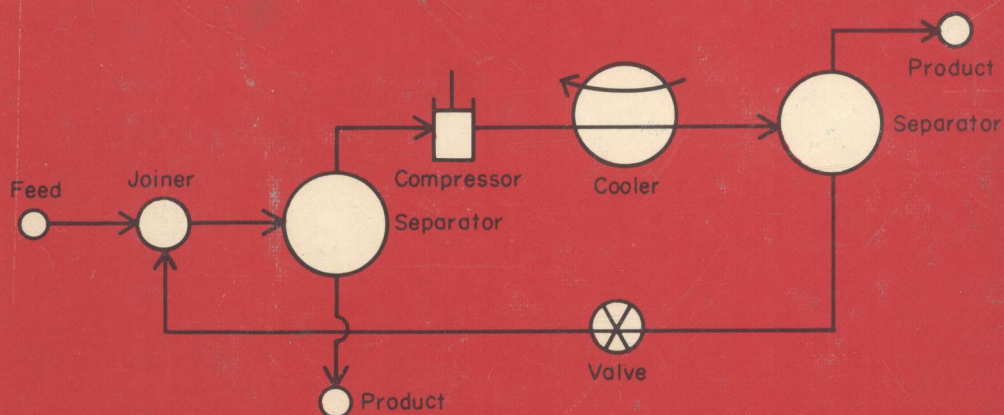CHEMICAL PROCESSING AND ENGINEERING   VOLUME 4
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THERMODYNAMICS
OF
FLUIDS

An Introduction to Equilibrium Theory

K. C. CHAO • R. A. GREENKORN

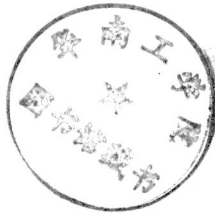# Thermodynamics of Fluids

AN INTRODUCTION TO EQUILIBRIUM THEORY

K. C. Chao and R. A. Greenkorn

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Thermodynamics of Fluids

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To our parents

Juipu and Chungpu Chao
and
Sophie and Frederick Greenkorn

8560771

Equilibrium models play a major part in the engineering
analysis of chemical processes. The main purpose of this
book is to present tools that are needed for the construc-
tion of these models for real systems. The usefulness of
equilibrium properties is, however, not limited to the con-
struction of models. The task of making mass and energy
balances requires a knowledge of the volumetric behavior and
of the energy functions of the materials in question. The
study of chemical reactors, of transport operations, and of
the dynamic response of real systems presupposes that the
equilibrium properties of the fluids involved are known.

        The diversity of substances encountered in chemical
processes precludes a compiler's approach, such as employed
by heat power engineers in the preparation of the steam
tables. Even when extensive experimental data are available
on a system of interest, the data are hardly ever adequate
without interpretation to account for effects of variation
of compositions, temperature, and pressure. Direct experi-
mental data for most real systems of practical interest are
usually either unavailable or fragmentary. A large body of
literature has been developed to answer the need for the cor-
relation, prediction, and estimation of physical properties.
The theory of equilibrium properties provides the basis for
the judicious use of this literature.

        The development of equilibrium theory has been rapid
during the last two decades. The developments rest on the
foundation of Gibbs' general theory of equilibrium, for which

v

practical measures were invented by Lewis and co-workers in
the 1920s and 1930s. The complexity of real fluid behavior
nevertheless defeated all efforts at reducing the theory to
meaningful practice except for ideal gases and ideal solu-
tions until the principle of corresponding states was estab-
lished on a molecular basis and exploited for the description
of pure fluid behavior. Following this major achievement,
the last two decades witnessed rapid advances in the study
of nonideal mixtures in both the gas and liquid states. As
a result of these advances more and more process systems are
amenable to quantitative description and analysis. It is
our intention to give a comprehensive account of theory to
include the basic principles, some significant developments,
and interesting applications.

The material contained in this book is meant to intro-
duce the reader to the frontiers of application starting with
the fundamental principles. The introductory nature of this
work does not imply the exclusive use of elementary subject
matter even though only elementary principles of classical
and statistical thermodynamics are included. The applica-
tions are illustrated with examples chosen to cover a wide
variety of subjects and from diverse sources in our effor
to present a broad view of the area, although we must ad
to an unavoidable predilection toward subjects that are
familiar to us.

