SOCIETA' ITALIANA DI FISICA

RENDICONTI

DELLA

SCUOLA INTERNAZIONALE DI FISICA

«ENRICO FERMI»

LXIX Corso

Elementary Modes of Excitation in Nuclei

ITALIAN PHYSICAL SOCIETY

PROCEEDINGS

OF THE

INTERNATIONAL SCHOOL OF PHYSICS
« ENRICO FERMI »

COURSE LXIX

edited by A. BOHR and R. A. BROGLIA

Directors of the Course

VARENNA ON LAKE COMO

VILLA MONASTERO

26th JULY - 7th AUGUST 1976

Elementary Modes of Excitation in Nuclei

NORTH-HOLLAND PUBLISHING COMPANY, AMSTERDAM - NEW YORK - OXFORD

Library of Congress Cataloging in Publication Data

Varenna, Italy. Scuola internazionale di fisica.
Elementary modes of excitation in nuclei.
(Proceedings of the International School of Physics « Enrico Fermi »; course 69).
At head of title: Italian Physical Society.
Added t. p.: Modi elementari di eccitazione nei nuclei.
Course held July 26-Aug. 7, 1976.
Bibliography: p.
1. Nuclear excitation-Congresses. I. Bohr, Aage. II. Broglia, R. A. III. Società italiana di fisica. V. Title: Modi elementari di eccitazione nei nuclei. IV. Title.
QC794.6.E9V37 1977 539.7'54 78-1402
ISBN 0-444-85153-4.

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Direttori del Corso

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SOCIETÀ ITALIANA DI FISICA

BOLOGNA - ITALY

Preface.

In the study of nuclear dynamics, the concept of elementary modes of excitation occupies a central place. The elementary modes reveal themselves directly as the building blocks of the nuclear excitation spectra. The understanding of these modes and of their couplings also provides a basis for the exploration of the nucleus under the more extreme conditions that are now coming within reach of experimental study.

The subject is a vast one, and cannot be dealt with comprehensively within the framework of a course such as the present. The topics selected by the lecturers emphasize focal points of current development and at the same time illustrate general methods that have been developed for the analysis of nuclear dynamics.

The course has been an occasion to confront different approaches to the description of nuclear excitations on the background of the high precision and quality of the experimental information that has been accumulated during the last years. The problem of the proper interpretation of the evidence gave rise to lively discussions concerning the relation between the different approaches and their degree of validity. The discussions helped also to bring into perspective a variety of open problems and exciting new areas of research.

On behalf of all the participants to the course we would like to express our gratitude to the Italian Physical Society for making this course possible and for providing hospitality in the exquisite atmosphere of Villa Monastero.

In the organization of the course it has been a great pleasure to work together with Prof. R. Ricci. At all stages of the preparation of the course and of the Proceedings the assistance of Drs. P. F. Bortignon and C. H. Dasso has been an invaluable help. We would also like to express our thanks for the very helpful contribution of Dr. A. Covello, who acted as scientific secretary of the course, and to pay tribute to the efficiency and devotion of the organizational staff headed by G. Wolzak.

A. Bohr, R. A. Broglia

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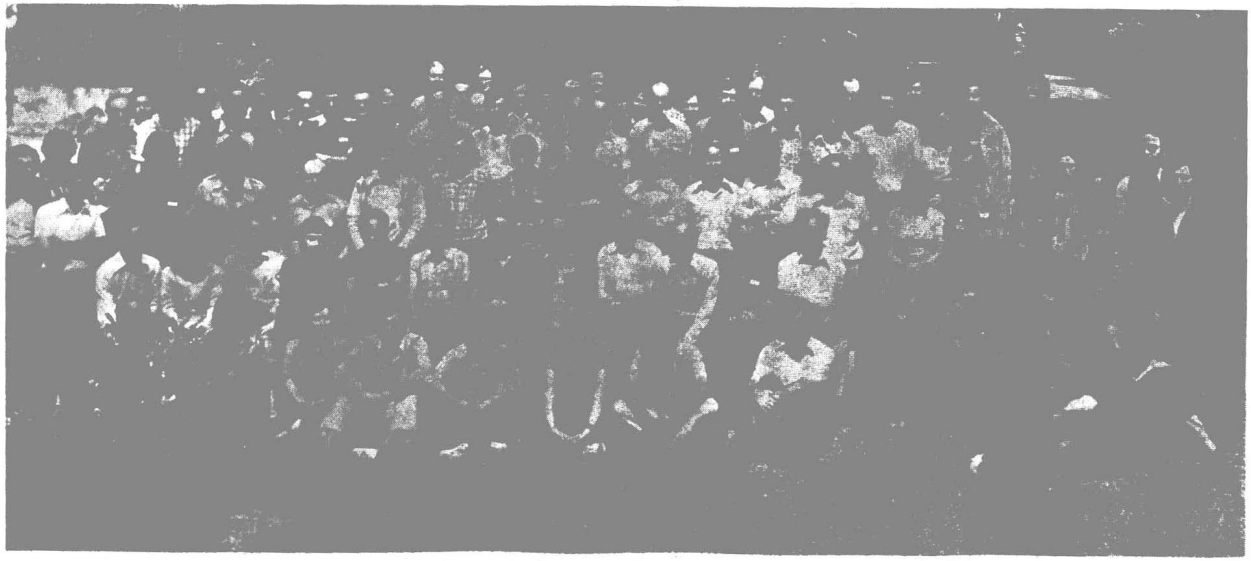
LXIX CORSO - VARENNA SUL LAGO DI COMO - VILLA MONASTERO - 26 Luglio - 9 Agosto 1976



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Tipografia Compositori - Bologna - Italy

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