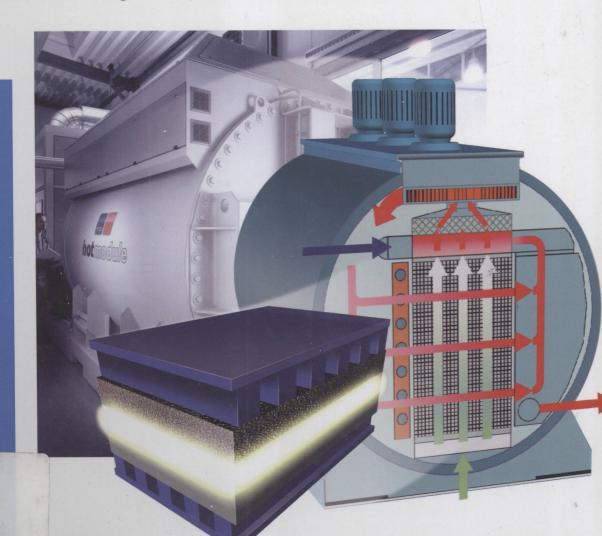
# Molten Carbonate Fuel Cells

Modeling, Analysis, Simulation, and Control



TM911.4 M729

# Molten Carbonate Fuel Cells

Modeling, Analysis, Simulation, and Control

Edited by Kai Sundmacher, Achim Kienle, Hans Josef Pesch, Joachim F. Berndt, and Gerhard Huppmann







WILEY-VCH Verlag GmbH & Co. KGaA

#### The Editors

**Prof. Dr. Kai Sundmacher**Max-Planck-Institut für Dynamik
komplexer technischer Systeme
Sandtorstr. 1
39106 Magdeburg

Germany

Prof. Dr. Achim Kienle Max-Planck-Institut für Dynamik komplexer technischer Systeme Sandtorstr. 1 39106 Magdeburg Germany

Prof. Dr. Hans Josef Pesch
Universität Bayreuth
Lehrstuhl für Ingenieurmathematik
Universitätsstr. 30
95440 Bayreuth
Germany

Dipl.-Ing. Joachim F. Berndt IPF Beteiligungsgesellschaft Berndt KG Carl-Benz-Str. 6 68799 Reilingen

**Dipl.-Phys. Gerhard Huppmann** MTU CFC Solutions GmbH 81663 München Germany

#### Cover Illustration

Germany

Cover photograph with kind permission from MTU CFC Solutions GmbH, Munich, Germany.

All books published by Wiley-VCH are carefully produced. Nevertheless, authors, editors, and publisher do not warrant the information contained in these books, including this book, to be free of errors. Readers are advised to keep in mind that statements, data, illustrations, procedural details or other items may inadvertently be inaccurate.

Library of Congress Card No.: applied for

Bibliographic information published by

**British Library Cataloguing-in-Publication Data** A catalogue record for this book is available from the British Library.

the Deutsche Nationalbibliothek
Die Deutsche Nationalbibliothek lists this
publication in the Deutsche Nationalbibliografie; detailed bibliographic data are
available in the Internet at <a href="http://dnb.d-nb.de">http://dnb.d-nb.de</a>>.

© 2007 WILEY-VCH Verlag GmbH & Co. KGaA, Weinheim

All rights reserved (including those of translation into other languages). No part of this book may be reproduced in any form – by photoprinting, microfilm, or any other means – nor transmitted or translated into a machine language without written permission from the publishers. Registered names, trademarks, etc. used in this book, even when not specifically marked as such, are not to be considered unprotected by law.

Typesetting Asco Typesetters, Hong Kong
Printing Strauss GmbH, Mörlenbach
Binding Litges & Dopf Buchbinderei
GmbH, Heppenheim
Wiley Bicentennial Logo Richard J. Pacifico

Printed in the Federal Republic of Germany Printed on acid-free paper

ISBN: 978-3-527-31474-4

# Molten Carbonate Fuel Cells

Edited by Kai Sundmacher, Achim Kienle, Hans Josef Pesch, Joachim F. Berndt, and Gerhard Huppmann

# 1807-2007 Knowledge for Generations

Each generation has its unique needs and aspirations. When Charles Wiley first opened his small printing shop in lower Manhattan in 1807, it was a generation of boundless potential searching for an identity. And we were there, helping to define a new American literary tradition. Over half a century later, in the midst of the Second Industrial Revolution, it was a generation focused on building the future. Once again, we were there, supplying the critical scientific, technical, and engineering knowledge that helped frame the world. Throughout the 20th Century, and into the new millennium, nations began to reach out beyond their own borders and a new international community was born. Wiley was there, expanding its operations around the world to enable a global exchange of ideas, opinions, and know-how.

