Solutions Manual to accompany

and Geotechnical Properties of Soils

JOSEPH E. BOWLES

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Physical and Geotechnical Properties of Soils

JOSEPH E. BOWLES

Professor of Civil Engineering Bradley University

SOLUTIONS MANUAL

for

Physical and Geotechnical Properties of Soils

To User: I have assembled a set of solutions for all of the problems which are not "opinion" problems for which a number of answers may be acceptable.

I have not included "solutions" for discussion questions since these must be read by the instructor on an individual basis.

I have not included any "solutions" where the student is asked to verify the text example. Most derivations include a solution unless the solution is given in the text and the student is asked to derive the equation already given.

These solutions are in a format suitable for separation and inclusion in the back of the instructors lecture notes (notebook) for ready reference and pull-out for grading.

I have included more steps than is usually given in "solutions manuals" and by typing for appearance some typing errors may have crept in. I have made a reasonable check for correctness and the answers should be correct. Missing parenthesis or misplaced parenthesis, while being nuisances, should not detract from the manual's value as a teaching aid.

Joseph E. Bowles

ERRATA Physical and Geotechnical Properties of Soils (1st printing as of December 1978).

p. 25 Change to read as follows:

.....will investigate at a sample population of N = 1 test which requires interpolation to obtain

$$n = 0.726 + 0.5(1.376 - 0.726) = 1.051 \text{ say, } 1.0$$

In other words \underline{one} test gives an approximate 75 percent reliability that any single test will be 19.86 \pm 2.128 percent for our example.

(rest of page is 0.K.)

- p. 29 In Eq. (a) $V_W = W_W/G_W\gamma_W = W_W$
- p. 52 In Problem 2-3: Change: Ex. 2-1 to Ex. 2-3. (see solutions manual)
- p. 93 5 lines from top: No. 0 to No. $\underline{4}$
- p. 212 Delete Eq. (8-9) number from Eq. numbered for k_2 .
- p. 232 In Prob. 8-10 change Fig. 8-14 to Fig. 8-15.
- p. 270 In Prob. 9-3: Change 3.6 to 4.0 m and 10 to 13 m (see solutions manual)
- p. 283 Last line: Fig. 6-10b to Fig. 6-10.
- p. 284 In Eq. (10-9) change (+) to (-).
- p. 297 10 lines from top: $\epsilon_i =(1 \exp(-1.5t))$
- p. 352 Change: $s = P_v/A_o$ and $\sigma_n = P_h/A_o$ to $s = P_h/A_o$ and $\sigma_n = P_v/A_o$.
- p. 456 In Example 16-3. Column headed P_p : 4628 2876 1835 1684 are revised values. Replotting results in F = 1.9 instead of 2.1
- p. 458 Answers for 16-4 and 16-6 are mixed--see solutions manual for correct values and order for all points.

1-1. Given: A material has a density of 1.76 g/cm³.

Required: Unit weight in fps and SI.

Solution:

fps: $\gamma = 1.76x62.4 = 109.8 \text{ pcf}$

SI: $\gamma = 1.76 \times 9.807 = 17.26 \text{ kN/m}^3$

1-2. Given: A soil sample has a diam. = 62.3 mm.

Required: area in fps and SI.

Solution:

diam = 62.3/25.4 = 2.543 in

fps: $A = 0.7854(2.453)^2 = 4.276$ sq in

SI: $A = 0.7854(6.23)^2 = 30.48 \text{ sq cm}$

= 4048 sq mm

= 0.003048 sq m

1-3. Given: Compaction test data as follows:

$$\gamma = 17.3$$
 17.1 17.7 kN/m³
18.4 16.9 18.1
17.9 17.2 18.0
18.3 17.0 17.9

Required: mean unit weight, γ.

 $\bar{\sigma}$ (standard deviation)

C (coefficient of variance)

Estimate of percent chance single test will be within $\pm \bar{\sigma}$.

