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NONPARAMETRIC STATISTICAL INFERENCE

Edited by:

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and

I. VINCZE



Vol. I.



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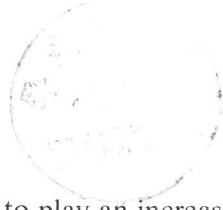
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PREFACE



The field of nonparametric statistics continues to play an increasingly successful role in statistical theory as well as in its applications. Nonparametric methods are not only mathematically elegant, they also provide a variety of applications in several fields such as engineering, economics, agriculture, meteorology and biometrics among others. To stimulate further research and provide an opportunity for personal contacts among scholars whose fields of specialization cover broad spectra, a colloquium on nonparametric statistical inference was held in Budapest from June 23-27, 1980. It was organized by the János Bolyai Mathematical Society and was sponsored by the Bernoulli Society for Mathematical Statistics and Probability and by the Hungarian Central Statistical Office. Professors D.R. Cox and I. Vincze were kind enough to make the opening remarks on behalf of the Bernoulli Society and the Bolyai Society respectively.

The program committee of the colloquium consisted of Professors D.R. Cox, B.V. Gnedenko, J. Jurečková, P. Révész, K. Sarkadi, I. Vincze (Chairman), W.R. Van Zwet and myself. The national organizing committee consisted of Professors M. Arató, P. Bártfai, E. Csáki, B. Gyires, A. Marton and G. Tusnády with A. Krámlí, T. Móri and L. Rejtő as secretaries. It is a pleasure to express our sincere thanks to the members of both these committees for the overall help they gave in making the colloquium a great success. Evidence of the results of their efforts was the rich and active participation of about 150 scholars from 19 different countries. The members of the national organizing committee are also to be thanked for taking care of problems connected with local arrangements. Our Hungarian hosts deserve our thanks not only for the superb organization of the conference but also for providing an excellent atmosphere of warmth, friendliness and generous hospitality.

The proceedings of the colloquium are divided into two volumes containing a broad range of topics such as testing and estimation, ranking and selection, empirical distributions and stochastic processes among

others. The papers in the volumes were presented at the colloquium and were reviewed by the referees. It is a pleasure to express our appreciation to them as well as the authors for their help and cooperation.

Special thanks are due to the Hungarian Central Statistical Office and to its President Mrs. Vera Nyitrai for their help as well as encouragement in organizing the colloquium.

We hope that the proceedings of the colloquium will be of interest to mathematicians as well as applied statisticians.

Madan L. Puri

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SCIENTIFIC PROGRAM

June 23, 1980

Morning session (Congress Hall)

Chairman: P. Révész

- 9³⁰ – 10⁰⁰ Opening session
10¹⁵ – 11⁰⁰ W.R. van Zwet: On the Edgeworth expansion for the simple linear rank statistic
11¹⁵ – 12⁰⁰ D.R. Cox: The randomization theory of experimental design

Afternoon session

Session A

Chairman: Z. Govindarajulu

- 14³⁰ – 14⁵⁰ P.K. Sen: The UI principle and LMP rank tests
14⁵⁵ – 15¹⁵ I.R. Savage: Lehmann models
15²⁰ – 15⁴⁰ M. Csörgő – P. Révész: An invariance principle for N.N. empirical density functions

Interval

- 16⁰⁰ – 16²⁰ R.J. Does – R. Helmers: Edgeworth expansions for functions of uniform spacings
16²⁵ – 16⁴⁵ K. Sarkadi: A direct proof for a ballot type theorem
16⁵⁰ – 17¹⁰ O.I. Toskin: Control of multidimensional hypothesis about quantity of fractiles of continuous distributions

Session B

Chairman: V.S. Koroljuk

14³⁰ – 15¹⁵ J. Blum – V. Susarla – G. Walter: Estimation of the prior distribution using differential operators

Interval

16⁰⁰ – 16²⁰ B. Epstein: Some nonparametric estimation techniques in reliability theory