For 200 years, Wiley has been an integral part of each generation's journey, enabling the flow of information and understanding necessary to meet their needs and fulfill their aspirations. Today, bold new technologies are changing the way we live and learn. Wiley will be there, providing you the must-have knowledge you need to imagine new worlds, new possibilities, and new opportunities.

Generations come and go, but you can always count on Wiley to provide you the knowledge you need, when and where you need it!

William J. Pesce

President and Chief Executive Officer

Peter Booth Wiley

Chairman of the Board

# **Preface**

Fuel cells generate electrical energy by electrochemical oxidation of chemical substances such as hydrogen, carbon monoxide, methanol, ethanol, glucose or other hydrocarbons. Due to their functional principle, fuel cells can achieve much higher efficiencies for energy conversion than conventional systems which are based on the Carnot cycle. Because of their high conversion efficiency, fuel cells will play a major role in the future mix of power supply systems.

The importance of fuel cells is also reflected by an exponential increase of journal papers and book contributions being published during the last two decades (see Fig. 1). Among the published papers and books, most are focused on polymer electrolyte fuel cells (PEMFC), direct methanol fuel cells (DMFC) and solid oxide fuel cells (SOFC). In comparison to these types of cells, the molten carbonate fuel cell (MCFC) so far has attracted relatively little attention. But this is in total contrast to the current status of system development. While large-scale applications of PEMFC, DMFC and SOFC-systems up to now are still quite rare, more than 20 demonstration plants of the MCFC HotModule type (power range: 250–300 kW) were already installed successfully for various applications by the company CFC Solutions Ltd./Ottobrunn in Germany.

As another trend, the literature analysis clearly reveals that the proportion of publications dealing with the model-based analysis and control of fuel cells is steadily increasing. But this research field is still young and therefore it comprises only about one tenth of the overall number of articles and books in this whole area (see Fig. 1). Designing efficient fuel cell stacks not only requires suitable electrode and membrane materials, but also powerful engineering methodologies and tools. Due to the complex nonlinear behaviour of fuel cells, their design and operation cannot be based on pure intuition. This is why advanced model-based methods for the analysis, control and operation have to be further developed in the next few years.

A comprehensive volume covering all aspects of model-based analysis, control and operation of fuel cell systems is still missing. To fill this gap, the present book was prepared with special focus on the MCFC as an example of high technical relevance. The presented concepts and methods are also transferable to other fuel cell types such as the PEMFC.

Molten Carbonate Fuel Cells. Edited by Kai Sundmacher, Achim Kienle, Hans Josef Pesch, Joachim F. Berndt, and Gerhard Huppmann Copyright © 2007 WILEY-VCH Verlag GmbH & Co. KGaA, Weinheim ISBN: 978-3-527-31474-4

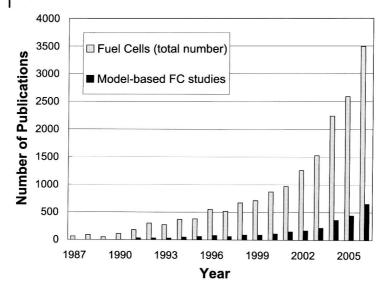


Fig. 1 Journal publications on fuel cells from 1987 to 2006 according to the Science Citation Index.

The book is divided into three parts: Part A surveys the design and operation of MCFC fuel cells with special focus on the HotModule type, which integrates the generation of hydrogen by methane steam reforming and the electrochemical oxidation of hydrogen in one single unit. Part B is dedicated to process analysis by means of mathematical models describing the complex interactions of mass, energy and charge transport phenomena within the fuel cell stack. Part C focuses on how process models can be used for state estimation, for advanced control strategies and for solving steady-state as well as dynamic optimization tasks.

