Specifically biochemical applications of NMR have also been largely omitted, in spite of their importance. mainly because it is difficult to develop such aspects without extensive discussion of strictly biochemical principles. Some will doubtless be critical of these decisions, but I defy anyone to produce a set of topics for a book of this size which would not arouse similar criticisms! Some texts on the omitted topics are listed under 'Further reading' at the end of this book (p. 241).

Problems are also encountered in deciding the level of mathematical sophistication used. I have tried to combine a degree of rigour with a desire both to give a physically-meaningful description of NMR behaviour and to minimize the amount of mathematics that is needed. A deliberate decision was taken not to introduce density matrix formalism, in spite of its power. Throughout the book SI units and equations are used. The form of relaxation equations may on occasion seem unfamiliar because of the factors of $(\mu_0/4\pi)$, and many scientists still apparently find Gauss rather than Tesla come first to mind for units of magnetic field, but these problems are not usually of great significance. I believe familiarity with SI is now such that a more detailed discussion of units is not required, but readers should refer if necessary to the booklet by M. L. McGlashan entitled Physico-Chemical Quantities and Units (Royal Society of Chemistry Monographs for Teachers, Number 15, 1968). Lists of SI units and of fundamental constants, in tabular form, follow this preface. IUPAC recommendations for NMR have been used throughout the book (see Pure Appl. Chem., 29, 627 (1972) and 45, 219 (1976)).

Chapters 1, 2 and 8 cover roughly the same ground as in the corresponding chapters of the earlier book. Chapter 1 is, indeed, a self-contained discussion of the simpler basic principles of NMR, as involved in the continuous wave (CW) mode of operation, and is intended for beginners of the subject. Chapter 2 discusses second-order spectral analysis, and it is largely possible for the student to omit detailed reading of this Chapter if it is not directly relevant to his or

her interests. Chapter 3 is largely new, and introduces the Fourier transform principle, together with the concept of relaxation. Chapter 4 continues the discussion of relaxation but concentrates on the dipolar interaction and on double resonance. The fifth chapter covers chemical exchange and the effects arising from quadrupolar interactions, in a form greatly expanded from the earlier book. Chapters 6 and 7 are entirely new. The former deals with NMR of solids, including the high-resolution techniques that are now finding increasing application. The latter discusses a number of special pulse sequences and develops the concepts of two-dimensional NMR. The final chapter is about the factors affecting chemical shifts and coupling constants. Problems are provided at the end of each chapter. A limited number of references, together with suggestions for further reading, are also included.

It is hoped that the whole volume provides a basis of understanding of NMR that will be valuable for chemists of many complexions, but particularly for those who value a physicochemical approach.

University of East Anglia 5 April 1982

Robin Harris

Acknowledgements

I am very grateful to Dr Ruth M. Lynden-Bell who joined me in writing a book on NMR in 1969. In particular, Chapter 2 of that book. which was written by Dr Lynden-Bell, has become, with modifications. Chapter 2 of the present book. Dr Lynden-Bell has also kindly read and commented on the present Chapter 3. I am also grateful to my colleagues Professors Norman Sheppard and Ken Packer who have, over the years, been the source of countless stimulating discussions of NMR. The work of many graduate students and other research workers at the University of East Anglia has also contributed to my enlightenment and has provided a number of the figures in the present book. Dr G. A. Webb has made some useful comments on Chapter 8 at galley-proof stage, which have resulted in improvements, and I thank him for his help. I would also like to thank Dr A. J. Jones of the National NMR Centre, the Australian National University, with whom I spent two months of sabbatical leave in 1981 during which the writing of this book was commenced. Some figures have been taken from the literature, and acknowledgements are given in the appropriate figure captions. A number of people have assisted with typing this book, but the largest share has been carried out by Mrs Janice Hancock, whom I would like to thank for all her work.

List of SI units and related quantities

Property	Symbol	SI unit	Symbol of unit	Equivalent SI units	Equivalents in other systems
Length	ℓ, r	metre	m	-	10 ² centimetres
Mass	m	kilogramme	kg	_	10 ³ grammes
Time	t	second	s	_	~
Force	\boldsymbol{F}	newton	N	$kg m s^{-2}$	10 ⁷ dynes
Energy	\boldsymbol{U}	joule	J	$kg m^2 s^{-2}$	10 ⁷ ergs
Angle	θ	radian	rad	$1/2\pi$ cycles	_
Frequency	ν	hertz	Hz	_	1 cycle per second (c/s or cps)
Electric charge	q	coulomb	С	A s	2.9979×10^{9} e.s.u.
Electric current	i	ampere	Α	-	$10^{-1} e.m.u.$
Magnetic induction field	В	tesla	T	$kg s^{-2} A^{-1}$	10⁴ gauss (e.m.u.)
Magnetic field intensity	H	ampere metre ⁻¹	-	$m^{-1} A$	$4\pi \times 10^{-3}$ oersted
Magnetic dipole moment	μ	ampere metre ²	_	m ² A	$10^{3} \mathrm{e.m.u. sec^{-1}}$
Magnetogyric ratio	γ	radian tesla ⁻¹ second ⁻¹	_	rad kg ⁻¹ s A	10 ⁻⁴ rad gauss ⁻¹ sec ⁻¹
Reduced coupling constant	K	newton ampere ⁻² metre ⁻³	_	$kg m^{-2} s^{-2} A^{-2}$	10cm^{-3}