Solution:

$$\gamma_{\text{mean}} = \bar{X} = \frac{\Sigma V}{N} = \frac{17.3 + 17.1 \dots + 17.9}{12} = \frac{211.8}{12} = \underline{17.65 \text{ kN/m}}^3$$

Find $\bar{\sigma}$:

$$\gamma$$
 $\Delta = \gamma_1 - \bar{\chi}$
 γ
 Δ
 0.05
 17.7
 0.05
 18.1
 0.45
 17.9
 0.25
 17.9
 0.25
 $\Sigma V^2 = 3741.32$
 $N(17.65)^2 = 3738.27$

$$\bar{\sigma} = ((3741.32 - 3738.27)/12)^{\frac{1}{2}} = 0.504 \text{ kN/m}^3$$

Find coefficient of variance:

$$\bar{C} = \bar{\sigma}/\bar{X} = 0.504/17.65 = 0.02856$$

Percent chance any single test will be within standard deviation:

Actual range =
$$17.65 \pm 0.504 = 18.15$$
 say 18.2 = 17.15 say 17.2

In range = 7 tests
Out or range = 5 tests

% reliability =
$$\frac{7}{12} \times 100 = \frac{58 \text{ percent}}{100}$$

From Table 1-2 and interpolating for N=12 tests for n=1R=0.810+0.026=0.826=82.6 percent reliable Correlation is very poor. 1-4. Given the following series of plastic limit water content values:

Test No.	w _p , %	Test No.	w _P , %
1.	24.3	5	19.3
2	26.2	6	24.2
3	18.1	7	23.8
4	24.1	8	25.1
		9	24.9

Required: Mean water content, \bar{X}

Standard deviation $\bar{\sigma}$

Coefficient of variance \bar{C} Percent reliability R

Solution:

$$W_{P(mean)} = \bar{X} = \frac{\Sigma V}{9} = \frac{210}{9} = \underline{23.3 \%}$$

$$\bar{\sigma}^2 = \frac{\Sigma V^2 - N\bar{X}^2}{N} = \frac{4959.94 - 4900}{9} = 6.66$$

$$\bar{\sigma} = (6.66)^{\frac{1}{2}} = \underline{2.58 \%}$$

$$\bar{C} = 2.58/23.3 = 0.11$$

Finding percent reliability:

N = 9: 1.383 (1.00) 0.883

$$\Delta R = 1.383 - 0.883 = 0.500$$
 $1.000 - 0.883 = 0.117$

R = 0.80 + 0.1(0.117)/0.5 = 0.823 or 82.3 %

Actual percent reliability:

No. tests inside $\bar{X} \pm 2.58 = 6$

Actual percent = $6/9 \times 100 = 67 \text{ percent.}$

Again correlation is not too good.

If the two extreme points are discarded the theoretical and actual reliability converges......

1-5. Estimate the minimum number of tests to give R = 85 percent (0.85) that a single test

$$V = \bar{X} \pm \bar{\sigma}$$

Solution: This is a case where n = 1.0

It is required to find N

Since 0.85 = (0.90 + 0.80)/2Find where $R_{0.9} + R_{0.8} = 2.00$

Find where
$$R_{0.9} + R_{0.8} = 2.00$$

At N = 105: $R_{0.9} = 1.290$
 $R_{0.8} = 0.845$
 $0.8 = 0.845$

Therefore it will take more than 105 tests

1-6. What is the best (minimum) value of k to give

$$V = \bar{X} \pm k\bar{\sigma}$$

with 92 percent reliability for not more than 10 tests?

Solution:

At N = 10

R.90 = 1.372

R.92 = _____ 1.552 (from below)

R.95 = 1.813

$$\Delta R = (\frac{1.813 - 1.372}{0.05})0.02 = 0.18$$

k = 1.372 + 0.18 = 1.552

2-4. Given: Sample of clay
$$V_T = 105.0 \text{ cm}^3$$
; Weight of sample in natural state = 143.0 g; Weight of dry sample = 111.3 g. Assume $G_c = 2.70$.

Required: What is natural moisture content of clay, w_N ?

What is degree of saturation, S?