## Part A: Design and Operation

Chapter 1 being written by Gerhard Huppmann, who is one of the inventors of MTU's Carbonate Fuel Cell HotModule, is concerned with the basic concepts and the key features of the cell design, presents possible applications using natural gas and other fuels, and discusses important economical aspects. Focus in Chapter 2 is on Operational Experiences which are reported by Koch et al. The authors collected a series of experimental data at different load scenarios at a 250 kWel MCFC HotModule stack which is installed as part of IPF's power plant at the University hospital in Magdeburg. The data form the basis for the identification of realistic model parameter values being a major prerequisite for reliable fuel cell simulations which are reported in the subsequent chapters.

#### Part B: Model-Based Process Analysis

In Chapter 3, Heidebrecht et al. present a rigorous MCFC reference model which accounts for the most important physico-chemical phenomena within the cell and also for the special recycle structure of the HotModule process. The model consists of a coupled set of hyperbolic and parabolic partial differential equations along with further ordinary differential and algebraic equations, completed by an integral equation expressing the overall charge conservation condition. The numerical treatment of these model equations, using finite volume discretization methods, results in a set of differential-algebraic equations (DAE) whose index analysis is performed by Chudej et al. in Chapter 4.

As outlined by Gundermann et al. in Chapter 5, parameter identification at an industrial-scale MCFC stack requires a special stepwise strategy which has to account for measurement errors as well as for possible leakages at the plant. With regard to cell dynamics, the solid heat capacity is the key parameter to be determined. Once realistic fuel cell model parameters have been identified, one can simulate the steady-state behaviour, particularly the current-voltage performance curve. Furthermore, the process analysis presented by Heidebrecht et al. in Chapter 6 includes the dynamic cell voltage decline after a load increase which can occur when the fuel cell is moved from a low-current operating point to a higher current load.

In Chapter 7, Krasnyk et al. present theoretical predictions of hot spot formation and steady-state multiplicities in high-temperature fuel cells. The discovered phenomena are relevant for the MCFC as well as for the SOFC and arise from the increase of the ion conductivity of electrolytes at increasing operating temperatures.

In the final chapter of part B, Heidebrecht et al. analyse and compare different conceptual designs and reforming concepts by means of a simple along-the-channel anode model. From this study it turns out clearly that the highest current yields are attainable by direct internal reforming within the anode channels.

# Part C: Optimization and Advanced Control

The efficient operation of industrial scale fuel cell plants such as the MCFC Hot-Module requires continuous monitoring of key state parameters. In particular, for safe load changes one would like to know the spatially distributed temperature field within the fuel cell stack. But the experimental accessibility of internal temperatures is quite limited. Therefore, as a very promising monitoring alternative, Grötsch et al. in Chapter 9 show how to develop a model-based observer via model reduction and state estimation for tracing the dynamic evolution of the MCFC temperature field.

The subject of Chapter 10 which was written by Sternberg et al. are optimal control strategies for load changes between two predefined steady-state operating points. The aim of control is to attain the new steady state as fast as possible after load change. This leads to a so-called boundary control problem which can be tackled with the help of the software package NUDOCCCS.

In the final contribution, Heidebrecht et al. show that the optimization of the reforming catalyst distribution can lead to significant improvements of the fuel cell efficiency. Since methane steam reforming is an endothermic reaction, it can be used as an internal cooling element for the exothermic electrochemical reactions.

In the appendix, the complete set of equations and related parameters is given for the MCFC reference model which is the "mother" of all reduced model variants being used for simulation, analysis, control and optimization as discusses in preceding chapters. This information will serve as a source of information for readers who are interested to get all details in order to start their own comparative studies.

## **Book History and Acknowledgements**

The present book presents the outcome of the joint research project "Optimised control of fuel cell systems using methods of nonlinear dynamics" which was performed from 2002 until the end of 2005 in close collaboration of five German research groups from academia and industry. The project was coordinated and organized by the editors of this book and their colleagues at the Otto-von-Guericke-University Magdeburg, the Max-Planck-Institute for Dynamics of Complex Technical Systems in Magdeburg, the University of Bayreuth, the power plant operating company IPF Heizkraftwerksbetriebsgesellschaft Ltd., and the Molten Carbonate Fuel Cell producing company MTU CFC Solutions Ltd. in Ottobrunn. The financial support of the joint project from the Federal Ministry of Education and Research (BMBF) in Germany is very gratefully acknowledged. Intermediate results were discussed in 2004 on a MCFC workshop with financial support from the German Competence Network Pro3 e.V. which is also gratefully acknowledged.

