# Principles of Gas-Solid Flows



Liang-Shih Fan and Chao Zhu

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### **Principles of Gas-Solid Flows**

Gas-solid flows are involved in numerous industrial processes and occur in various natural phenomena. This authoritative book addresses the fundamental principles that govern gas-solid flows and the application of these principles to various gas-solid flow systems.

The book is arranged in two parts: Part I deals with basic relationships and phenomena, including particle size and properties, collision mechanics of solids, momentum transfer and charge transfer, heat and mass transfer, basic equations, and intrinsic phenomena in gas—solid flows. Part II discusses the characteristics of selected gas—solid flow systems such as gas—solid separators, hopper and standpipe flows, dense-phase fluidized beds, circulating fluidized beds, pneumatic conveying systems, and heat and mass transfer in fluidization systems.

As a comprehensive information source on gas-solid flows, this text will be useful to a broad range of engineers and applied scientists – chemical, mechanical, agricultural, civil, environmental, aeronautical, and materials engineers, as well as atmospheric and meteorological scientists.

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## **Preface**

Gas-solid flows are involved in numerous industrial processes and occur in various natural phenomena. For example, in solid fuel combustion, gas-solid flows are involved in pulverized coal combustion, solid waste incineration, and rocket propellant combustion. Gas-solid flows are encountered in pneumatic conveying of particulates commonly used in pharmaceutical, food, coal, and mineral powder processing. Fluidization is a common gas-solid flow operation with numerous important applications such as catalytic cracking of intermediate hydrocarbons, and Fischer-Tropsch synthesis for chemicals and liquid fuel production. Gas-solid flows occur in gas-particle separations, as exemplified by cyclones, electrostatic precipitators, gravity settling, and filtration operations. Fine powder-gas flows are closely associated with material processing, as in chemical vapor deposition for ceramics and silicon production, plasma coating, and xerography. In heat transfer applications, gassolid flows are involved in nuclear reactor cooling and solar energy transport using graphite suspension flows. Solid dispersion flows are common in pigment sprays, dust explosions and settlement, and nozzle flows. The natural phenomena accompanied by gas-solid flows are typified by sand storms, moving sand dunes, aerodynamic ablation, and cosmic dusts. The optimum design of the industrial processes and accurate account of the natural phenomena that involve gas-solid flows as exemplified previously require a thorough knowledge of the principles governing these flows.

This book is intended to address basic principles and fundamental phenomena associated with gas-solid flows, as well as characteristics of selected gas-solid flow systems. It covers the typical range of particle sizes of interest to gas-solid flows, i.e., 1  $\mu$ m-10 cm, recognizing that flow characteristics for submicrometer particles are also of great industrial importance. The book features a systematic account of important theories or models concerning particle mechanics as well as fluid dynamics from their origins of the development. The physical interpretation and limitations in application of these theories or models are emphasized. Various intrinsic phenomena underlying the gas-solid flow systems are also illustrated. The book is aimed as a textbook for seniors and graduate students who are interested in general or specific topics of gas-solid flows. In addition, it can be used as a reference for researchers and practitioners who are interested in the general field of multiphase flow. It is written with multidisciplinary engineering readers in mind. Specifically, it will be of benefit to chemical and mechanical engineering readers as well as readers in other engineering disciplines, including agricultural, civil, environmental, pharmaceutical, aeronautical, mining, and atmospheric and meteorological sciences.

The book contains two parts; each part comprises six chapters. Part I deals with basic relationships and phenomena of gas—solid flows while Part II is concerned with the characteristics of selected gas—solid flow systems. Specifically, the geometric features (size and size distributions) and material properties of particles are presented in Chapter 1. Basic particle sizing techniques associated with various definitions of equivalent diameters of particles are also included in the chapter. In Chapter 2, the collisional mechanics of solids, based primarily on elastic deformation theories, is introduced. The contact time, area, and

