ELECTRON CORRELATIONS IN MOLECULES AND SOLIDS

Third Enlarged Edition

分子和固体中的电子关联

第3版

Peter Fulde

Electron Correlations in Molecules and Solids

Third, Enlarged Edition

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Preface

Since its first publication in 1991, sufficient time has elapsed for this book to undergo a number of improvements, extensions and updates made desirable by progress in the field. In particular, the projection and partitioning technique can now be formulated in a simple and appealing way that also enables us to easily derive the standard quantum-chemical approximations. Thus, extensive rewriting of Chaps. 4 and 5 was imperative. Chapter 6 now contains an extension of the cumulant formalism to excited states, while Chap. 7 formulates the projection method for finite temperature calculations.

The second part of the book, which presents various applications of the theory, also includes a number of extensions. Chapter 9, which deals with semi-conductors, presents new and highly accurate results for the ground state based on the method of increments. In Chap. 11 the treatment of excitations in transition metals has been improved. Chapter 12 on strong correlations has been thoroughly rewritten to take account of new developments and insights. Chapters 13 and 14 have likewise been extended and modified; in particular, the section on high- $T_{\rm c}$ superconducting materials has been updated.

Without the immense support of Dr. H. Lotsch, the spiritus rector of the physical science program of Springer-Verlag, it would have taken far longer for this edition to appear. I am very grateful to him.

Dresden February 1995 P. Fulde

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Preface to the First Edition

Any participant in a quantum chemistry meeting will notice that the attendance of solid-state physicists is rather sparse, and the reverse holds true for solid-state physics conferences, where one will meet hardly any quantum chemists. This shows how little contact exists between these two very active and important fields of condensed matter research. This is regrettable because, as solid-state physics becomes more and more a materials science and as quantum chemists are able to treat larger and larger molecules, the topics of mutual interest in these two fields are rapidly increasing. In order to change this situation, monographs are required that emphasize the features common to quantum chemistry and solid-state physics. It is the aim of this book to make a contribution here. An attempt is made to present the problem of electron correlations in molecules and solids in a unified form. For that we need a framework within which we can treat not only molecules and solids but also weakly and strongly correlated electrons. Such a framework is provided here. Because the terminology is often quite different in quantum chemistry and solid-state physics we have tried to compromise by using vocabulary and notation which should be reasonably familiar to scientists in both fields.

The book is divided into two parts. The first seven chapters concentrate on the various methods and techniques which are used to treat electron correlations in molecules and solids, whereas Chaps. 8–14 deal mainly with applications. They range from atoms and molecules to semiconductors and metals, with special emphasis on transition metals. Particular attention is paid to strongly correlated electron systems, a topic to which the last three chapters are devoted. The Kondo effect and in particular heavy-fermion systems and the new high-temperature superconducting materials fall into that category.

Without the fine cooperation and the support of Dr. H. Lotsch of Springer-Verlag this book would have taken much longer to complete. Ms. D. Hollis, also of Springer-Verlag, made important improvements to the manuscript. I am thankful to both of them.

Stuttgart March 1991

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List of Abbreviations

AD average density
AF antiferromagnet

ARPES angular resolved photoelectron spectroscopy

BCS Bardeen, Cooper, Schrieffer

BIS bremsstrahlung isochromat spectroscopy

BOA bond orbital approximation CEF crystalline electric field

CEPA coupled electron pair approximation

CGTO contracted Gauss-type orbital configuration interaction

CI-SD configuration interaction with single and double substitutions

CMO canonical molecular orbital

CNDO complete neglect of differential overlap CPA coherent potential approximation

DZ double zeta

DZ + P double zeta plus polarization function EELS electron energy loss spectroscopy

GTO Gauss-type orbital HF Hartree-Fock

HOMO highest occupied molecular orbital

INDO intermediate neglect of differential overlap

LDA local density approximation LMO localized molecular orbital

LSD local spin density

MC-SCF multiconfiguration self-consistent field MNDO modified neglect of differential overlap

MO molecular orbital

MP-2(4) Møller-Plesset perturbation expansion including second

(fourth) order terms

MR-CI-SD multireference configuration interactions using single and

double excitations

NCA noncrossing approximation

NO natural orbital

OLRO off-diagonal long range order

PCILO perturbation configuration interaction using localized

orbitals

XIV List of Abbreviations

DATO		
PNO	pair natural orbita	1
1110	Dan Hatulai Ol Olla	

RKKY	Ruderman, Kittel, Kasuya, Yoshida
RPA ·	random phase approximation

Fourier Transforms

of operators:
$$a_{i\sigma} = \frac{1}{\sqrt{N_0}} \sum_{\mathbf{k}} a_{\mathbf{k}\sigma} e^{-i\mathbf{k} \cdot \mathbf{R}_i}$$

$$N_0$$
 = number of sites

of functions:
$$F_i = \frac{1}{N_0} \sum_{\mathbf{k}} F_{\mathbf{k}} e^{-i \mathbf{k} \cdot \mathbf{R}_i}$$