The editors like to thank particularly their colleagues Peter Heidebrecht, Matthias Gundermann, Michael Mangold, Markus Grötsch, Mihai Krasnyk, Kurt Chudej, Kati Sternberg and Mario Koch for their excellent support during the project work and in preparing the manuscripts being the basis for the present book publication. Last but not least, we are very thankful to Dr. Rainer Münz from Wiley-VCH for his helpful assistance during the production of this book.

March 2007

Kai Sundmacher, Achim Kienle, Hans-Josef Pesch, Joachim Berndt, Gerhard Huppmann

# **List of Contributors**

## Joachim F. Berndt

IPF Beteiligungsgesellschaft Berndt KG Postfach 1110 68795 Reilingen Germany joachim.berndt@ipf-online.com

## Kurt Chudei

Lehrstuhl für
Ingenieurmathematik
Universität Bayreuth
Universitätsstraße 30
95440 Bayreuth
Germany
kurt.chudej@uni-bayreuth.de

#### Markus Grötsch

Max-Planck-Institut für Dynamik komplexer technischer Systeme Sandtorstraße 1 39106 Magdeburg Germany groetsch@mpi-magdeburg.mpg.de

# Matthias Gundermann

Process Systems Engineering
Lehrstuhl für Systemverfahrenstechnik
Otto-von-Guericke Universität
Magdeburg
Universitätsplatz 2
39106 Magdeburg
Germany
matthias.gundermann@vst.unimagdeburg.de

## Peter Heidebrecht

Max-Planck-Institut für Dynamik komplexer technischer Systeme Sandtorstraße 1 39106 Magdeburg Germany heidebrecht@mpi-magdeburg.mpg.de

## Gerhard Huppmann

Christa-McAuliffe-Straße 1 Ottobrunn 81663 München Germany gerhard.huppmann@mtu-cfc.com

MTU CFC Solutions GmbH

Molten Carbonate Fuel Cells. Edited by Kai Sundmacher, Achim Kienle, Hans Josef Pesch, Joachim F. Berndt, and Gerhard Huppmann Copyright © 2007 WILEY-VCH Verlag GmbH & Co. KGaA, Weinheim ISBN: 978-3-527-31474-4

#### Achim Kienle

Max-Planck-Institut für Dynamik komplexer technischer Systeme Lehrstuhl für Automatisierungstechnik/ Modellbildung Otto-von-Guericke-Universität Magdeburg Universitätsplatz 2 Germany kienle@mpi-magdeburg.mpg.de

#### Mario Koch

IPF Heizkraftwerksbetriebsgesellschaft mbH Brenneckestraße 4B Magdeburg Germany

## Michael Krasnyk

Max-Planck-Institut für Dynamik komplexer technischer Systeme Sandtorstraße 1 39106 Magdeburg Germany miha@mpi-magdeburg.mpg.de

## Michael Mangold

Max-Planck-Institut für Dynamik komplexer technischer Systeme Sandtorstraße 1 39106 Magdeburg Germany

## Hans Josef Pesch

Lehrstuhl für Ingenieurmathematik Universität Bayreuth Universitätsstraße 30 95440 Bayreuth Germany hans-josef.pesch@uni-bayreuth.de

## Joachim Rang

Institut für Wissenschaftliches Rechnen Technische Universität Braunschweig 38092 Braunschweig Germany

## Min Sheng

Max-Planck-Institut für Dynamik komplexer technischer Systeme Sandtorstraße 1 39106 Magdeburg Germany

# Kati Sternberg

Lehrstuhl für Ingenieurmathematik Universität Bayreuth Universitätsstraße 30 95440 Bayreuth Germany

#### Kai Sundmacher

Max-Planck-Insitute for Dynamics of Complex Technical Systems Sandtorstraße 1 39106 Magdeburg Germany sundmacher@mpi-magdeburg.mpg.de

# **Further Reading**

Sundmacher, K., Kienle, A., Seidel-Morgenstern, A. (Eds.)

# **Integrated Chemical Processes**

Syntheses, Operation, Analysis, and Control

2005

Hardcover

ISBN: 978-3-527-30831-6

Olah, G. A., Goeppert, A., Prakash, G. K. S.

# Beyond Oil and Gas: The Methanol Economy

2006

Hardcover

ISBN: 978-3-527-31275-7

Elvers, B. (Ed.)