Fundamental constants(a)

			Unit		
Constant	Symbol	Value	SI	CGS	
Elementary charge	e	1.602192	×10 ⁻¹⁹ C	×10 ⁻²⁰ e.m.u.	
		4.80325	_	$\times 10^{-10}$ e.s.u.	
Electron rest mass	m _e	9.10956	$\times 10^{-31} \text{ kg}$	$\times 10^{-28}$ g	
Proton rest mass	m_{v}	1.67261	$\times 10^{-27} \text{ kg}$	$\times 10^{-24} \text{g}$	
Planck constant	h	6.62620	$\times 10^{-34}$ J s	$\times 10^{-27}$ erg s	
	$\hbar = h/2\pi$	1.054592	$\times 10^{-34} \text{J s}$	$\times 10^{-27}$ erg s	
Charge-to-mass ratio for electron	e/m _e	1.758803	$\times 10^{11} \mathrm{C kg^{-1}}$	$\times 10^7$ e.m.u.	
Permeability constant	$\mu_{ m o}$	4π	$\times 10^{-7} \text{ kg m s}^{-2} \text{ A}^{-2}$	<u>-</u>	
		1	_	×1 e.m.u.	
Free electron Landé splitting factor	g _s	2.00232	-	_	
Magnetogyric ratio of proton	$\gamma_{\scriptscriptstyle p}$	2·675197 ^(b)	$\times 10^{8} \mathrm{rad} \mathrm{s}^{-1} \mathrm{T}^{-1}$	$\times 10^4$ rad s ⁻¹ gauss ⁻¹	
	$\gamma_{\rm p}/2\pi$	4·25771(b)	$\times 10^{7} \text{Hz} \text{T}^{-1}$	$\times 10^{3} \mathrm{s}^{-1} \mathrm{gauss}^{-1}$	
Bohr magneton	μ_{B}	9.27410	$\times 10^{-24} \mathrm{J}\mathrm{T}^{-1}$	$\times 10^{-21} \mathrm{erg \ gauss^{-1}}$	
Nuclear magneton	μ_N	5.05095	$\times 10^{-27} \mathrm{J}\mathrm{T}^{-1}$	$\times 10^{-24} \mathrm{erg gauss^{-1}}$	
Boltzmann constant	k	1.38062	$\times 10^{-23} \mathrm{J K^{-1}}$	$\times 10^{-16} \mathrm{erg} \mathrm{K}^{-1}$	
Avogadro constant	N	6.02217	$\times 10^{23} \mathrm{mole^{-1}}$	$\times 10^{23} \text{mole}^{-1}$	

⁽a) Taken from B. N. Taylor, W. H. Parker & D. N. Langenberg, Rev. Mod. Phys. 41, 375 (1969), but quoted to fewer places.

⁽b) Corrected for the diamagnetic shift of H₂O.

Symbols and abbreviations

These lists contain the symbols and abbreviations most frequently used in this book, but they are not expected to be exhaustive. Some specialized notation is only defined in the relevant chapter. An attempt has been made to standardize usage throughout the book as far as is feasible, but it must be borne in mind that the original research literature certainly is not standardized in this way, and some difficulties may arise from this fact. Trivial use of subscripts, etc. is not always mentioned in the symbols list below. Some of the other symbols used in the text, e.g. for physical constants such as h or π , or for thermodynamic quantities such as H or S, are not included in the list since they are reckoned to follow completely accepted usage. In general, vectors are in bold print, and quantum mechanical operators are indicated by circumflexes.