Solution:

$$W_N = \frac{W_W}{W_S}(100) = \frac{143.0 - 11.3}{111.3}(100) = 31.7(100)/111.3 = \underline{28.5 \%}$$

Finding degree of saturation, S:

$$V_S = W_S/(G_S Y_W) = 111.3/(2.70 \times 1) = 41.22 \text{ cm}^3$$

$$V_V = V_T - V_S = 105.0 - 41.22 = 63.78 \text{ cm}^3$$

$$V_W = W_W = 31.7 \text{ cm}^3$$

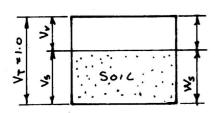
$$S = \frac{V_W}{V_V}(100) = 31.7(100)/63.78 = \frac{49.7 \%}{49.7 \%}$$

2-5. Given:
$$\rho_{dry} = 1.73 \text{ g/cm}$$
; Void ratio, e = 0.55

Required: γ_{wet} at S = 50 %

 γ_{wet} at S = 100 %

 $^{\gamma}$ wet at S = 100 % using oil at $_{0il}$ = 0.90



$$e = V_v/V_s = 0.55$$
 $V_v = 0.55V_s$
 $V_T = V_v + V_s = 1.00$
 $0.55V_s + V_s = 1.00$
 $V_s = 1/1.55 = 0.645 \text{ cm}^3 \text{ (or ft}^3 \text{ or m}^3 \text{)}$
 $V_v = 1 - V_s = 1 - 0.645 = 0.355 \text{ cm}^3$

$$\rho_{.50} = 1.73 + 0.5(0.355)(1) = 1.91 \text{ g/cm}^3$$

$$\gamma = 1.91 \times 9.807 = 18.73 \text{ kN/m}^3$$

$$\rho_{100} = 1.73 + 1.0(0.355)(1) = 2.09 \text{ g/cm}^3$$

$$\gamma = 20.50 \text{ kN/m}^3$$

Using oil at $G_0 = 0.90$

$$\rho_{100} = 1.73 + 1.0(0.355)(0.9) = 2.05 \text{ g/cm}^3$$

$$\gamma_0 = 2.05 \times 9.807 = 20.10 \text{ kN/m}^3$$

2-6. Given: A saturated clay. Water content w = 160 percent; $G_s = 2.40$.

Required: Ydry and Ysaturated.

Solution: (refer to sketch)

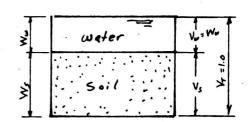
Assume $V_T = 1.00$

$$V_{s} + V_{v} = 1.00$$

$$V_s = W_s/(G_{s w}) = W_s/G_s$$

$$V_{w} = V_{v} = W_{w}/G_{w} = W_{w}$$

$$W_W = WW_S = 1.60W_S = V_W$$



Substituting:

$$1.60W_{S} + W_{S}/G_{S} = 1.00 \rightarrow 1.60(2.40)W_{S} + W_{S} = 1.0(2.40)$$

$$W_{S} = 2.40/4.84 = 0.496 g$$

$$W_{W} = wW_{S} = 1.60(0.496) = 0.793 g$$

$$W_{T} = W_{S} + W_{W} = 0.496 + 0.793 = 1.289 g$$

$$\rho = 1.289/1 = 1.289 g/cm^{3}$$

$$\gamma_{Sat} = 1.289x9.807 = 12.64 kN/m^{3}$$

$$\gamma_{dry} = 0.496 \times 9.807/1 = 4.86 kN/m^{3}$$

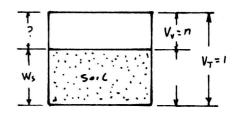
2-7. Given: G_s , n, γ_w .

Required: Derive an expression for γ_{dry} .