# Handbook of Fuels

**Energy Sources for Transportation** 

2007

Hardcover

ISBN: 978-3-527-30740-1

Häring, W. (Ed.)

# **Industrial Gases Processing**

2007

Hardcover

ISBN: 978-3-527-31685-4

Vielstich, W., Lamm, A., Gasteiger, H. (Eds.)

# Handbook of Fuel Cells

Fundamentals, Technology, Applications

4 Volumes

2003

Hardcover

ISBN: 978-0-471-49926-8

# **Contents**

Preface	XI

# List of Contributors XV

Part I Design and Operation 1	Part I	Design	and	Operation	1
-------------------------------	--------	--------	-----	-----------	---

1	MTU's Carbonate Fuel Cell HotModule 3 Gerhard Huppmann
1.1	The Significance of Fuel Cells 3
1.2	Basic Statements of Power Production and Combined Heat and Power Systems 4
1.3	Fuels for Fuel Cells 5
1.3.1	Fuels Containing Gaseous Hydrocarbons 5
1.3.2	Synthesis Gases 6
1.3.3	Group of Gasified Hydrocarbons 7
1.3.4	Secondary Fuel 7
1.4	Why Molten Carbonate Fuel Cells 7
1.5	The Carbonate Fuel Cell and its Function 8
1.6	Optimisation by Integration: The HotModule Concept 11
1.7	Manufacturing 12
1.8	Advantages of the MCFC and its Utilization in Power Plants 13
1.8.1	Electrical Efficiency 13
1.8.2	Modularity 13
1.8.3	Inherent Safety 15
1.8.4	Environmentally Friendly – Pollution Free 16
1.8.5	Silent 16
1.9	History 16
1.9.1	The European MCFC Development Consortium 16
1.9.2	Continuing of the HotModule Development at MTU CFC Solutions 17
1.10	Possible Applications of MCFC Systems 20
1.10.1	Different Applications Using Different Fuels 20

٧ı	Contents	
•		_

Different Applications Using the Different Products of the MCFC System 23 Economical Impacts 25
Operational Experiences 27 Mario Koch, Joachim Berndt, and Matthias Gundermann
Combined Heat and Power Plant of the Company IPF in Magdeburg 27 The HotModule in Magdeburg 27 Operation Experience 30 Results and Outlook 32
Model-based Process Analysis 33
MCFC Reference Model 35 Peter Heidebrecht, and Kai Sundmacher
Model Hierarchy 35 General 36 Model Equations 40 Indirect Internal Reformer 41 Anode Channel 43 Combustion Chamber 45 Reversal Chamber 48 Cathode Channels 49 Electrode Pores 51 Solid Phase 53 Electric Potential 55 Reaction Kinetics 57 Thermodynamics 59 Summary 61 Bibliography 61
Index Analysis of Models 63 Kurt Chudej, Hans Josef Pesch, and Joachim Rang
Differential Time Index 63  MOL Index 68 Perturbation Index 69 Transformation to Homogenous Dirichlet Boundary Conditions 69 Abstract Problem 70 Perturbation Index 70 Garding-Type Inequality 71 Estimate for $v$ and $\bar{v}$ 71 Estimate for $u$ , $w$ and $\bar{w}$ with Garding-Type Inequality 72 Conclusion 73 Bibliography 73

5	Parameter Identification 75  Matthias Gundermann and Kai Sundmacher
5.1	Experimental Work 75
5.1.1	Measurement of Cell Current and Cell Voltage 76
5.1.2	Temperature Measurement 76
5.1.3	Measurement of Concentrations 79
5.1.4	Measurement of Flow Rates 80
5.1.5	Conversion of the Measurements into Dimensionless Values 81
5.1.6	Measurement Errors 81
5.1.7	Measuring Campaigns 83
5.2	Strategy for Parameter Estimation 84
5.2.1	Determination of Relevant Parameters 84
5.2.2	Balancing of the Fuel Cell Plant 86
5.2.3	Sensitivity Analysis 93
5.2.4	Parameter Estimation for a Single Load Case 97
5.2.5	Parameter Estimation for the Whole Operating Range 99
5.2.6	Temperature Dynamics 103
5.3	Results of the Parameter Identification 104
5.3.1	Steady State Measurements 104
5.3.2	Plant Balancing and Error Minimisation 107
5.3.3	Parameter Estimation 109
5.3.4	Dynamic Measurements 113
5.3.5	Estimation of the Solid Heat Capacity 116
5.3.6	Evaluation of the Results 117
5.4	Summary 122
	Bibliography 123
6	Steady State and Dynamic Process Analysis 125 Peter Heidebrecht, Matthias Gundermann, and Kai Sundmacher
6.1	Steady State Simulation 125
6.2	Current–Voltage Curve 132
6.3	Transient Simulation 133
6.4	Summary 139
	Bibliography 140
7	Hot Spot Formation and Steady State Multiplicities 141 Michael Krasnyk, Michael Mangold, Achim Kienle, and Kai Sundmacher
7.1	Introduction 141
7.1	Models Nonlinear Analysis 143
7.2.1	
7.2.1	Spatially Distributed Model 143 Lumped Model 145
7.2.2	
7.4	
/ · T	Analysis of the Spatially Distributed FC Model 152