This book is designed primarily as a textbook fo
graduate students in chemical engineering. However, t
troductory nature of the work should make it equally o
to practicing engineers who wish to learn the subject m
but have had no prior training in it. The example appli
tions and quantitative correlations presented should als
of interest to experienced practitioners.

At Purdue University, we use the book as the text
a course entitled "Thermodynamics" for the entering gra
students. With judicious selection of text material we
the major part of the contents in one semester with th
hour classes per week. There is enough material in th

to offer some degree of flexibility in the selection of top-
ics for use in a semester course to suit the interest of a
particular institution or instructor.

We are indebted to many individuals directly and in-
directly for their contribution and assistance. Both of us
were introduced to the subject area by Professor O. A. Hougen.
Dr. J. A. Ellis read parts of the manuscript and made many
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and M. G. White for contributions with calculations and other
materials. Mrs. Mary Dobrasko, Susie O'Dore, and Nancy Smith
typed and retyped parts of the manuscript.

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K. C. Chao
R. A. Greenkorn
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Chapter 5
PHASE AND CHEMICAL EQUILIBRIA

Chapter 1

THERMODYNAMIC PRINCIPLES AND FUNCTIONS

1.1   INTRODUCTION

The subject matter of this chapter is classical thermo-
dynamics.   Our purpose is to present a concise recapitulation
of the fundamental concepts and functions used in classical
thermodynamics.   The emphasis is to show the structure and to
develop the relations that are needed for the study of physi-
cochemical equilibrium.

    We begin with several definitions and then discuss
exact and inexact differentials.   Thermodynamic laws are pre-
sented on the basis of this discussion as statements regarding
state functions.   The zeroth, first, and second laws are
stated in terms of the state functions they introduce: tem-
perature, internal energy, and entropy, respectively.   The
ideal gas and absolute temperatures are defined in the course
of discussion of the laws.   (The statement and discussion of
the third law will be postponed until Chapter 5.)

    The usefulness of the thermodynamic laws is greatly
extended with the introduction of the energy functions.   The
concept of their association with certain natural variables
is basic to this usefulness.   Since these functions are re-
lated to reversible shaft work under various conditions of

constraint, they provide the basis for the development of
criteria of equilibrium and stability.

The quantity of central importance in all studies of
equilibrium is the Gibbs chemical potential, which is intro-
duced through considerations of open systems. The usefulness
of the chemical potential is indicated, but not developed,
because the development is one of the central themes of several
chapters to follow.

We close this chapter with a discussion of Jacobians as
the mathematical tool for manipulating thermodynamic identi-
ties and include a collection of such identities of common
occurrence.

1.2 SYSTEMS, PROCESSES, AND PROPERTIES

In thermodynamic analysis, we study a portion of the universe.
This portion is called a *system*. The rest of the universe is
the *surroundings*. If a system is separated from its surround-
ings so as to preclude exchange of mass and energy between the
system and its surroundings, the system is called *isolated*.
An *open* system is free to exchange mass and energy with its
surroundings; the exchange can take place through a porous
wall, a phase-boundary surface, or just an imaginary geometri-
cal surface. A *closed* system cannot exchange mass with the
surroundings.

A *phase* is a homogeneous part of a system. Homogeneity
must be defined in terms of an appropriate scale, since, with
a sufficiently fine scale, all matter is heterogeneous in
view of its atomic and molecular constitution. With a coarse
scale, an emulsion could be considered homogeneous. All homo-
geneous phases have *extensive* properties that are directly
proportional to the mass of the phase. For example, volume,
internal energy, and entropy are extensive properties. An
extensive property of a system is the sum of the extensive
property values for all the phases in the system. The proper-
ties of a phase that are independent of mass, such as density,
temperature, and pressure, are called *intensive* properties.

An extensive property E is a homogeneous function of degree 1 in mass m of the components and is expressed by

$$\lambda E(T,p,\rho,m_1,m_2,\ldots) = E(T,p,\rho,\lambda m_1,\lambda m_2,\ldots) \qquad (1.1)$$

where λ is a positive number that is not necessarily equal to 1 and the subscripts refer to components. An intensive property I is a homogeneous function of degree zero in m,

$$I(T,p,\rho,m_1,m_2,\ldots) = I(T,p,\rho,\lambda m_1,\lambda m_2,\ldots) \qquad (1.2)$$

The ratio of two extensive properties is an intensive property.