Solution: (refer to sketch)

Assume
$$V_T = 1.00$$

 $n = V_V/V_T = V_V/1.0 = V_V$
 $V_S = V_T - V_V = 1 - n$
 $W_S = V_S G_S Y_W = G_S Y_W (1-n)$
 $Y_{dry} = W_S/V_T = W_S/1 = W_S = G_S Y_W (1-n)$



2-8. Required: Derive an expression for
$$\gamma_{sat} = f(G_s, e, \gamma_w)$$

Solution:

Let
$$V_{S} = 1.0$$
; $e = V_{V}/V_{S} = V_{V}/1.0 = V_{V}$
 $V_{T} = V_{S} + V_{V} = 1 + e$
 $W_{W} = V_{V}G_{W}Y_{W} = eG_{W}Y_{W} = eY_{W}$
 $W_{S} = G_{S}V_{S}Y_{W} = G_{S}Y_{W}$
 $W_{T} = W_{W} + W_{S} = eY_{W} + G_{S}Y_{W} = (G_{S} + e)Y_{W}$
 $Y_{Sat} = W_{T}/V_{T} = \frac{(G_{S} + e)}{1 + e}Y_{W}$

2-9. Required: Derive an expression for
$$e = f(\gamma_{sat}, \gamma_{w}, w)$$

Solution:

e =
$$V_V/V_S$$
 for S = 100 percent: $V_V = V_W = W_W/\gamma_W = wW_S/\gamma_W$
 $V_S = 1 - V_V = 1 - wW_S/\gamma_W$

Substituting for e:

$$e = \frac{wW_s/\gamma_w}{1 - wW_s/\gamma_w} = \frac{wW_s}{\gamma_w - wW_s}$$

$$Now W_T/1.0 = \gamma_{sat} = W_s + W_w = W_s + wW_s$$

$$therefore: W_s = \gamma_{sat}/(1 + w)$$

$$e = \frac{w\gamma_{sat}/(1 + w)}{\gamma_w - w\gamma_{sat}/(1 + w)} = \frac{w\gamma_{sat}}{\gamma_w - (\gamma_{sat} - \gamma_w)w}$$

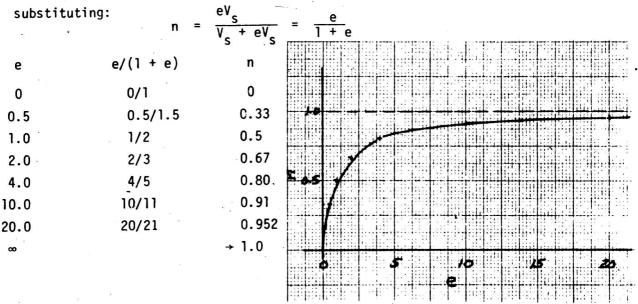
Valid for: $\gamma_{sat} = kN/m^3$, pcf or g/cm³

2-10. Required: Plot a curve of n = f(e).

Solution:

$$n = V_v/V_t$$
 $e = V_v/V_s$ $V_v = eV_s$
 $V_T = V_v + V_s = eV_s + V_s$

substituting:



2-11. Required: Prove that $e = wG_s$ for S = 100 %.

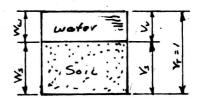
Solution: Refer to sketch.

$$e = V_{v}/V_{s} \quad \text{but } V_{s} = W_{s}/G_{s}\gamma_{w}$$

$$S = V_{w}/V_{v}$$

$$V_{v} = 1.0 - V_{s} = V_{w}/S$$

$$V_{w}/S = wW_{s}/(SxG_{w}x\gamma_{w})$$



From which
$$e = wW_s/(SxG_wY_wXV_s) = wG_sW_sY_w/(SxG_wY_wXW_s) = wG_s/(SG_w)$$

Noting $G_w = 1.0$
 $e = wG_s/S$ but if $S = 1.0$
 $e = wG$

2-12. Given: Data from a \mathbf{w}_{L} test.

34 28 20

w% 68.0 60.1 54.3

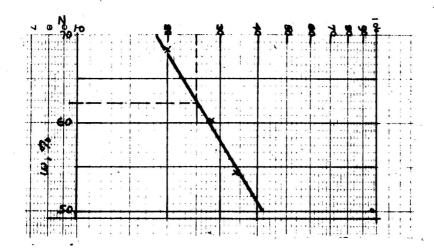
 w_p = 28.6 and 29.1 percent (2 tests); w_N = 78.0 percent.