vIII	Contents		
1	7.5 7.6 7.7 7.7.1 7.7.2 7.3.3	Analysis of a More General High Temperature Fuel Cell Model Conclusions 157  Appendix: Model Equations for Nonlinear Analysis 158  Equations of the Spatially Distributed Model 158  Equations of the Lumped Model 161  Model Parameters 162  Bibliography 162	154
	8	Conceptual Design and Reforming Concepts 165 Peter Heidebrecht and Kai Sundmacher	
	8.1 8.1.1 8.1.2 8.1.3 8.2 8.2.1 8.2.2 8.2.3 8.2.4 8.3	Steady State Anode Model 166 General 166 Equations 167 Conversion Diagram 170 Applications of the Steady State Anode Model 173 Comparison of Reforming Concepts 173 Fuel Cell Cascades 175 Anode Exhaust Gas Recycling 178 Fuel Gas Sidefeed 179 Summary 181 Bibliography 182	
	Part III	Optimization and Advanced Control 183	
	Part III	Optimization and Advanced Control 183  Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle	
		Model Reduction and State Estimation 185	
	9	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle	
	<b>9</b> 9.1	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188	
	9.1 9.2 9.2.1 9.2.2	Model Reduction and State Estimation 185 Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle Introduction 185 Development of a Nonlinear Reduced Model 186 Choice of Basis Functions 188 Treatment of Boundary Conditions 190	
	9.1 9.2 9.2.1 9.2.2 9.2.3	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4 9.5	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193  Simulation Results 196	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4 9.5 9.6	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193  Simulation Results 196  Experimental Results 196  Conclusions 197	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4 9.5 9.6 9.7	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193  Simulation Results 196  Experimental Results 196  Conclusions 197  Bibliography 199  Optimal Control Strategies 201	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4 9.5 9.6 9.7	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193  Simulation Results 196  Experimental Results 196  Conclusions 197  Bibliography 199  Optimal Control Strategies 201  Kati Sternberg, Kurt Chudej, and Hans Josef Pesch	
	9.1 9.2 9.2.1 9.2.2 9.2.3 9.3 9.4 9.5 9.6 9.7	Model Reduction and State Estimation 185  Markus Grötsch, Michael Mangold, Min Sheng, and Achim Kienle  Introduction 185  Development of a Nonlinear Reduced Model 186  Choice of Basis Functions 188  Treatment of Boundary Conditions 190  Resulting Reduced Model of the HotModule 191  Investigation of Observability 192  Design of an Extended Kalman Filter 193  Simulation Results 196  Experimental Results 196  Conclusions 197  Bibliography 199  Optimal Control Strategies 201  Kati Sternberg, Kurt Chudej, and Hans Josef Pesch  Model and Simulation Setting 202	

11	Optimisation of Reforming Catalyst Distribution 211 Peter Heidebrecht and Kai Sundmacher
11.1	Introduction 211
11.2	Objective Functions and Optimisation Parameters 212
11.3	Numerical Aspects 214
11.4	Results 216
11.4.1	Optimisation of Input Conditions at Constant Catalyst Density 216
11.4.2	Optimisation of the Reforming Catalyst Density Distribution 218
11.4.3	Optimisation of the Input Conditions for a System with Optimised
	Catalyst Density 219
11.5	Summary 220
	Bibliography 220
	Appendices 221
A	List of Symbols 223
В	<b>Benchmark Problem: Complete Set of Equations and Parameters</b> 227 Peter Heidebrecht
B.1	Equations 227
B.2	Parameters 227
	Index 235