force of colliding particles are discussed using theories of elastic collision, which are important to the formulation of the momentum, heat, and charge transfer processes involving collisions of solids. Chapter 3 is devoted to the momentum and charge transfer of gas-solid flows. Various forces in gas-solid flows due to gas-particle interactions, particle-particle interactions, and external fields are delineated. Equations for single-particle motion, based on a force balance analysis, are derived. Basic mechanisms of charge generation in gassolid flows are also introduced in the chapter, along with a detailed discussion of charge transfer mechanism by particle collisions. Chapter 4 deals with fundamental concepts and theories of heat and mass transfer in gas-solid flows. Highlights include thermal radiation of the particulate phase and heat conduction in collisions of elastic particles. Chapter 5 presents four basic modeling approaches of gas-solid flows, namely, continuum modeling of multiphase flows or multifluid modeling, trajectory modeling, kinetic theory modeling for collision-dominated dense suspensions, and the Ergun equation for flow through a packed bed of particles. In this chapter, the hydrodynamic equations of single-phase flows are first discussed. Here, basic concepts of kinetic theory of gas and turbulence models are introduced as a preamble to discussion of these basic modeling approaches. In contrast to the  $k-\epsilon$  turbulence model for single-phase flows, the  $k-\epsilon-k_{\rm p}$  model is introduced with the continuum approach of gas-solid flows to account for gas-solid turbulence interactions. Chapter 6 focuses on the discussion of intrinsic phenomena in gas-solid flows, such as erosion and attrition, acoustic wave and shock wave propagation through a gas-solid suspension flow, thermodynamic properties of a gas-solid mixture, flow instability, and gas-solid turbulence interactions.

Chapter 7 is concerned with gas-solid separations. The basic separation methods introduced in this chapter include cyclone, filtration, electrostatic precipitation, gravity settling, and wet scrubbing. Chapter 8 deals with hopper flows and standpipe flows, which are commonly encountered in the bulk solids handling and transport processes. In order to understand the fundamental hopper and standpipe flow characteristics, some basic concepts of powder mechanics are illustrated. Chapter 9 introduces the general concept of gas fluidization. Specifically, the chapter addresses dense-phase fluidization, which represents a gas-particle operation of enormous industrial importance. Various operating regimes including particulate fluidization, bubbling/slugging fluidization, and turbulent fluidization are discussed along with spouting. The fundamental properties of bubble, cloud, and wake and the intrinsic bubble coalescence and breakup and particle entrainment phenomena are illustrated. Chapter 10 continues the discussion of fluidization under higher-velocity conditions which are characterized by fast fluidization. Fast fluidization is conducted in a riser of a circulating fluidized bed system where solid particles are circulating in a loop. This chapter illustrates the interactive relationship of gas-solid flows in a loop situation by considering the flow behavior of the individual loop components and their effects on the overall gas-solid flow characteristics. Chapter 11 is concerned mainly with the dilute transport or pipe flow of gas-solid suspensions. Some pertinent phenomena such as drag reduction are discussed. Fully developed pipe flow and gas-solid flow in a bend are also illustrated. Chapter 12 describes transport phenomena underlying heat and mass transfer in fluidized systems. Transport models and empirical correlations are introduced to allow heat and mass transfer properties in various fluidized systems to be quantified. An appendix which summarizes the scalar, vector, and tensor notations presented in the text is provided. Throughout the text, unless otherwise noted, the correlation equations presented are given in SI units. Common notations used across the chapters such as superficial gas velocity

and particle Reynolds number are unified. The solution manual for homework problems is available. Interested instructors are urged to contact the publisher about it.

The book is intended to be used in various ways depending on the specific information that the readers desire. While the material is described in a logical sequence chapter by chapter, each chapter is presented with extensive cross-references and maintains reasonable independence. Thus, readers who wish to have a quick grasp of a specific subject may go directly to the relevant chapters. It is important to note that gas—solid flow is a rapidly developing field of research, and that the physical phenomena of gas—solid flows are so complex that a comprehensive understanding of the phenomena is far from complete. Therefore, the present text is also intended to provide readers with ample fundamental concepts to allow them to follow through new developments in the field.