Symbols

- hyperfine (electron-nucleus) coupling constant
- **B** magnetic induction field (magnetic flux density)
- **B**₀ static magnetic field of an NMR spectrometer
- $\mathbf{B}_1, \mathbf{B}_2$ r.f. magnetic fields associated with ν_1, ν_2 .
 - \mathbf{B}_{L} local magnetic field (components B_{xL} , B_{yL} , B_{zL})—of random field or dipolar origin
 - c coefficient in linear expansion of wave functions
 - C spin-rotation interaction tensor
 - $C_{\rm x}$ (i) natural abundance of nuclide X, expressed as a %
 - (ii) spin-rotation coupling constant of nuclide X
 - **D** dipolar interaction tensor
 - D^C nuclear receptivity relative to that of carbon-13
 - D^p nuclear receptivity relative to that of the proton
 - E electric field
 - F spectral width
 - $\hat{\mathbf{F}}_X$ nuclear spin operator for a group, G, of nuclei (components \hat{F}_{Gx} , \hat{F}_{Gy} , \hat{F}_{Gz} , \hat{F}_{G+} , \hat{F}_{G-})
 - F_G magnetic quantum number associated with $\hat{\mathbf{F}}_G$
 - g nuclear or electronic g factor (Landé splitting factor)
 - H_{ii} element of matrix representation of $\hat{\mathcal{H}}$
 - $\hat{\mathcal{H}}$ Hamiltonian operator (in energy units)—subscripts indicate the nature of the operator
 - $i \sqrt{-1}$
 - $\hat{\mathbf{I}}_i$ nuclear spin operator for nucleus j (components \hat{I}_{jx} , \hat{I}_{jy} , \hat{I}_{jz})
- $\hat{I}_{j+}, \hat{I}_{j-}$ 'raising' and 'lowering' spin operators for nucleus j
 - I_i magnetic quantum number associated with $\hat{\mathbf{I}}_i$
 - I moment of inertia

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- munect coupling tensor
- ⁿJ nuclear spin-spin coupling constant through n bonds (in Hz). Further information may be given by subscripts or in brackets. Normally subscripts are only used for algebraic symbols for nuclei in spectral analysis cases, e.g. J_{AX} . Brackets are used for indicating the species of nuclei coupled, e.g. $J(^{13}C, ^{1}H)$ or, additionally, the coupling path, e.g. J(POCF)
- $J(\omega)$ spectral density at angular frequency ω
 - ⁿK reduced nuclear spin-spin coupling constant (see the notes concerning ⁿI)
 - m_a mass of the electron
 - m_i eigenvalue of \hat{I}_{iz} (magnetic component quantum number)
 - m_T total magnetic quantum number for a spin system (eigenvalue of $\sum_i \hat{I}_{iz}$)
- $m_{\tau}(X)$ total magnetic quantum number for X-type nuclei
 - \mathbf{M}_0 equilibrium macroscopic magnetization of a spin system in the presence of B_0
- $M_{\rm r}, M_{\rm o}, M_{\rm c}$ components of macroscopic magnetization
 - M_n moment of a spectrum (M_2 = second moment, etc.)
 - n_{α} , n_{β} populations of the α and β spin states
 - N total number of nuclei of a given type in the sample
 - P (i) angular momentum
 - (ii) transition probability
 - **q** electric field gradient tensor (principal components q_{xx} , q_{yy} , q_{zz})
 - O nuclear quadrupole moment
 - r (i) general symbol for distance
 - (ii) general symbol for spin state (as $\langle r | \text{ or } | r \rangle$)
 - R dipolar coupling constant, $(\mu_0/4\pi)\gamma_1\gamma_2(\hbar/2\pi)r^{-3}$
 - s general symbol for spin state (as (s| or |s))
 - S (i) signal height
 - (ii) electron (or, occasionally, nuclear) spin—cf. I
 - T temperature
 - T. coalescence temperature for an NMR 'spectrum
 - T_1^X spin-lattice relaxation time of the X nuclei (further subscripts refer to the relaxation mechanism)
 - T_2^X spin-spin relaxation time of the X nucleus (further subscripts refer to the relaxation mechanism)
 - T_2' inhomogeneity contribution to the dephasing time for M_x or M_y
 - T_2^* total dephasing time for M_r or M_v ; $(T_2^*)^{-1} = T_2^{-1} + (T_2')^{-1}$
 - $T_{1\rho}^{X}$ spin-lattice relaxation time of the X nuclei in the frame of reference rotating with B_1
 - $T_{\rm d}$ pulse delay time (in FT NMR)
 - $T_{\rm ac}$ acquisition time (in FT NMR)
 - $T_{\rm p}$ period for repetitive pulses (= interpulse time = $T_{\rm ac}$ + $T_{\rm d}$ if $\tau_{\rm p}$ is negligible)
 - u in-phase (dispersion mode) signal
 - v out-of-phase (absorption mode) signal
- W_0 , W_1 , W_2 relaxation rates between energy levels differing by 0, 1 and 2 (respectively) in m_T