16²⁵ – 16⁴⁵ R. Zmyślony: On admissible estimation in linear models

16⁵⁰ – 17¹⁰ G. Leunbach: Parameter-free inference in models with sufficient estimation

June 24, 1980

Morning session

Session A

Chairman: V. Mammitzsch

9⁰⁰ – 9⁴⁵ E. Hmaladze: The martingale approach in the theory of nonparametric goodness of fit tests

9⁵⁰ – 10¹⁰ S.S. Gupta – G.C. McDonald: Nonparametric procedures in multiple decisions (ranking and selection procedures)

Interval

10³⁰ – 10⁵⁰ H.S. Konijn: Evaluation of a new treatment

10⁵⁵ – 11¹⁵ R.S. Sudakov: A confidence bound for function with preventing binomial parameters

11²⁰ – 11⁴⁰ H. Callaert – P. Janssen: The convergence rate of fixed width sequential confidence intervals

11⁴⁵ – 12⁰⁵ C. Stepniak: On testability of statistical hypotheses

Session B

Chairman: B. Penkov

- 9⁰⁰ – 9⁴⁵ J. Jurečková: Tests of location and criterion of tails
9⁵⁰ – 10¹⁰ B. Gyires: Linear rank statistics generated by uniformly distributed sequences

Interval

- 10³⁰ – 10⁵⁰ Z. Prášková: A local limit theorem and an asymptotic expansion for a two-sample rank test
10⁵⁵ – 11¹⁵ M. Hušková: On bounded length sequential confidence interval for parameter in regression model based on ranks
11²⁰ – 11⁴⁰ D. Vorličková: Exact slopes for rank statistics for a two-sample problem under discrete distribution
11⁴⁵ – 12⁰⁵ T. Gerstenkorn: On some statistical problem joining the inflated Polya distribution to Bayes rule

Afternoon session

Session A

Chairman: D. Rasch

- 14⁰⁰ – 14²⁰ B. de Finetti: Aspects of heuristics
14²⁵ – 14⁴⁵ V.K. Rohatgi: Operator self-similarity
14⁵⁰ – 15¹⁰ H. Grimm: Transformation of variables versus nonparametrics

Interval

- 15³⁰ – 15⁵⁰ G. Enderlein: Hierarchical clustering methods
15⁵⁵ – 16¹⁵ M. Ghosh – R. Dasgupta: Berry – Esseen theorems for U -statistics in the non i.i.d. case
16²⁰ – 16⁴⁰ Z. Grabos: Some applications of spectral decomposition of a matrix in analysis of variance
16⁴⁵ – 17⁰⁵ C. Domański: Notes on the Theil test for the hypothesis of linearity for the model with two explanatory variables

Session B

Chairman: H. Witting

- 14⁰⁰ – 14²⁰ K. Jogdeo: Nonparametric methods for gross error models involving location parameters
- 14²⁵ – 14⁴⁵ V.S. Koroljuk – Y.V. Borovskih: Analytical method in theory of rank statistics
- 14⁵⁰ – 15¹⁰ Z. Govindarajulu: Asymptotic normality of linear combinations of functions of order statistics in one and several samples
- Interval
- 15³⁰ – 15⁵⁰ U. Müller-Funk: On contiguity and weak convergence with an application to sequential analysis
- 15⁵⁵ – 16¹⁵ W. Schlee: Nonparametric tests of the monotony and convexity of regression
- 16²⁰ – 16⁴⁰ S.A. Hashimov: An effective estimate of nonlinear functionals
- 16⁴⁵ – 17⁰⁵ G. Sadasivan: Within pair order effects in paired comparisons

June 26, 1980
Morning session

Session A

Chairman: J. Blum

- 9⁰⁰ – 9²⁰ J.K. Ghorai – A. Susarla – V. Susarla – J. Van Ryzin:
Nonparametric estimation of mean residual life time
with censored data
- 9²⁵ – 9⁴⁵ E.G. Phadia: Nonparametric Bayesian inference based on
censored data – an overview
- 9⁵⁰ – 10¹⁰ V.N. Nair: Goodness of fit tests for multiply right censored
data