The *state* of a phase is specified by its composition and a relatively few intensive properties; usually two intensive properties (e.g., temperature and pressure) are enough. The exact number or kind of intensive properties required are determined by experience. Additional intensive properties such as specific surface area, gravitational acceleration, and magnetic or electric fields may be required to specify state of a phase for some systems.

State properties assume the same value at the same state regardless of the previous history of the system; that is, state properties are reproducible and have no memory. The hardness of a specimen of steel is not reproducible inasmuch as it depends on its heat treatment. Liquids of high polymers likewise have nonreproducible properties.

A system is at *equilibrium* if the net fluxes of mass, energy, and chemical reactions in the system are all zero. Temperature and chemical potentials are uniform in equilibrium systems. An equilibrium state is a *steady state*; that is, it does not change with time. Not all steady states, however, are equilibrium states, because there may be net flow of mass or energy.

A change of state is called a *process*. An *adiabatic* process takes place when the system is insulated from its surroundings; an *isothermal* process takes place at a constant temperature; and an *isobaric* process takes place at constant pressure.

A process is *reversible* when caused by an infinitesimal
net driving force and when proceeding at infinitesimal speed.
All the states that a system assumes during a reversible pro-
cess are equilibrium states. The reversible process is an
ideal zero-speed limit for actual processes, which must take
place with finite speed; all actual processes are irreversible.

1.3 EXACT AND INEXACT DIFFERENTIALS

The quantities of interest in thermodynamics can be divided
into two broad classes. One class contains quantities that
are associated with the state of a system, such as density,
isothermal compressibility, and heat capacity. These quanti-
ties are called state properties or state functions and assume
definite values depending only on the state of the system.
They are represented by exact differentials. The other class
of quantities such as heat and work are associated with proc-
esses and are represented by inexact differentials.

The first and the second laws are statements regarding
certain functions being state functions, which are independent
of path. Since the values of state properties are independent
of path, only the initial and final states must be determined,
either by direct observations or by indirect derivations. The
results become applicable to the myriad of possible processes
that can take place in between the initial and final states.
In this section we address ourselves to the mathematical con-
siderations regarding exact and inexact differentials.

Consider the mechanical work done by a fluid at pressure
p undergoing an infinitesimal change in volume dV; the mechan-
ical work is p dV. The total work associated with a change
from state 1 to state 2 is the integral $\int_1^2$ p dV and is repre-
sented by an area between V_1 and V_2 on the p-V diagram (Fig.
1.1). The value of the integral representing work depends on
the path taken between 1 and 2. Without specifying the path,
we could not meaningfully talk about the work. Another way
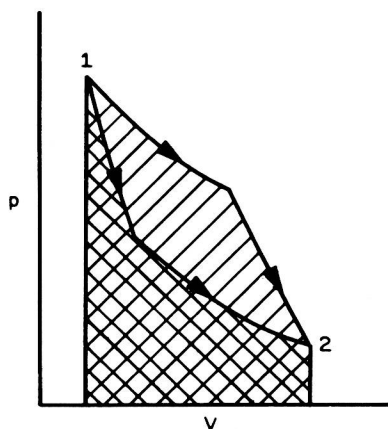of stating this is to say that work is not an exact differen-
tial.

FIG. 1.1.   p-V work.

An infinitesimal quantity of work is expressed by $\delta W = p\,dV$. By this equation we do not mean that W is a function of p or V, nor that δW is the differential of this function. On the other hand, take the ideal-gas equation,

$$T = \frac{p\tilde{V}}{R} \tag{1.3}$$

which says T is a function of p and $\tilde{V}$. A differential change of T, expressed by $dT = (p/R)\,d\tilde{V} + (\tilde{V}/R)\,dp$, is an exact differential.

We recall that a differential expression

$$M(x,y)\,dx + N(x,y)\,dy$$

is exact if

$$\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x} \tag{1.4}$$

Equation (1.4) is a necessary and sufficient condition for a function $f(x,y)$ to exist such that

$$df = M\,dx + N\,dy \tag{1.5}$$

It is easily seen that Eq. (1.4) is a necessary condition for Eq. (1.5) to be valid, because $M = \partial f/\partial x$ and $N = \partial f/\partial y$, and upon differentiating