Required: Liquid and plastic limits for soil

Liquidity index and Consistency index

Make appropriate comments on soil in natural state

Solution: Plot water content data for liquid limit tests as shown and obtain \mathbf{w}_{L} .



from plot above $w_L = 62.8$ percent From plastic limit data $w_p = (29.1 + 28.6)/2$ 28.9 percent.

$$I_p = 62.8 - 28.9 = 33.9$$

$$I_p = 62.8 - 28.9 = 33.9$$

$$I_L = \frac{w_N - w_P}{I_p} = \frac{78.0 - 28.9}{33.9} = 1.448$$

$$I_C = (w_L - w_N)/I_P = (62.8 - 78.0)/33.9 = -0.448$$

The in situ soil is in a potentially unstable state since any remolding will convert it into a viscous fluid.

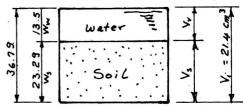
2-13. Given: Sample of saturated clay:
$$V_i = 21.4 \text{ cm}^3$$
 $V_{dry} = 13.7 \text{ cm}^3$ $W_i = 36.7 \text{ g}$ $W_{dry} = 23.2 \text{ g}$

Required: In <u>natural</u> state find: (a) w_N ; (b) G_S ; (c) Void ratio, e;

(d) γ_{sat} ; (e) γ_{dry} ; (f) Shrinkage limit w_S

Solution: Refer to sketch

(a) Natural water content w_N : $w_N = \frac{36.7 - 23.2}{23.2} = \frac{13.5}{23.2}(100) = \frac{58.2 \%}{23.2}$



(b) Find specific gravity G_c :

Since
$$W_W = V_W = 13.5 \text{ g} = 13.5 \text{ cm}^3$$

 $V_S = V_t - V_W = 21.4 - 13.5 = 7.9 \text{ cm}^3$
 $G_S = W_S/(V_S Y_W) = 23.2/(7.9 \times 1.0) = 2.94$

(c) Find void ratio e:

$$e = V_v/V_s = 13.5/7.9 = 1.709$$

(d) Find saturated unit weight

$$\gamma_{\text{sat}} = W_{\text{t}}/V_{\text{t}} = 36.7(9.807)/21.4 = 16.82 \text{ kN/m}^3$$

(e) Find dry unit weight

$$\gamma_{drv} = W_s/V_t = 23.2(9.807)/21.4 = 10.63 \text{ kN/m}^3$$
 (based on natural state)

(f) Shrinkage limit w_s

$$\Delta V$$
 to $w_S = 21.4 - 13.7 = 7.7 \text{ cm}^3 = \Delta W_W = 7.7 \text{ g}$

$$V_S \text{ at } w_S = 13.7 - H_2 0 \text{ in soil} \rightarrow H_2 0 \text{ in soil} = 13.5 - 7.7 = 5.8 \text{ g}$$

$$V_S = 13.7 - 5.8 = 7.9 \text{ cm}^3 \text{ (as before and checks)}$$

$$w_S = W_W / W_S = 5.8(100) / 23.2 = 25 \%$$

2-14. Given: Soil specimen with $V = 60.0 \text{ cm}^3$

$$W_{t} = 105.0 g$$

$$W_s = 80.2 \text{ g (after drying); } G_s = 2.65$$

Required: (a) water content w; (b) void ratio e; (c) porosity n;

(d) G_{mass}; (e) degree of Saturation S.