Interval

- 10³⁰ – 10⁵⁰ N. Reid: Nonparametric estimation for censored data
- 10⁵⁵ – 11¹⁵ R. Thrum: Convergence of quadratic forms and applica-
tions in mixed models
- 11²⁰ – 11⁴⁰ B. Levit: On asymptotic optimality of nonparametric esti-
mators
- 11⁴⁵ – 12⁰⁵ B. Prasad – R.S. Singh: Nonparametric kernel estimates
of a density function alongwith its derivatives

Session B

Chairman: V.K. Rohatgi

- 9⁰⁰ – 9²⁰ G. Halász: Nonparametric regression and density estimations for smooth functions
- 9²⁵ – 9⁴⁵ B. Kim -- J. Van Ryzin: On the asymptotic distribution of a histogram density estimator
- 9⁵⁰ – 10¹⁰ M.A. Mirzahmedov: Nonparametric estimation of probability density

Interval

- 10³⁰ – 10⁵⁰ R.J. Serfling: Properties and applications of metrics on nonparametric density estimators
- 10⁵⁵ – 11¹⁵ A. Kozek – W. Wertz. Estimators with values in Banach spaces under convex loss and applications to curve estimation problems
- 11²⁰ – 11⁴⁰ H.L. Koul: Some weighted empirical inferential procedures for a simple regression model
- 11⁴⁵ – 12⁰⁵ P. Deheuvels: Some applications of the dependence functions to statistical inference: nonparametric estimates of extreme values distributions, and a Kiefer type universal bound for the uniform test of independence

Session C

Chairman: B. Epstein

- 9⁰⁰ – 9²⁰ K.A. Borovkov: On the rate of convergence in the generalized invariance principle
- 9²⁵ – 9⁴⁵ E. Schumacher: Kendall's Tau, used as a coefficient of disarray between permutations with unoccupied places
- 9⁵⁰ – 10¹⁰ P. Stolarski: A nonparametric method for classification based on orthonormal series

Interval

- 10³⁰ – 10⁵⁰ W.R. Allen: On Kolmogorov bounds for survival functions when there are losses as well as deaths
- 10⁵⁵ – 11¹⁵ V. Mammitzsch: Is the distribution function of $f(X + Y) - X$ continuous, if X and Y are independent and have continuous distribution functions?
- 11²⁰ – 11⁴⁰ M.L. Puri – N.S. Rajaram: Stochastic integrals and rank statistics

Afternoon session

Session A

Chairman: P.K. Sen

- 14⁰⁰ – 14²⁰ E. Csáki: On the standardized empirical distribution function
- 14²⁵ – 14⁴⁵ I.S. Borisov: An approximation of empirical fields
- 14⁵⁰ – 15¹⁰ A. Sahanenko: On unimprovable estimates of the rate of convergence in invariance principle

Interval

- 15³⁰ – 15⁵⁰ J.-P. Raoult: Some remarks on generalized Skorohod topology, in connection with weak convergence of multi-dimensional empirical processes (non-stationary φ -mixing case)
- 15⁵⁵ – 16¹⁵ S. Csörgő: The empirical moment generating function
- 16²⁰ – 16⁴⁰ H.-G. Müller: Uniformly consistent kernel estimates of a multivariate regression function and of its mixed partial derivatives

Session B

Chairman: W. Wertz

- 14⁰⁰ – 14⁴⁵ K.B. Athreya – P. Ney: Some aspects of ergodic theory and laws of large numbers for Harris-recurrent Markov chains
- 14⁵⁰ – 15¹⁰ W. Jahn: Regression analysis under the condition that the determinant of the covariance matrix is small

Interval

- 15³⁰ – 15⁵⁰ D. Dabrowska: Parametric and nonparametric models with special schemes of stochastic dependence
- 15⁵⁵ – 16⁴⁰ D. Rasch – G. Herrendörfer: Optimum experiment design and analysis – estimating the regression function