We would like to express our sincere thanks to the following colleagues who have reviewed the text and provided constructive suggestions and overviews: Professor R. S. Brodkey, Professor R. Clift, Professor J. F. Davidson, Dr. R. Davis, Professor N. Epstein, Professor J. R. Grace, Dr. K. Im, Professor B. G. Jones, Professor D. D. Joseph, Dr. C.-H. Lin, Dr. P. Nelson, Dr. S. L. Passman, Professor R. Pfeffer, Professor M. C. Roco, Professor S. L. Soo, Dr. B. L. Tarmy, Professor U. Tüzün, and Professor L.-X. Zhou. We are grateful to Dr. E. Abou-Zeida, Dr. P. Cai, Mr. S. Chauk, Dr. T. Hong, Dr. P.-J. Jiang, Professor J. Kadambi, Dr. T. M. Knowlton, Dr. S. Kumar, Dr. R. J. Lee, and Dr. J. Zhang for their valuable technical assistance in providing information which was incorporated in the text. Special thanks are due to Mr. R. Agnihotri, Dr. D.-R. Bai, Dr. H.-T. Bi, Dr. A. Ghosh-Dastidar, Mr. E.-S. Lee, Dr. S.-C. Liang, Mr. J. Lin, Mr. T. Lucht, Mr. X.-K. Luo, Dr. S. Mahuli, Mr. J. Reese, Mr. S.-H. Wei, Dr. J. Zhang, Mr. T.-J. Zhang, and Mr. J.-P. Zhang, who have read part of the text and have provided valuable comments. The outstanding editorial assistance of Dr. T. Hong and Dr. K. M. Russ is gratefully acknowledged. Thanks are also extended to Dr. E. Abou-Zeida and Mrs. Maysaa Barakat for their excellent drawing of the figures. The inquisitive students in the Chemical Engineering 801 course, Gas-Solid Flows, and the 815.15 course, Fluidization Engineering, taught by the senior author in the Department of Chemical Engineering at the Ohio State University have provided important feedback about the text. Their input is indeed extremely helpful. Financial assistance to this writing project provided by the members of the Ohio State University/Industry Consortium Program on Fluidization and Particulates Reaction Engineering, including Shell Development Co., E. I. duPont de Nemours & Co., Hydrocarbon Research Inc., Exxon Research & Engineering Co., Texaco Inc., and Mitsubishi Chemical Co., is deeply appreciated.

# **Contents**

Preface					χv
Pa	rt I	Basic R	elationships		
1	Size	and Pro	perties of Particles		3
	1.1	Introdu			3
	1.2	Particle	e Size and Sizing Methods		3
		1.2.1	Equivalent Diameters of a Nonspherical Particle		4
		1.2.2	Particle Sizing Methods		10
	1.3		e Size Distributions and Averaged Diameters		17
			Density Functions		18
		1.3.2	Typical Distributions		19
		1.3.3	Averaged Diameters of a Particulate System		23
	1.4		al Properties of Solids		24
		1.4.1	Physical Adsorption		25
		1.4.2	Deformation and Fracture		28
		1.4.3	Thermal Properties		32
		1.4.4	Electrical Properties		35
		1.4.5	Magnetic Properties		37
		1.4.6	Material Densities		38
		1.4.7	Optical Properties		39
		lature			40
	ferenc				42
Pro	blem	S			43
2		ision Me	echanics of Solids		46
	2.1	Introdu			46
	2.2	Stereor	mechanical Impact		47
		2.2.1	Collinear Impact of Spheres		47
		2.2.2	Planar Impact of Spheres		48
	2.3	100 to 10	of Elastic Contact of Solids		49
		2.3.1	General Relations of Stresses in a Solid Medium in Equilibrium	ı	50
		2.3.2	Concentrated Force at a Point in an Infinite Solid Medium		52
		2.3.3	Force on the Boundary of a Semiinfinite Solid Medium		53
		2.3.4	Hertzian Theory for Frictionless Spheres in Contact		59
		2.3.5	Theories for Frictional Spheres in Contact		63
	2.4		on of Elastic Spheres		72
		2.4.1	Normal Collision of Elastic Spheres		72
		2.4.2	Collision of Frictional Elastic Spheres		74