- α nuclear spin wave function (eigenfunction of \hat{I}_z) for a spin- $\frac{1}{2}$ nucleus
- α_A^2 s-character of hybrid orbital at atom A
- $\alpha_{\rm F}$ the Ernst angle (for optimum FT sensitivity)
- β nuclear spin wave function (eigenfunction of \hat{I}_z) for a spin- $\frac{1}{2}$ nucleus
- γ_X magnetogyric ratio of nucleus X
- δ_X chemical shift (for the resonance) of nucleus of element X (positive when the sample resonates to high frequency of the reference). Usually in ppm. Further information regarding solvent, references or nucleus of interest may be given by superscripts or subscripts or in brackets.
- Δn population difference between nuclear states (Δn_0 at Boltzmann equilibrium)
- $\Delta\delta$ change or difference in δ
- $\Delta \nu_{1/2}$ full width (in Hz) of a resonance line at half-height
 - $\Delta \sigma$ (i) anisotropy in $\sigma(\Delta \sigma = \sigma_{\parallel} \sigma_{\perp})$
 - (ii) difference in σ for two different situations
 - $\Delta \chi$ (i) susceptibility anisotropy ($\Delta \chi = \chi_{\parallel} \chi_{\perp}$)
 - (ii) difference in electronegativities
 - ε_0 permittivity of a vacuum
 - (i) nuclear Overhauser enhancement
 - (ii) asymmetry factor (e.g. in e^2qQ/h)
 - (iii) viscosity
 - θ angle—especially for that between a given vector and \mathbf{B}_0
 - μ_0 (i) magnetic dipole moment (component μ_z along \mathbf{B}_0)
 - (ii) electric dipole moment
 - μ_0 permeability of a vacuum
 - μ_B Bohr magneton
 - μ_N nuclear magneton
 - $\nu_{\rm c}$ carrier frequency of the radiation
 - ν_i Larmor precession frequency of nucleus j (in Hz)
 - ν_0 (i) spectrometer operating frequency
 - (ii) Larmor precession frequency (general, or of bare nucleus)
 - ν_1 frequency of 'observing' r.f. magnetic field
 - ν_2 frequency of 'irradiating' r.f. magnetic field
 - Ξ_X resonance frequency for the nucleus of element X in a magnetic field such that the protons in TMS resonate at exactly 100 MHz
 - σ shielding tensor
 - σ_i shielding constant of nucleus j (used sometimes in tensor form). Usually in ppm. Subscripts may alternatively indicate contributions to σ
- $\sigma_{\parallel}, \sigma_{\perp}$ components of σ parallel and perpendicular to a molecular symmetry axis
 - τ time between r.f. pulses (general symbol)
 - τ_A pre-exchange lifetime of molecular species A
 - $\tau_{\rm c}$ correlation time, especially for molecular tumbling
 - $\tau_{\rm d}$ dwell time
 - $\tau_{\rm e}$ electronic correlation time
 - τ_{null} recovery time sufficing to give zero signal after a 180° pulse
 - $\tau_{\rm p}$ pulse duration

correlation time for relaxation by the scalar mechanism

 $\tau_{\rm sr}$ correlation time for spin-rotation relaxation

 $au_{\parallel}, au_{\perp}$ correlation times for molecular tumbling parallel and perpendicular to a symmetry axis

(i) magnetic susceptibility

(ii) electronegativity

(iii) nuclear quadrupole coupling constant $(=e^2qQ/h)$

 $\omega_i, \omega_0, \omega_1, \omega_2, \omega_c$

 ω_2, ω_c as for $\nu_i, \nu_0, \nu_1, \nu_2, \nu_c$ but in rad s⁻¹ Ω_1, Ω_2 the strength of a radiofrequency magnetic field, expressed in angular frequency units for a nucleus of magnetogyric ratio γ ($\Omega_1 = \gamma B_1, \Omega_2 = \gamma B_2$).

 γB_2)

Abbreviations

acac acetylacetonato

ASIS aromatic solvent-induced shift

CIDNP chemically-induced dynamic nuclear polarization

CPMG Carr-Purcell pulse sequence, Meiboom-Gill modification

CW continuous wave

DD dipole-dipole (interaction or relaxation mechanism)

DMSO dimethylsulphoxide

EFG electric field gradient

en ethylenediamine

ESR electron spin resonance

FID free induction decay

fod 1,1,1,2,2,3,3-heptafluoro-7,7-dimethyl-4,6-octanedionato

FT Fourier transform

LCAO linear combination of atomic orbitals

MO molecular orbital

mol. wt. molecular weight

NMR nuclear magnetic resonance

NOE nuclear Overhauser effect

NQR nuclear quadrupole resonance

o.d. outside diameter

ppm parts per million

QF quadrupole moment/field gradient (interaction or relaxation

mechanism)

r.f. radiofrequency

r.m.s. root mean square

SA shielding anisotropy

S/N signal-to-noise ratio

SPI selective population inversion

SPT selective population transfer

SR spin-rotation (interaction or relaxation mechanism)

tmhd 2,2,6,6-tetramethylheptane-3,5-dionato (also known as dpm,

dipivaloylmethanato)

TMS tetramethylsilane

UE unpaired electron relaxation mechanism

WAHUHA Waugh, Huber and Haeberlen (pulse sequence)

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