Solution: Refer to sketch

(a) Water content

$$w = \frac{105.0 - 80.2}{80.2}(100) = 24.8(100)/80.2$$

$$w = 30.9 \%$$

(b) Void ratio

$$V_s = W_s/(G_s \gamma_w) = 80.2/2.65 = 30.26 \text{ cm}^3$$

 $V_v = V_t - V_s = 60.0 - 30.26 = 29.74 \text{ cm}^3$

$$e = V_v/V_s = 29.74/30.26 = 0.983$$

(c) Porosity n

$$n = V_V/V_{\uparrow} = 29.74/60.0 = 0.496$$

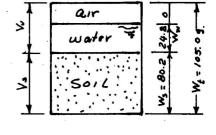
(d) Specific gravity of mass (not grains)

$$G_{m} = W/(Vx\gamma_{W}) = 105/(60.0x1.0) = 1.75$$

(e) degree of Saturation S

$$V_W = W_W/(G_W Y_W) = 24.8/(1x1) = 24.8 \text{ cm}$$

 $S = V_W(100)/V_V = 24.8(100)/29.74 = 83.4 \%$



2-15. Given: Medium graded damp sand ρ = 1.77 g/cm . The water content w = 15.1 %.

Required: (a) void ratio e; (b) dry unit weight γ_{dry} ; (c) degree of Saturation S.

Solution: (refer to sketch)

It is necessary to assume $G_s = 2.65$

(a) Void ratio

$$W_t = W_s + W_w = 1.77$$

 $w = W_w/W_s = 0.151$
 $W_s + 0.151W_s = 1.77$
 $W_s = 1.77$

$$W_s = 1.77/1.151 = 1.538 g$$

$$V_s = W_s/(G_s \gamma_w) = 1.538/(2.65 \times 1) = 0.580 \text{ cm}^3$$

 $V_v = 1.0 - 0.580 = 0.420 \text{ cm}^3$

$$e = V_v/V_s = 0.420/0.580 = 0.724$$

(b) Dry unit weight

Since the volume = 1.00

$$\gamma_{dry} = W_s(9.807/1 = 1.538(9.807) = 15.08 \text{ kN/m}^3$$

(c) Degree of Saturation

$$S = V_w^{(100)}/V_v$$

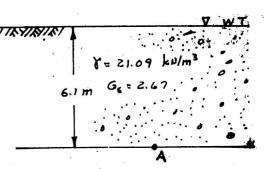
$$V_w = W_w = W_t - W_s = 1.770 - 1.538 = 0.232 \text{ g (or cm}^3)$$

$$S = 0.232(100)/0.420 = 55.2 \%$$

2-16. Given: Soil profile shown

Required: (a) σ' at point A

- (b) σ' and σ_{tot} if water table falls to a and with w = 10 percent in soil.
- (c) Redo "b" in fps units.



(a) σ' at A:

Obviously the unit weight shown is the saturated weight since it is below water table with no qualifying remarks.

$$\sigma' = h(\gamma_{sat} - \gamma_w) = 6.1(21.09 - 9.807) = 68.83 \text{ kPa}$$

(b) σ' and γ_{tot} if water table falls and water content in soil = 10 %.

$$\gamma_{\text{wet}}$$
: $V_s + V_w = 1 \text{ cm}^3$

$$W_s + W_w = 21.09/9.807 \rightarrow W_w = 2.15 - W_s$$
but $W_w = V_w$ in cgs units

Substituting:

$$W_{s}/G_{s} + 2.15 - W_{s} = 1.0$$

$$W_{s} - W_{s}/2.67 = 2.15 - 1.0$$

$$0.6255W_{s} = 1.15$$

$$W_{s} = 1.839 \text{ g}$$
Check: $V_{s} = W_{s}/G_{s} = 1.839/2.67 = 0.689 \text{ cm}^{3}$

$$V_{v} = 1 - V_{s} = 0.311 \text{ cm}^{3}$$

$$W_{t} = (1.839 + 0.311)9.807 = 21.09 \text{ kN/m}^{3} = 0.689 \text{ cm}^{3}$$

The weight of wet soil: $\gamma_{wet} = \gamma_{dry} + w\gamma_{dry} = 1.839(1.10)9.807 = 19.81 \text{ kN/m}^3$

$$\sigma' = \sigma_{tot} = 19.81(6.1) = 120.8 \text{ kPa}$$

(c) Part "b" in fps units:

$$\sigma' = \sigma_{tot} = \frac{19.81}{9.807}(62.4)(\frac{6.1\times3.2808}{1000}) = \frac{2.52 \text{ k/sq ft}}{1000}$$