	2.5	Collisi	on of Inelastic Spheres	78				
		2.5.1	Onset of Plastic Deformation	78				
		2.5.2	Restitution Coefficient	80				
No	menc	lature		83				
Re	eferences							
Pre	oblem	s		85				
•			Turnefan and Change Transfer	87				
3		nentum Introdi	Transfer and Charge Transfer	87				
	3.1 3.2		e-Fluid Interactions	87				
	3.2	3.2.1	Drag Force	87				
		3.2.2	Basset Force	88				
		3.2.3	Saffman Force and Other Gradient-Related Forces	95				
		3.2.4	Magnus Effect and Force Due to Rotation of a Sphere	97				
	3.3		article Forces and Field Forces	101				
	3.3	3.3.1	Van der Waals Force	101				
		3.3.2	Electrostatic Force	103				
			Collisional Force	103				
			Field Forces	105				
	2.4	3.3.4		103				
	3.4		n of a Single Particle	107				
		3.4.1	Basset, Boussinesq, and Oseen (BBO) Equation	107				
	2.5	3.4.2	General Equation of Motion	111				
	3.5	_	e Generation and Charge Transfer Static Electrification of Solids	111				
		3.5.1		119				
N.T.		3.5.2	Charge Transfer by Collision	123				
	oblem			126 128				
PI	obiem	is		120				
4	Basi	ic Heat	and Mass Transfer	130				
	4.1	Introd		130				
	4.2		Conduction	130				
		4.2.1	Heat Transfer of a Single Sphere in a Quiescent Fluid	131				
		4.2.2	Heat Conduction in a Collision of Elastic Spheres	133				
	4.3	Conve	ective Heat Transfer	138				
		4.3.1	Dimensional Analysis of Forced Convection in a Single-Phase					
			Flow	138				
		4.3.2	Heat Transfer of a Single Sphere in a Uniform Flow	138				
		4.3.3	Thermal Convection in Pseudocontinuum One-Phase Flow	141				
	4.4	Thern	nal Radiation	142				
		4.4.1	Single-Particle Scattering	143				
		4.4.2	Radiant Heating of a Particle	148				
		4.4.3	General Considerations in Radiation with a Particle Cloud	150				
		4.4.4	Radiation Through an Isothermal and Diffuse Scattering Medium	154				
	4.5	Mass	Transfer	156				
		4.5.1	Diffusion and Convection	156				
		452	Mass and Heat Transfer Analogy	157				

ontents	ix

	menc			159 161		
Re	References					
Pro	blem	S		162		
5	Basi	Basic Equations				
	5.1	Introduction				
		5.1.1	Eulerian Continuum Approach	164		
		5.1.2	Lagrangian Trajectory Approach	165		
		5.1.3	Kinetic Theory Modeling for Interparticle Collisions	166		
		5.1.4	Ergun Equation	166		
		5.1.5	Summary	167		
	5.2	Modeling of Single-Phase Flows				
		5.2.1	General Transport Theorem and General Conservation	167		
		5.2.2	Governing Equations	169		
		5.2.3	Kinetic Theory and Transport Coefficients	170		
		5.2.4	Modeling for Turbulent Flows	174		
		5.2.5	<b>Boundary Conditions</b>	179		
	5.3	Contin	nuum Modeling of Multiphase Flows	182		
		5.3.1	Averages and Averaging Theorems	182		
		5.3.2	Volume-Averaged Equations	189		
		5.3.3	Volume-Time-Averaged Equations	193		
		5.3.4	Transport Coefficients and Turbulence Models	196		
		5.3.5	Boundary Conditions of Particle Phase	205		
	5.4	Trajectory Modeling of Multiphase Flows				
		5.4.1	Deterministic Trajectory Models	206		
		5.4.2	Stochastic Trajectory Models	208		
	5.5	Kineti	c Theory Modeling for Collision-Dominated Dense Suspensions	210		
		5.5.1	Dense-Phase Transport Theorem	211		
		5.5.2	Hydrodynamic Equations	213		
		5.5.3	Collisional Pair Distribution Function	215		
		5.5.4	Constitutive Relations	217		
	5.6	Equat	ions for Flows Through Packed Beds	222		
		5.6.1	Darcy's Law	223		
		5.6.2	Straight Capillaric Model	224		
		5.6.3	Ergun's Equation	225		
	5.7	Dime	nsional Analysis and Similarity	230		
		5.7.1	Scaling Relationships for Pneumatic Transport			
			of Dilute Suspensions	230		
		5.7.2	Scaling Relationships for Fluidized Beds	232		
No	menc	lature		236		
Re	feren	ces		239		
Pro	oblem	s		242		
6	Intri	nsic Ph	enomena in a Gas-Solid Flow	244		
	6.1 Introduction		luction	244		
	6.2	Erosio	on and Attrition	244		
			Ductile Erosion and Brittle Erosion	245		