1. Introduction

This book aims at bridging the gap between two active fields of research, i.e., quantum chemistry and solid-state theory. Soon after the development of quantum mechanics by Heisenberg [1.1], Schrödinger [1.2], Born and Jordan [1.3], Dirac [1.4], and others, the paper by Heitler and London [1.5] on the ground state of the H_2 molecule opened the way to a theoretical understanding of chemical bonding. Their work marks the beginning of quantum chemistry. The Heitler-London ansatz for the ground-state wavefunction of H_2 treats the two electrons as being strongly correlated, i.e., by excluding ionic configurations the two electrons stay completely out of each other's way. The ground state is a singlet and has the form

$$\psi_{\text{HL}}^{\text{S}}(\mathbf{r}_1, \mathbf{r}_2) = \frac{1}{2} [\phi_1(\mathbf{r}_1)\phi_2(\mathbf{r}_2) + \phi_2(\mathbf{r}_1)\phi_1(\mathbf{r}_2)](\alpha_1\beta_2 - \beta_1\alpha_2). \tag{1.0.1}$$

The functions $\phi_{1,2}(\mathbf{r})$ are centered on atoms 1 and 2, and the spinors α and β refer to spin up and spin down, respectively.

A distinctly different approach to the problem of interacting electrons was taken shortly thereafter by Hartree~[1.6], Fock~[1.7], and Slater~[1.8], who treated the electrons as being independent of each other and introduced the idea of the self-consistent field. The latter is the interaction field an electron experiences when we take a spatial average over the positions of all the other electrons. Within the independent-electron approximation, the ground-state wavefunction of H_2 is of the form

$$\psi_{\text{HF}}^{\text{S}}(\mathbf{r}_{1}, \mathbf{r}_{2}) = \frac{1}{2^{3/2}} [\phi_{1}(\mathbf{r}_{1})\phi_{1}(\mathbf{r}_{2}) + \phi_{1}(\mathbf{r}_{1})\phi_{2}(\mathbf{r}_{2}) + \phi_{2}(\mathbf{r}_{1})\phi_{1}(\mathbf{r}_{2}) + \phi_{2}(\mathbf{r}_{1})\phi_{2}(\mathbf{r}_{2})](\alpha_{1}\beta_{2} - \beta_{1}\alpha_{2}).$$
(1.0.2)

One notices that the ionic configuration $\phi_1\phi_1$ and $\phi_2\phi_2$ in (1.0.2) enter with equal weight when compared with the nonionic configurations. Thus, when the two hydrogen atoms are pulled apart, the wavefunction does not reduce properly to the atomic limit. On the other hand, (1.0.1) does not reduce properly to the correct wavefunction in the limit of small atomic distances. As one might expect, the true ground state lies between the two extremes (1.0.1) and (1.0.2). Electron correlations reduce the ionic configuration relative to the nonionic ones, but they do not reduce them to zero as (1.0.1) suggests.

The forms (1.0.1) and (1.0.2) are prototypes of wavefunctions which apply not only to the H_2 molecule but, more generally, to both quantum chemistry

and to solid-state physics. They stand for localized versus delocalized electrons and have been the subject of countless discussions and controversies. Whether an improved calculation should start from a wavefunction of the Heitler-London (strong-correlation limit) or the Hartree-Fock form (limit of independent electrons) depends on how strong electron correlations become in a given molecule or solid. In principle, one would like to have a quantity which specifies the correlation strength in different bonds or atoms in a given chemical environment. This textbook intends to provide this information in a systematic fashion.

Two different roads have been pursued in quantum chemistry towards a qualitative and quantitative understanding of chemical bonding. Pauling [1.9] introduced and developed one of those approaches, basing it on the concept of resonance and resonance structures and essentially using the Heitler-London picture. The other one, the molecular orbital theory, was first developed by Hund [1.10] and Mulliken [1.11] and elaborated by Slater [1.8], Hückel [1.12], and others. It is based on the idea of independent electrons and hence corresponds to (1.0.2). When formulated broadly enough, both approaches described above are equivalent. In practice, however, often only the lowest-order corrections can be calculated for the two limiting cases. The molecular orbital theory has had great success, since most chemical bonds are relatively weakly correlated. It has failed, however, with certain metal-organic complexes or, as far as solids are concerned, with the copper-based high-temperature superconducting oxides, in which electron correlations are strong. The independent-electron approximation proves in those cases an inappropriate starting point.

This leads us to the theory of solids. Sommerfeld and Bethe [1.13] offered the first coherent presentation of a microscopic theory of solids. In particular, their theory of metals is based on free electrons. In view of the strong electron interactions, the fact that a theory of free electrons was so successful remained a puzzle for a long time. It was resolved only after the development of the concept of quasiparticles in Fermi liquids by Landau [1.14]. From his contribution we have gained the insight that the low-energy excitations of a metal can be described by quasiparticles which behave like electrons with renormalized mass, Fermi velocity, etc. This concept holds even for metals with strongly correlated electrons like the heavy-fermion systems. Whether it holds in all cases remains an open problem. As regards the high- T_c superconducting materials, for example, Anderson [1.15] has claimed that this is not the case.

The competition between the Heitler-London and independent-electron descriptions played an important role in the development of the theory of transition metals. Prominent representatives of the two approaches were Van Vleck [1.16] and Slater [1.17]. There is general consent today that in transition metals the d electrons are delocalized; it is also clear, however, that correlations among them are far from weak. Thus a number of atomic features—like Hund's rule coupling—persist despite delocalization. Correlations are particularly strong in some of the transition metal oxides; a well-known example is CoO. Were it not for the strong correlations, this substance would be