X Contents

			Locations of Erosive Wear	247			
		6.2.3	Mechanisms of Attrition	252			
	6.3		nodynamic Properties of a Gas-Solid Mixture	254			
		6.3.1	Density, Pressure, and Equation of State	254			
		6.3.2	Internal Energy and Specific Heats	257			
		6.3.3	Isentropic Change of State	258			
	6.4		ure Waves Through a Gas-Solid Suspension	259			
		6.4.1	Acoustic Wave	259			
		6.4.2	Normal Shock Wave	265			
	6.5	Instability					
		6.5.1	Wave Motions in Stratified Pipe Flows	270			
		6.5.2	Continuity Wave and Dynamic Wave	280			
	6.6		le–Turbulence Interaction	285			
	omenc			288			
	eference			292			
Pr	oblem	S		293			
Pa	rt II	Syste	m Characteristics				
7	7.1		eparation luction	297			
	7.1		ation by Rotating Flow	297			
	1.2	7.2.1		297			
		7.2.1	Mechanism and Type of Rotary Flow Dust Separators Flow Field in a Cyclone	297			
		7.2.3	Collection Efficiency of Cyclones	300			
	7.3		rostatic Precipitation	303 309			
	7.5	7.3.1	Mechanism of an Electrostatic Precipitator				
		7.3.2	Migration Velocity and Electric Wind	310			
		7.3.3	Collection Efficiency of Electrostatic Precipitators	311			
	7.4	Filtrat		312 314			
		7.4.1	Mechanisms of Filtration and Types of Filters	314			
		7.4.2	Pressure Drop in a Filter	315			
		7.4.3	Collection Efficiency of Fabric Filters	319			
	7.5		ty Settling and Wet Scrubbing	320			
		7.5.1	Gravity Settling Chambers	321			
		7.5.2	Mechanisms of Scrubbing and Types of Scrubbers	323			
		7.5.3	Modeling for Scrubbing and Collection Efficiency	324			
No	omenc		and concerton Differency	328			
	ferenc			330			
	oblem			331			
8	Hop	per and	Standpipe Flows	333			
	8.1						
	8.2		er Mechanics in Hopper Flows	333 333			
		8.2.1	Mohr Circle for Plane Stresses	334			
		8.2.2	Mohr-Coulomb Failure Criterion and Coulomb Powders	336			
		8.2.3	Static Stress Distributions in Standpipes and Hoppers	337			
			1 1				

Contents xi

		8.2.4	Stress Distribution in a Steady Hopper Flow	340		
		8.2.5	Flowability of Powders in Hopper Design	342		
	8.3	Hoppe	er and Standpipe Flow Theories	346		
		8.3.1	Moving Bed Flows in a Feed Hopper	346		
		8.3.2	Standpipe Flows	350		
		8.3.3	Hopper-Standpipe-Discharger Flow	354		
		8.3.4	Multiplicity of Steady Standpipe Flows	357		
		8.3.5	Leakage Flow of Gas in a Standpipe	359		
	8.4		of Standpipe Systems	361		
		8.4.1	Overflow and Underflow Standpipes	361		
		8.4.2	Inclined Standpipe and Nonmechanical Valves	364		
	menc			366		
	feren			368		
Pr	oblem	S		369		
9	Den	se-Phase	e Fluidized Beds	371		
	9.1	Introd		371		
	9.2		le and Regime Classifications and Fluidized Bed Components	371		
	<b>7.2</b>		Classification of Fluidized Particles	372		
		9.2.2	Fluidization Regimes	374		
		9.2.3	Components in a Dense-Phase Fluidized Bed	376		
	9.3		num Fluidization and Particulate Fluidization	378		
	,	9.3.1	Minimum Fluidization	378		
			Particulate Fluidization	380		
	9.4		ing Fluidization	381		
	· · ·	9.4.1	Onset of Bubbling	381		
		9.4.2	Single Bubble in a Fluidized Bed	382		
		9.4.3	Bubble/Jet Formation and Bubble Coalescence and Breakup	388		
		9.4.4	Bubble/Jet Size and Bubble Rise Velocity	389		
		9.4.5	Gas Flow Division and Bed Expansion	392		
	9.5		lent Fluidization	396		
		9.5.1	Regime Transition and Identification	396		
		9.5.2	Determination of Transition Velocity	398		
		9.5.3	Hydrodynamic Characteristics	399		
	9.6		nment and Elutriation	400		
		9.6.1	Mechanisms of Solids Ejection into the Freeboard	401		
		9.6.2	Correlations and Modeling	402		
	9.7	Slugg	-	403		
		9.7.1	Shapes and Rise Velocities of Single Slugs	403		
		9.7.2	Continuous Slugging	404		
	9.8		ed Beds	406		
		9.8.1	Onset of Spouting	407		
		9.8.2	Maximum Spoutable Bed Depth and Spout Diameter	408		
		9.8.3	Fountain Height	408		
		9.8.4	Gas Flow Distribution	408		
N	omeno	lature		409		
Re	References 41					
	oblen			415		

xii Contents

10	Circulating Fluidized Beds						
		Introduction					
	10.2	System Configuration					
	10.3	•					
		10.3.1	Flow Regimes and Regime Diagrams	423			
		10.3.2	Regime Transition Determination	425			
		10.3.3	Operable Fluidization Regimes	429			
	10.4	Hydrod	ynamic Behavior in a Macroscale	438			
		10.4.1	Axial Profiles of Cross-Sectional Averaged Voidage	438			
		10.4.2	Radial Profiles of Voidage and Solids Flux	440			
		10.4.3	Overall Solids Holdup	442			
	10.5	Local S	olids Flow Structure	443			
		10.5.1	Transient Nature of Solids Flow	444			
		10.5.2	Characterization of Intermittent Solids Flow	445			
	10.6	Mathem	natical Models of Fast Fluidization	447			
		10.6.1	Models Based on the Concept of Cluster	447			
		10.6.2	Models Based on the Core-Annular Flow Structure	448			
		10.6.3	Models Based on the Axial Profiles of Solids Holdup	451			
		10.6.4	Two-Phase Flow Models and Computational Fluid Dynamics	451			
Non	nenclatu			453			
References				455			
Prob	lems			459			
	Pneumatic Conveying of Solids						
11			• •	461 461			
	11.1	Introdu		461			
	11.2		cations of Pneumatic Conveying Systems	461			
		11.2.1	·	461			
		11.2.2	Negative- and Positive-Pressure Pneumatic Conveyings	464			
		11.2.3		464			
		11.2.4	Flow Regimes and Regime Transitions				
	11.3	Pressur	-	466			
		11.3.1	General Pressure Drop in One-Dimensional Flow	467			
		11.3.2	Drag Reduction	469			
		11.3.3	Pressure Drop and Acceleration Length in Developing	470			
		G ::: 1	Regions	472 474			
	11.4		Transport Velocities	474			
		11.4.1	Minimum Transport Velocity				
		11.4.2	Pick-up Velocity	476			
	11.5		n Bends	478			
		11.5.1	Single-Phase Flow in a Curved Pipe	478 481			
	11.6	11.5.2	Particulate Flow in a Bend				
	11.6	•	Developed Dilute Pipe Flows	482			
		11.6.1	Basic Equations and Boundary Conditions	483			
		11.6.2	Characteristic Relations	487			
		11.6.3	Temperature Distributions of Phases	489			
	nenclati	ure		494			
References				496			
Prol	blems			498			

•
1

### **Contents**

12	Heat a	nd Mass	Transfer Phenomena in Fluidization Systems	499	
	12.1	Introdu		499	
	12.2	Suspension-to-Surface Heat Transfer			
		12.2.1		500	
		12.2.2	Film Model	502	
		12.2.3	Single-Particle Model	503	
		12.2.4	Emulsion Phase/Packet Model	506	
	12.3	Heat Tr	ransfer in Dense-Phase Fluidized Beds	512	
		12.3.1	Particle-to-Gas and Bed-to-Gas Heat Transfer	512	
		12.3.2	Bed-to-Surface Heat Transfer	513	
		12.3.3	Effect of Operating Conditions	518	
	12.4 Heat Transfer in Circulating Fluidized Beds		ransfer in Circulating Fluidized Beds	521	
		12.4.1	Mechanism and Modeling	521	
		12.4.2	Radial and Axial Distributions of Heat Transfer Coefficient	524	
		12.4.3	Effect of Operating Parameters	525	
	12.5	Heat Tr	ransfer in Spouted Beds	526	
		12.5.1	Gas-to-Particle Heat Transfer	526	
		12.5.2	Bed-to-Surface Heat Transfer	527	
	12.6	Mass T	ransfer in Multiparticle Gas-Solid Systems	527	
		12.6.1	Mass Transfer in Dense-Phase Fluidized Beds	527	
		12.6.2	Mass Transfer in Circulating Fluidized Beds	532	
Non	enclatu	ıre		532	
Refe	rences			535	
Prob	lems			537	
App	endix:	Summe	ary of Scalar, Vector, and Tensor Notations	540	
Inde	ex			545	

# Basic Relationships